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Lowering the Energy Threshold of the CUORE Experiment: Benefits in the Surface Alpha Events Reconstruction:

Comparison Between Optimum Trigger and Derivative Trigger Performance in the Search for 0 $\nu\beta\beta$

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Abstract

CUORE is a tonne-scale cryogenic experiment located at the Laboratori Nazionali del Gran Sasso that exploits bolometric

technique to search for

neutrinoless double beta decay of $^{130}\mathrm{Te}$. Thanks to its very low background and large mass, CUORE is also a powerful tool to study a broad class of phenomena,

such as solar axions and WIMP scattering. The ability to conduct such sensitive searches crucially depends on the energy threshold, which has to be kept as low—as possible. In this contribu-tion, we show how the trigger algorithm affects the sensitivity to low-energy phe-nomena and the interpretation of the energy spectrum. In particular, we focus on the impact that the trigger algorithm has—on—the identification of the coincidence events among different crystals and, consequently, on the reconstruction of the background.

1 CUORE Experiment

Neutrinoless double beta decay (0vf]f[1]) is a rare, second-order nuclear transition in which an initial nucleus (A, Z) decays to a member (A, Z + 2) of the same iso-baric multiplet with the simultaneous emission of two electrons. In the attempt to investigate the nature of the 0vf]f[1] various theoretical possibilities were considered; however, the general interest has remained focused on the neutrino mass mechanism. 0vf]f[1] is forbidden by the Standard Model and explicitly violates the lepton number by two units. Its observation would thus prove that the lepton number is not a conserved quantity, and it would also provide us with precious information on the neutrino mass nature and scale. The experimental signature 0vvf[f]f[1] is a

monoenergetic peak at the Q-value of the decay, considering the summed energy spectrum of the two emitted electrons. The candidate isotopes that could undergo 0v/3/3 are even-even nuclei for which single beta decay is energetically forbidden.

The Cryogenic Underground Observatory for Rare Events (CUORE) is an experiment located at the LNGS, Italy, searching for the $0\nu/3/3$ of 130 Te. This isotope has the highest natural isotopic abundance (34.2% [2]) among the nuclei of inter- est. CUORE exploits the bolometric technique to get a high resolution around the

0v/3/3 O-value (~ 2527.5 keV [3]). The detector consists of an

S. J. Freedman: Deceased.

array of 988 natural- TeO_2 cubic crystals [4], for a total active mass of 742 kg (\sim 206 kg of ^{130}Te).

A bolometer is a sensitive calorimeter that measures the energy deposited by a

particle interaction via increase in the temperature of the absorber. CUORE has three Each bolometer fundamental components: an energy absorber, i.e., the crystal itself; a temperature sensor, a neutron-transmutation-doped germanium tor that converts the temperature rise into a voltage pulse; and a weak thermal link to the copper frame, which acts both as the structural support and thermal bath to restore the reference temperature. By measuring the signal amplitude, we can recon- struct the amount of energy released. At an operating temperature of 10 mK, the

typical TeO_2 heat capacity gives a temperature increase of ~ 100 µK per MeV and a signal amplitude of 1 V per MeV. The actual CUORE working temperature is a

compromise between a maximal thermal gain and an optimized signal bandwidth. CUORE is operated at cryogenic temperatures by mean of a powerful custom ³

He/ 4 He dilution refrigerator [5]. The dimensions, namely an experimental volume of $\sim 1~\text{m}^3$ and a mass of 17 tonnes, make the CUORE cryostat the largest dilution refrigeration in operation. The cryostat design and construction had to respect very stringent experimental constraints: an effective mechanical insulation, with extremely low vibration levels, and minimal contribution to the radioactive back-

ground for the experiment. In particular, in order to suppress the y and neutron back- ground, two lead shields have been integrated into the cryogenic volume and a lead

+ polyethylene shield surround the whole cryostat.

The analysis of the data from CUORE-0, a prototype detector equivalent to a single CUORE tower operated as a standalone experiment [6], together with an extensive radio-assay measurement campaign of the materials used for CUORE construction, allowed us to identify the main background sources in the 0v/3/3 region of interest (ROI) and to build a Monte Carlo simulation to estimate the expected background index [7]. This is $[1.00 \pm 0.03 \, (\text{stat.})^{+0.23} \, (\text{syst.})]10^{-2}$ -0.10 counts keV⁻¹ kg⁻¹ $vear^{-1}$.

The installation of the CUORE towers inside the cryostat was performed during summer 2016, and we could start the data taking in April 2017.

2 Data Processing: Derivative and Optimum Trigger

The voltage crossing the thermistor of each bolometer is continuously acquired with a sampling frequency of 1 kHz. A single

event is contained in a 10-s window: a 3-s pretrigger gives a measurement of the bolometer temperature, while the 7 s-pulse gives the amount energy release, since this is proportional to its amplitude. We also

analyze waveforms that do not contain visible pulses to monitor and model our detector noise behavior. Moreover, each crystal is instrumented with a silicon heater, so that we are able to periodically inject stable voltage pulses with precise and fixed energy in order to correct for possible variation in the detector response.

During the online data acquisition, we save continuous detector waveforms and separately trigger them with a software derivative trigger. This algorithm acts on the rising edge of a pulse: a trigger is fired when the derivative of the pulse stays above a certain threshold for a minimum number of consecutive samples. This threshold depends on the noise RMS of the individual bolometers.

In order to study low-energy events, we developed an optimum trigger, which runs in parallel to the derivative one [8, 9]. We then retriggered all the runs since the beginning of the data taking, using the new algorithm. The optimum trigger is a low threshold trigger based on the optimum filter [10] that maximizes the signal-to-noise ratio exploiting the distinct power spectra of particle-induced and noise waveforms. Each pulse transfer function is matched to the signal shape so that pulses with a dif-ferent trend in time are suppressed. We get:

$$H(w_k) = h \frac{s^*(w_k)}{N(w_k)} e^{-jw_k i}$$
(1)

where $s(w_k)$ is the discrete Fourier transform of the signal, $N(w_k)$ the noise power spectrum, i_M the position of the maximum of the signal in the acquisition window, and h a normalization factor to leave the signal amplitude unchanged. The data buffer is divided into sections that are continuously filtered in the frequency domain with the optimum filter. Once the optimum filter transfer function is built, the base- line is filtered. A trigger threshold, based on the filtered noise RMS, is then applied to properly identify particle events. An example of low-energy event triggered with the optimum trigger is shown in Fig. 1.

2.1 Trigger Efficiency Evaluation

As a figure of merit for the quality of energy thresholds obtained with a given trig- ger procedure, we use the 90% of the trigger efficiency. We acquire a test run during which we fire multiple heater pulses at different (known) amplitudes on each bolom- eter. These data are then processed to reconstruct the energy of pulser

Raw data

100

iltered data

200

300

400

500 600 sample index

events that are

Fig. 1 Window containing a pulse with reconstructed energy of 3 keV. The pulse after the

application of the optimum filter is shown in red (Color figure online)

measured. For each bolometer and each pulser amplitude, we compare the number of detected pulser events to the number of events generated. The detection efficiency is estimated as the ratio of the former over the latter. We fit the efficiency as a func- tion of the pulser energy using the error function (sigmoid shape) and invert it to evaluate the function at the 90% efficiency. This is the value of the energy threshold. We apply this procedure to both derivative and optimum trigger and then com- pare the threshold distribution on the whole CUORE detector. In the final steps of the analysis chain (Sect. 3), in order to select events in the energy spectrum for the 0v/3/3 search, we set an analysis threshold common to all bolometers. This choice is specifically meant for the 0v/3/3 analysis both with the aim to minimize the back- ground contribution in the region of interest (55 keV around $Q_{(3/3)}$) from the 2615 keV ²⁰⁸Tl line, and to ensure that we preserve a trigger efficiency > 90% for the majority of detectors. The value for this common threshold is 150 keV for derivative trigger (purple line in Fig. 2), and 40 keV with optimum trigger (green line).

3 CUORE Analysis Chain and Coincidence Identification

The CUORE data analysis consists of a series of following steps that are performed by using a modular software specifically designed for the experiment.

Initially, the pulse amplitude is estimated by the optimum filter algorithm described in the previous section as the maximum value of the filtered waveform. The signal amplitude is then stabilized against thermal drifts, while the calibration is applied referring to y lines from $^{232}{\rm Th}$ and $^{60}{\rm Co}$ sources. Once the energy of physical events is reconstructed, a series of cut is applied to the pulse in order to reliably identify 0v/3/3 candidate events. In addition, noisy periods of data taking

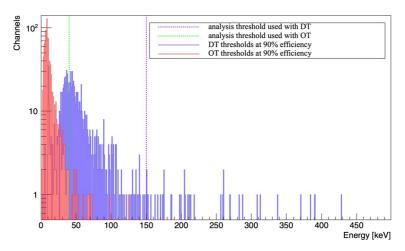


Fig. 2 Distribution of the energy threshold at 90% detection efficiency. Analysis threshold for both trig- ger configurations is indicated by the vertical lines (Color figure online)

are removed from the analysis and pulses whose shape is not consistent with a true particle-interaction are rejected.

Since we expect from the CUORE Monte Carlo simulations that the largest fraction of the 0vfff events (\sim 88%) will release the whole energy in the same crystal, we apply an anti-coincidence cut that excludes a particles and multiple-Compton

scatterings. We assign a value of *multiplicity*, M, to each event. This parameter indi- cates the number of crystals interested by the same particle process (within a certain time window). In order to identify the true time difference between two signals, the channels (bolometers) are synchronized using a double correction based both on the time difference between simultaneous events occurring on different towers (i.e., pul-ser events) and on the intrinsic jitter that exists between physically coincident multidetector events (e.g., events that sum at 2615 keV, energy of the 208 TI line from the 232 Th, during calibration). We set a coincidence window width of 10 ms (\pm 5 ms).

As mentioned in the previous section, lowering the trigger thresholds has an impact on the energy range of particle interactions we can probe. Our capability to detect low-energy events considerably increases our efficiency of reconstructing events with energy release in more than one bolometer, i.e., events with multiplicity larger than 1.

Disentangling M_1 and $M_{x\geq 2}$ interactions improves our background reconstruction ability.

Let us focus on the events that populate the M_2 spectrum, referring to Fig. 3. For the purpose of this analysis, we order the energy of coincident events so that, by definition, $E_1 < E_2$, w hile the derivative and optimum trigger a nalysis thresholds (150 and 40 keV, respectively) are reported to highlight the energy region that can-

not be investigated. As the derivative analysis threshold completely excludes nuclear recoils from a-decay coincidence reconstruction, we will not consider this constrain in the following discussion. Each bolometer will contribute with its own energy threshold, as shown in Sect. 2. The clustering of events along lines with negative

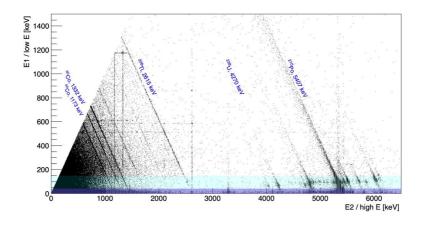


Fig. 3 Multiplicity 2 events scatter plot. $E_1 < E_2$ always. Light blue (blue) box represents derivative (optimum) trigger analysis threshold. The energy of the main y and lines is superimposed (Color figure online)

slope collect coincident particle events on two bolometers with $E_1 + E_2 = E_{\rm peak}$, where $E_{\rm peak}$ corresponds to a known y - or -line, e.g., the 208 Tl photopeak. The clus- tering along vertical lines, i.e., $E_2 = E_{\rm peak}$, while E_1 can have any positive value, cor- responds to accidental coincidences in most of the cases, that is to say uncorrelated interactions involve different crystals within the same time window. This can interest lines in the spectrum such as the 60 Co y s at 1173 and 1332 keV, or the decays of the 238 U and 232 Th chains, such as 210 Po, that has the highest intensity ($Q_{\rm value} = 5407$ keV) (Fig. 4).

The energy region above the ²⁰⁸Tl line is mainly populated by events originated by contaminants of the TeO₂ crystals (i.e., of the detector itself) and of the detector holder (mostly copper frames). In this region, the dominant background comes from decaying isotopes from the ²³⁸U and ²³²Th decay chains, particles travel extremely short distances inside matter before they are absorbed (a 5 MeV has a range of about 10 µm in copper); therefore, if such an event is seen by the detector, the contaminant has to be in the close proximity of the detector (indeed inside the crystal or the holder surface). If the contaminant is inside the bulk of a crystal, both the particle and the recoiling nucleus deposit their energy inside it. Such an event has multiplicity 1 and energy equal to the decay O-value. On the other hand, if the contaminant lies on the crystal surface, the emitted can leave the crystal. If the same particle is then absorbed by another neighboring crystal, an M_2 event is generated: one crystal triggers on the particle, the other on the recoiling nucleus. Events of this kind can be easily identified fixing a constrain on the sum of the energies that should match the Q_{value} of the decay. They are schematically pictured in Fig. 5. As an example, the raw waveforms of both the particle and the recoiling nucleus for a typical M_2 event are also shown.

Typically, the nuclear recoil decreases the total energy of the decay peak by

 \sim (70–150) keV. This means that the analysis threshold has a strong impact on its detection. Alpha particles and nuclear recoils from the 210 Po decay in the M_2 spectrum reconstruction are shown in Fig. 6: while the particle is detected with

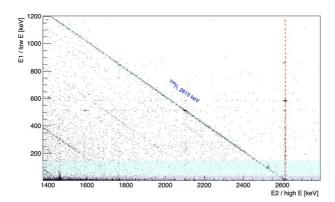


Fig. 4 Zoom around thallium photopeak (2615 keV) of Fig. 3. The green line represents physical coincidences at 2615 keV ($E_1+E_2=2615$ keV), and the red one indicates accidental coincidences ($E_2=2615$ keV, E_1 any positive value) (Color figure online)

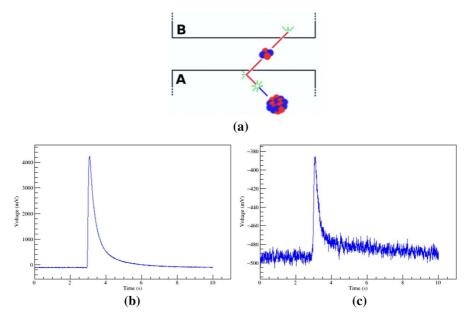


Fig. 5 a Schematic representation of the processes populating the alpha and recoil peaks in multiplicity 2 spectrum. A and B are two CUORE bolometers. **b**, **c** Are the raw pulses of a typical M_2 event coming from alpha decay; **b** is the particle waveform and **c** the nuclear recoil waveform (Color figure online)

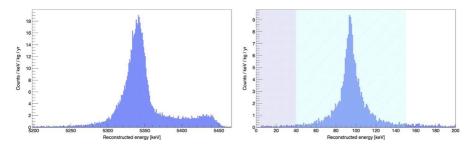


Fig. 6 Alpha particle (left) and nuclear recoil (right) from ²¹⁰Po decay. Light blue (blue) box represents derivative (optimum) trigger analysis threshold (Color figure online)

both the derivative and optimum trigger analysis, the 150 keV threshold com- pletely prevents the observation of the daughter nuclei events. As a consequence, physical M_2 events wrongly end up in M_1 spectrum.

Moving from derivative to optimum trigger analysis, we expect a considerable

improvement in our efficiency in M_2 reconstruction, especially in the region of the spectrum. This is highlighted in Fig. 7. In fact, events in M_1 spectrum move to M_2 when passing from the derivative (*blue*) to optimum (*red*) trigger analy- sis. Again, we consider the 210 Po particle and compare M_1 and M_2 spectra. To

exclude accidentals from the second, we apply an arbitrary cut on the sum of the $\,$

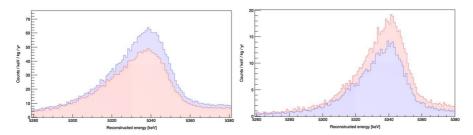


Fig. 7 M_1 (left) and M_2 (right) spectrum comparison in the region of the particle from 210 Po decay. His- tograms in blue (red) are referred to derivative (optimum) trigger analysis (Color figure online)

events energy, i.e., $E_1 + E_2 = Q_{\text{value}} \pm L$. L is set to 70 keV as it is enough to properly include both the alpha particle and the nuclear recoil events.

It is worth to underline that this analysis was performed with cuts specifically optimized for the 0v/3/3 search (Sect. 2). Using a channel-dependent thresh- old (Fig. 2), recoil peaks from surface alpha decays would be visible for a fraction of channels also with the derivative trigger. However, setting a common analysis threshold significantly simplifies the analysis from a technical point of view. Fur- thermore, having access to the low-energy region is helpful both for the background reconstruction and the comprehension of CUORE in general: the spectrum below 40 keV helps us in the reconstruction of X-rays from 130 Te and also X-rays from both copper and lead contaminations [11].

Extending this analysis to other background sources, we can fix a constraint on the contributions due to contaminants at the crystals surface. This helps us identify- ing contributions to the region of the spectrum due to other contaminants, inside the bulk of crystals or at the holder surface. Thus, improving our background model, we can extract with higher accuracy an estimate of our background index in the region of interest for the 130 Te 0v/3/3.

4 Conclusions and Outlook

The analysis presented shows only a small fraction of the overall improvement we can obtain by using the optimum trigger in the reconstruction of the low-energy spectrum. Besides representing a powerful tool to increase the precision of our back- ground model, the optimum trigger can help us improve the 0v/3/3 search by includ- ing events in which the electrons release energy in multiple crystals.

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