

## Società Italiana di Statistica

# Proceedings of the XLVI Scientific Meeting

## SAPIENZA UNIVERSITY OF ROME June 20-22, 2012

Plenary sessions Invited sessions Contributed sessions

ISBN 978 88 6129 882 8



## SIS SCIENTIFIC MEETING 2012

## PRESENTATIONS AND AUTHORS

## **BROWSE PAPERS BY SECTION**

### PLENARY

Research advances and new challenges in Cluster Analysis Maurizio Vichi Handling Measurement Error in Survey Estimation using Accuracy Indicators PAPER NOT AVAILABLE Chris Skinner Integrating micro and macro data in historical demography PAPER NOT AVAILABLE Marco Breschi SPECIALIZED A Bayesian nonparametric model for count functional data Antonio Canale, David B. Dunson ROI analysis of pharmafMRI data: an adaptive approach for global testing Giorgos Minas, John A.D. Aston, Thomas E Nichols, Nigel Stallard Distance - Based Statistics for Covariance Operators in Functional Data Analysis Davide Pigoli Clustering Multivariate Longitudinal Data: Hidden Markov of Factor Analyzers Antonello Maruotti, Francesca Martella Model based clustering of multivariate spatio-temporal data: a matrix-variate approach Cinzia Viroli Random coefficient based dropout models: a finite mixture approach Alessandra Spagnoli, Marco Alfò Bayesian inference for causal effects in randomized experiments with noncompliance: The role of multivariate outcomes Fan Li, Alessandra Mattei, Fabrizia Mealli Unconditional and Conditional Quantile Treatment Effect: Identification Strategies and Interpretations Margherita Fort Dealing with complex problems of confounding in mediation analysis Stiin Vansteelandt A Unified Approach for Defining Optimal Multivariate and Multi-Domains Sampling Designs Pietro Demetrio Falorsi, Paolo Righi Forest Inventories: Multi-Phase Sampling Strategies for Estimating Forest and Non-Forest Resources Over Large Areas Lorenzo Fattorini Recent Advances in Estimation of Poverty Indicators for Domains and Small Areas Risto Lehtonen, Ari Veijanen Weighted likelihood in Bayesian inference Claudio Agostinelli, Luca Greco Disclosure risk estimation via nonparametric log-linear models Cinzia Carota, Maurizio Filippone, Roberto Leombruni, Silvia Polettini Bayesian Latent Class Models in Veterinary and Human Epidemiology Luzia Goncalves, Ana Subtil, Nuno Brites, M. Rosario de Oliveira, Ana Margarida Alho, Jose Meireles, L. M. Madeira de Carvalho, Silvana Belo STAR modeling of pulmonary tubercolosis delay-time in diagnosis Bruno de Sousa, Dulce Gomes, Patricia A. Filipe, Cristina Areias, Teodoro Briz, Carla Nunes ROC Curves in medical decision Ana Cristina Braga, Lino Costa, Pedro Oliveira On Dividing an Empirical Distribution into Optimal Segments Jan W. Owsiński A composite indicator of sustainable well-being: the relative importance of weights in the European Strategy for Sustainable Development Elena Giachin Ricca, Stefano Tarantola Non-aggregative assessment of subjective well-being Marco Fattore On the Extraction of a Common Persistent Component from Several Volatility Indicators Fabrizio Cipollini, Giampiero M. Gallo Estimating jumps in volatility using realized-range measures Massimiliano Caporin, Eduardo Rossi, Paolo Santucci de Magistris The Value of Model Sophistication: DJIA Option Pricing Jeroen V.K. Rombouts, Lars Stentoft, Francesco Violante Families in Italy: the Quiet Revolution Silvana Salvini, Gustavo De Santis

Enterprise in a globalised context and public and private statistical setups Fabrizio Guelpa, Giovanni Foresti, Stefania Trenti Imputation and outlier detection in banking datasets Andrea Pagano, Domenico Perrotta, Spyros Arsenis Something for nothing? Shirlev Coleman On consistency of Bayesian variable selection procedures Elias Moreno, Javier Giron, George Casella, Lina Martinez, F. Vazquez-Polo, Maria Martel Dynamic Classification Trees for imprecise data Massimo Aria, Valentina Cozza An innovative procedure for smoothing parameter selection Gianluca Frasso, Paul Eilers The Italian Statistical Institute Macroeconometric Model - MEMo-It Fabio Bacchini, et al. A statistical overview of the economic situation in the euro area Gian Luigi Mazzi, Filippo Moauro, Rosa Ruggeri Cannata M-Estimation of Shape Matrices under Incomplete and Serially Dependent Data PAPER NOT AVAILABLE Gabriel Frahm Convergence of Depths and Depth-Trimmed RegionsPAPER NOT AVAILABLE Rainer Dyckerhoff On Robustifying Some Blind Source Separation Methods for Second Order Nonstationary DataPAPER NOT **AVAILABLE** Klaus Nordhausen The impact of the three crises on health in Italy: evidence and lack of adequate information systems Giovanni Fattore LISA map based on distances for functional data PAPER NOT AVAILABLE Pedro Delicado, Sonia Broner Smoothing mortality risks in space and time using flexible modelsPAPER NOT AVAILABLE Maria Dolores Ugarte, Toma Goicoa, Jaione Etxeberria, Ana F. Militino Economic recession and fertility in the developed world: Past evidence and recent trendsPAPER NOT AVAILABLE Tomas Sobotka Generalized boosted additive models Sonia Amodio, Jacqueline Meulman

### SOLICITED

Which family model makes couples more happy - dual earner or male breadwinner ? Anna Baranowska-Rataj, Anna Matysiak Socioeconomic determinants of persistence in poor subjective health Paolo Li Donni, Daria Mendola Family structures and subjective wellbeing in Italy Silvia Montecolle, Francesca Rinesi, Alessandra Tinto Identifiability of Discrete Graphical Models with Hidden Variables Marco Valtorta, Elizabeth S. Allman, John A. Rhodes Identifiability of hierarchical loglinear models with one hidden binary variable Barbara Vantaggi Binary models of marginal independence: a comparison of different approaches Monia Lupparelli, Luca La Rocca Small Area Estimation with Uncertain Random Effects Gauri Sankar Datta, Abhyuday Mandal, Anthony Wanjoya Interacting Multiple Try Algorithms Roberto Casarin, Radu Craiu, Fabrizio Leisen Higher-order asymptotics in Bayesian inference Laura Ventura, Walter Racugno Online Detection of Outliers and Structural Breaks Giovanni Petris Estimating the prevalence of cancer patients who have recurred Angela B. Mariotto, Roberta De Angelis, Lucia Martina Multivariate Permutation Test to Compare Survival Curves for Matched Data Stefania Galimberti Patterns of care and related costs of cancer prevalent cases by phase of disease Silvia Francisci, Anna Gigli Estimating the incidence of cancer disease using a Bayesian backcalculation approach Leonardo Ventura Bayesian T-optimal designs by simulation: a case-study on model discrimination Rossella Berni, Federico M Stefanini From Markov moves in contingency tables to linear model estimability Roberto Fontana, Fabio Rapallo, Maria Piera Rogantin Sensitivity Analysis and FANOVA Graphs for Computer Experiments Jana Fruth, Sonja Kuhnt Factorial Graphical Lasso and Slowly Changing Graphical Models for Estimating Dynamic Networks Antonino Abbruzzo, Ernst Wit New Statistics for Estimating the Parameter of the Stochastic Actor-Oriented Model Viviana Amati Graph embedding via dissimilarity mapping for network comparison Domenico De Stefano

Statistical models for virtual water network analysis Alessandra Petrucci, Emilia Rocco Latent Class CUB Models Leonardo Grilli, Maria Iannario, Domenico Piccolo, Carla Rampichini Formative and reflective models to determine latent construct Anna Simonetto Log-ratios analysis to study the relative information of ordinal variables Michele Gallo Ordinal Models for Financial Evaluation Paola Cerchiello Bayesian model averaging for financial evaluation Silvia Figini Labour market response models for university evaluation Daniele Checchi, Silvia Salini A Statistical Framework to Measure Reputation Risk Tiziano Bellini, Luigi Grossi The integration of administrative data to analyse the business economic performance: methodological aspects and results of a study Fulvia Cerroni, Viviana De Giorgi, Marianna Mantuano The micro economics of trade patterns and firm performances Giovanni Dosi, Marco Grazzi, Federico Tamagni, Chiara Tomasi The post-entry effect of exporting on productivity: inference on the conterfactual distribution Maria Ferrante, Marzia Freo, A. Viviani Data Integration and Productivity Estimation at a Firm Level Filippo Oropallo, Stefania Rossetti A PLS algorithm version working with ordinal variables Giuseppe Boari, Gabriele Cantaluppi Bivariate logistic models for the analysis of the Students University "Success" Marco Enea, Massimo Attanasio University admission test and students' careers: an analysis through a regression chain graph with a hurdle model for the credits Leonardo Grilli, Carla Rampichini, Roberta Varriale Comparing degree programs using unadjusted performance indicators. Assessing the bias from the Potential Confounding Factors Mariano Porcu. Isabella Sulis University of Pisa and academic performance: a sample survey on students with no exams in 2011 Lucio Masserini, Monica Pratesi Assessing the Impact of Financial Aids to Firms: Causal Inference in the presence of Interference Bruno Arpino, Alessandra Mattei Inverse probability weighting to estimate causal effects of sequential treatments: a latent class extension to deal with unobserved confounding Francesco Bartolucci, Leonardo Grilli, Luca Pieroni A two-part geoadditive model for geographical domain estimation Chiara Bocci, Alessandra Petrucci, Emilia Rocco Application of Marginal Structural Models in Chronic Kidney Disease (CKD) Epidemiology: practical implementation in the Swedish National CKD Registry Elena Pasquali, Marie Evans, Juan Jesus Carrero, Rino Bellocco A Dimension Reduction Method for Approximating Integrals in Latent Variable Models for Binary Data Silvia Bianconcini, Silvia Cagnone, Dimitris Rizopoulos Kalman Filter for Maximum Likelihood Estimation of GMRFs Luigi Ippoliti, Luca Romagnoli Monte Carlo Likelihood Inference in Multivariate Model-Based Geostatistics Marco Minozzo, Clarissa Ferrari Statistical Modelling of Spatial Extremes Anthony Davison, Simone Padoan, Mathieu Ribatet Nonparametric smoothing of circular data Agnese Panzera, Charles C. Taylor Inverse Batschelet Distributions as Models for Circular Data Arthur Pewsey Depth Analysis of Directional Data Claudio Agostinelli, Mario Romanazzi Simulation of random rotation matrices John T. Kent, Asaad M. Ganeiber Dynamically modelling of fuzzy sets for flexible data retrieval Miroslav Hudec Factor PD-Co-clustering in Official Statistics Marina Marino, Germana Scepi, Cristina Tortora Extracting meta-information by using Network Analysis tools Agnieszka Stawinoga, Maria Spano, Nicole Triunfo How the text mining measures complex phenomena in official statistics Sergio Bolasco, Pasquale Pavone Assessing assumptions for data fusion procedures Alfonso Piscitelli, Antonio D'Ambrosio Filling in long gap sequences by performing EOF and FDA jointly Antonella Plaia, Francesca Di Salvo, Mariantonietta Ruggeri, Gianna Agrò Missing Data Imputation within the Statistical learning Paradigm Antonio D'Ambrosio The use of adminitrative registers in the 2011 Census in Germany PAPER NOT AVAILABLE Stephanie Hirner Robust methods for correction and control of Italian Agriculture Census data PAPER NOT AVAILABLE

Alessandra Reale, Francesca Torti, Marco Riani

The industry and services continuous census" based on administrative sources: opportunities and problems PAPER NOT AVAILABLE Manlio Calzaroni, Caterina Viviano Using coarse resolution satellite images for crop area estimation: benchmarking their efficiency Javier Gallego, Mohamed El-Avdam How to select sample sites onto a study area? Lucio Barabesi, S. Franceschi, M. Marcheselli Do personal characteristics affect the Rasch measures of perceived physical risk? A quantile regression approach. Fabio Aiello, Giovanni Boscaino, Monica Mandalà Modeling nonignorable missingness in multidimensional latent class IRT models Silvia Bacci, Francesco Bartolucci, Bruno Bertaccini Risk profile versus portfolio selection: a case study Valeria Caviezel, Sergio Ortobelli Lozza, Lucio Bertoli Barsotti Cycles Syllogisms and Semantics: Examining the Idea of Spurious Cycles Stephen Pollock Spectral filtering for trend estimation Marco Donatelli, Alessandra Luati, Andrea Martinelli Robust estimation for multivariate data under the independent contamination model Claudio Agostinelli, R. A. Maronna, V. J. Yohai Adaptive robust location-scale estimation Pietro Coretto Minimum Volume Peeling: a Multivariate Mode Estimator Giovanni Porzio, Giancarlo Ragozini, Steffen Liebscher, Thomas Kirschstein A comparison of robust methods with small sample experimental data Marco Riani, Andrea Cerioli, Maria Adele Milioli, Gianluca Morelli Patterns of Mortality Decline and Individual Ageing: An Overview Elisabetta Barbi Survival predictive models in centenarians PAPER NOT AVAILABLE Rossella Miglio, Paola Gueresi Health status in over 85 years old living in Residential Facilities in Italy PAPER NOT AVAILABLE Giulia Cavrini, Claudia Di Priamo, Lorella Sicuro, Alessandra Battisti, Alessandro Solicapa, Giovanni de Girolamo CONTRIBUTED

Variation in Obstetric Intervention Rates across Hospitals in Sardinia Massimo Cannas, Emiliano Sironi On the role of normalized inverse-Gaussian priors in continuous-time models Matteo Ruggiero Randomly Reinforced Urn Designs whose Allocation Proportions Converge to Arbitrary Prespecified Values Giacomo Aletti, Andrea Ghiglietti, Anna Maria Paganoni Calibration estimation in dual frame surveys Maria Giovanna Ranalli, Annalisa Teodoro Comparing model-assisted estimators of structural variables in forest surveys Ivan Arcangelo Sciascia, Matteo Garbarino, Giorgio Vacchiano, Renzo Motta A study in panel cointegration and poolability: Long-run money demand equations for Gulf Cooperation Council countries Stefano Fachin Uncertainty in statistical matching for discrete categorical variables Pier Luigi Conti, Daniela Marella, Mauro Scanu Independent Component Analysis of Milan Mobile Network Data Paolo Zanini, Piercesare Secchi, Simone Vantini An Objective Bayesian analysis of dichotomous sensitive data Maria Maddalena Barbieri, Brunero Liseo Ensuring comparability over time and between domains by means of complex sample techniques Tiziana Tuoto, Francesca Inglese Confidence intervals for the Berger & Boos' procedure in the 2x2 Binomial Trial Enrico Ripamonti, Piero Ouatto Kalman Filter for Maximum Likelihood Estimation of GMRFs Luigi Ippoliti, Luca Romagnoli Bayesian inference for the multivariate skew-normal model: a Population Monte Carlo approach Antonio Parisi, Brunero Liseo Reconstructing a multinormal covariance matrix from its spherically truncated projection Filippo Palombi, Simona Toti, Romina Filippini Clustering of financial time series in extreme scenarios Roberta Pappadà, Fabrizio Durante Investments in Renewable energies: evidence from a panel of countries Giuseppe Scandurra A Topological Definition of Phase and Amplitude Variability of Functional Data Simone Vantini Nonparametric saddlepoint test and pairwise likelihood inference Nicola Lunardon, Elvezio Ronchetti On the stationarity of the Threshold Autoregressive process: the two regimes case Marcella Niglio, Francesco Giordano, Cosimo Damiano Vitale Filling in long gap sequences by performing EOF and FDA jointly Francesca Di Salvo, Mariantonietta Ruggieri, Gianna Agro' Parallel Adaptive Markov chain Monte Carlo with applications

Mauro Bernardi, Lea Petrella Modern Bayesian Inference in Zero-Inflated Poisson Models Erlis Ruli, Laura Ventura A comparison of different procedures for combining high-dimensional multivariate volatility forecasts Giuseppe Storti, Alessandra Amendola Estimation of wind speed prediction intervals by multi-objective genetic algorithms and neural networks Valeria Vitelli On a predictive measure of discrepancy between classical and Bayesian estimators Stefania Gubbiotti A prediction error for a linear regression model with fuzzy random elements Maria Brigida Ferraro Some further results for the two-parameter Poisson-Dirichlet partition model Annalisa Cerquetti Matching immigrant and native workers: evidence from the recent downturn in Italy Adriano Paggiaro The analysis of firm demography: an approach based on micro-geographic data Diego Giuliani, Simonetta Cozzi, Giuseppe Espa Regression estimators for capure-recapture frequency data Irene Rocchetti Towards an integrated surveillance system of road accidents Tiziana Tuoto, Silvia Bruzzone, Luca Valentino, Giordana Baldassarre, Nicoletta Cibella, Marilena Pappagallo On the Design Based Inference for Continuous Spatial Populations Giorgio Eduardo Montanari, Giuseppe Cicchitelli A Critical Look at Compositional Analysis for Assessing Habitat Selection Caterina Pisani Small area estimation for panel data Annamaria Bianchi Interpreting Deviations from Long-run Parity in an I(2) Model Giuliana Passamani Contributions from income components to Zenga's point and synthetic inequality measures: an application to EU countries Michele Zenga, Leo Pasquazzi An income mobility measure based on Zenga's inequality index Mauro Mussini Equivalence scales, inflation, and PPP: a unique (and simple) approach to estimation Gustavo De Santis Sensitivity analysis on a Cellular Automata model for the diffusion of Pleural Mesothelioma Claudia Furlan, Cinzia Mortarino Reproducibility Probability Estimation and Testing for some common nonparametric tests Daniele De Martini, Lucio De Capitani Multilevel algorithmic models to measure item importance on latent variables' indicators Marica Manisera, Marika Vezzoli A multiple imputation procedure of censored values in family-based genetic association studies Fabiola Del Greco M., Cristian Pattaro, Cosetta Minelli, Peter P. Pramstaller, John R Thompson Ridge analysis through profile likelihoods Valeria Sambucini, Ludovico Piccinato Migrant students classroom allocation policy in Italian schools Andrea Scagni Testing Phase and Amplitude Variability in Functional Data Analysis: a Hierarchical Permutation Test Approach Alessia Pini, Simone Vantini A hierarchical bayesian model for modelling benthic macroinvertebrates densities in lagoons Serena Arima, Alberto Basset, Giovanna Jona Lasinio, Alessio Pollice, Ilaria Rosati Life-Course Transitions, Market Work and Domestic Work of Italian Couples Antonino Di Pino Adjusting Time Series of Possible Unequal Lengths Ilaria Lucrezia Amerise, Agostino Tarsitano Variable selection in competing risks model Marialuisa Restaino, Alessandra Amendola A Bayesian Semiparametric Fay-Herriot-type model for Small Area Estimation Silvia Polettini Assessing Multivariate Measurement Systems in Multisite Testing Michele Scagliarini, Stefania Evangelisti Predicting EQ-5D responses from SF-12: should we take into account dependece and ordering? Caterina Conigliani, Andrea Tancredi, Andrea Manca Large sample properties of Gibbs-type priors Pierpaolo De Blasi, Antonio Lijoi, Igor Pruenster Bayesian Unit Root Tests: a Monte Carlo Study Margherita Gerolimetto, Isabella Procidano Data fusion in pharmaceutical marketing: new perspective from administrative data. Paolo Mariani How internal and international migrations shape the age structure of the Italian regions, 1955-2008 Paola Di Giulio, Cecilia Reynaud, Luca Vergaglia Bayesian modeling of presence-only data Fabio Divino, Giovanna Jona Lasinio, Natalia Golini An Evaluation of the Student Satisfaction based on CUB Models Barbara Cafarelli Limited Information Estimation Methods for Paired Comparison Data

Manuela Cattelan Closed Likelihood-Ratio Testing Procedures to Assess Similarity of Covariance Matrices Francesca Greselin, Antonio Punzo Fiducial Distributions for Real Exponential Families Piero Veronese, Eugenio Melilli Hedonic Indexes and GDP estimate in the USA Gabriele Serafini Some results on stochastic comparisons of ROC curves Silvia Figini, Chiara Gigliarano, Pietro Muliere Efficiency in the use of natural non-renewable resources from mining and quarrying in Italy. Time series analysis and Economy-wide Material Flows Accounts Donatella Vignani Marital Disruption and Subjective Well-being: Evidence from an Italian Panel Survey Giulia Rivellini, Alessandro Rosina, Emiliano Sironi The Decision Making Process of Leaving Home: A Longitudinal Analysis of Italian Women Giulia Ferrari, Alessandro Rosina, Emiliano Sironi Alternative Bayesian analysis of capture recapture data with behavioral effect modelling Danilo Alunni Fegatelli PDE penalization for spatial fields smoothing Laura Azzimonti, Maurizio Domanin, Laura Maria Sangalli, Piercesare Secchi Multivariate Nonlinear Least Squares: Direct and Beauchamp and Cornell Methodologies Renato Guseo, Cinzia Mortarino Handling weak dependence structures with copulas Enrico Foscolo, Fabrizio Durante Bayesian nonparametric predictions for count time series Luisa Bisaglia, Antonio Canale How to integrate macro and micro perspectives: an example on Human Development and Multidimensional Poverty. Silvia Terzi Composite Indicator of Social Inclusion in the European Union Erasmo Vassallo, Francesca Giambona Depth measures for the study of real and simulated ECG signals Francesca Ieva Experimental design for the estimation of Rician-distributed intensity fields in MRI Stefano Baraldo, Francesca Ieva, Luca Mainardi, Anna Maria Paganoni A von Mises Markov random field model for the analysis of spatial circular data Francesco Lagona A Multivariate VEC-BEKK Model for Portfolio Selection Andrea Federico Pierini, Alessia Naccarato Combining the complete-data and nonresponse models for drawing imputations under MAR Shahab Jolani, Stef van Buuren, Laurence E, Frank A Well-being Index Based on the Weighted Product Method Matteo Mazziotta, Adriano Pareto A comparison of semiparametric density estimation methods for multivariate risk management Marco Bee Modelling poverty transitions in Luxembourg: true state dependence or heterogeneity? Alessio Fusco, Nizamul Islam Causal analysis of education and birth inequalities through a latent class SEM Silvia Bacci, Francesco Bartolucci, Luca Pieroni Prediction of nonstationary functional data: Universal Kriging in a Hilbert Space Alessandra Menafoglio, Matilde Dalla Rosa, Piercesare Secchi School tracking and equality of opportunity in a multilevel perspective Isabella Romeo, Emanuela Raffinetti Indexing the Worthiness of Social Agents Giulio D'Epifanio Asymptotic estimation of right and left kurtosis measures, with applications to finance Anna Maria Fiori, Davide Beltrami Ordinal Lorenz Regression with application in Customer Satifaction Surveys Emanuela Raffinetti A computational method to estimate sparce multiple Gaussian graphical models Rossella Onorati, Luigi Augugliaro, Angelo Marcello Mineo Deterministic or stochastic seasonality in daily electricity prices? Paolo Chirico Social capital and its impact on poverty reduction: measurement issues in logitudinal and cross-country comparisons. The case of UE. Isabella Santini, Anna De Pascale The diffusion of nuclear energy in the developing countries Alessandra Dalla Valle, Claudia Furlan A model for the joint distribution of income and wealth Markus Jantti, Eva Sierminska, Philippe Van Kerm Mothers with children aged 0-2 years: work/family reconciliation and support networks Cinzia Castagnaro, Alessandra Fasano, Antonella Guarneri A novel method for spatial smoothing Laura M. Sangalli, James O. Ramsay Poverty transitions in Italy Lucia Coppola, Davide Di Laurea, Daniela Lo Castro, Mattia Spaziani Spatial smoothing over non-planar domains Bree Ettinger, Simona Perotto, Laura M. Sangalli Lattice Models for the analysis of Urban Crime

Enrico di Bella, Luca Persico, Lucia Leporatti Family resources and cognitive decline among elderly in Italy Stefano Mazzuco The median of a set of histogram data Lidia Rivoli, Rosanna Verde, Antonio Irpino Estimating the Homeless Population through Indirect Sampling and Weight Sharing Method Claudia De Vitiis Rates for Bayesian estimation of location-scale mixtures of super-smooth densities Catia Luisa Scricciolo Data gathering for elusive population. The case of foreigners during the XV Italian Census. A focus on Prato Linda Porciani Immigrant entrepreneurship through the economic crisis in Italy Benedetta Cassani, Cristina Giudici, Roberta Rizzi International Mobility of University Students: the Italian case Domenica Fioredistella Iezzi, Mario Mastrangelo, Scipione Sarlo Chronological analysis of textual data and curve clustering: preliminary results based on wavelets Matilde Trevisani, Arjuna Tuzzi Exponential Random Graph Model for multivariate networks: an application in knowledge network analysis Domenico De Stefano, Susanna Zaccarin The Role of Social Capital in Preventing Irregural Work in Italian Regions Maria Felice Arezzo Bayesian model averaging for financial credit risk measurement Silvia Figini Considerations about the Quotient of two Correlated Normals Angiola Pollastri, Vanda Tulli Estimating Business Statistics from administrative data: a study on small and medium enterprises Orietta Luzi, Giovanni Seri, Viviana De Giorgi, Giampiero Siesto The Coverage Survey of the 6th Agricultural Census Matteo Mazziotta, Antonella Bernardini, Loredana De Gaetano, Lorenzo Soriani A Local Price Observatory - Price minimarket: innovations and additional knowledge about prices - The experience of Umbria Cristina Carbonari, Angiona Sabrina, Paradisi Francesca Frailty Multi-State Models based on Maximum Penalized Partial Likelihood Federico Rotolo, Catherine Legrand Reconciliation of Time Series according to a Growth Rates Preservation Principle Tommaso Di Fonzo A decision support system for duopolies with incomplete information Paola Vicard, Julia Mortera False discovery rate control and the dependence structure of test statistics Claudio Lupi Neural Network Approach Applied for Classification in Business and Trade Statistics Jana Juriová The analysis of the material deprivation of foreigners in Italy Anna Maria Milito, Annalisa Busetta, Antonino Mario Oliveri Effective Facebook population: the Italian case Cristiano Tessitore, Ester Macrì A Clustream strategy for Functional Boxplots on multiple streaming time series Antonio Balzanella, Elvira Romano New approach to the identification of the Inverse Weibull model Biagio Palumbo, Giuliana Pallotta Stochastic Frontiers Approach: an Empirical Analysis of Italian Environmental Spending Sabrina Auci, Annalisa Castelli, Donatella Vignani Estimating student learning value-added models from repeated cross-sections Dalit Contini Intergenerational Mobility and Gender Gap: Evidence from Mediterranean Countries Rosalia Castellano, Gennaro Punzo, Antonella Rocca The role of Istat territorial offices for data quality control in the 15th Population and Housing Census. The case of Tuscany Alessandro Valentini, Sabina Giampaolo Longitudinal patterns of financial product ownership: a latent growth mixture approach Francesca Bassi Measuring job quality: a composite indicator Giovanna Boccuzzo, Martina Gianecchini On Measuring Inequity in Taxation Between Groups of Tax Payers Achille Vernizzi, Simone Pellegrino, Maria Giovanna Monti Capital income inequality: evidences from ECHP data Francesca Greselin, Leo Pasquazzi, Ricardas Zitikis Note on a new generalization of the skew-normal distribution Valentina Mameli, Monica Musio Estimates of Foreign Trade Using Genetic Programming Miroslav Klucik Machine learning techniques for Propensity score matching with clustered data. A simulation study. Massimo Cannas, Bruno Arpino, Francesco Billari Impact of Audio Tools in Web Surveys Daniele Toninelli, Silvia Biffignandi Early-life circumstances and late-life income Omar Paccagnella, Christelle Garrouste A Simple Risk-Adjusted CUSUM chart for monitoring binary health data

Marco Marchi From theory to practice: a methodological proposal for operationalising and summarizing the concept of quality of work Marco Centra, Maurizio Curtarelli, Valentina Gualtieri Partners' income and decision making Lucia Coppola, Domenica Quartuccio Dealing With a Potential Bias in Estimating the Share of Discriminated Women Rosa Giaimo, Giovanni Luca Lo Magno Border surveys and Time Location Sampling (TLS): an application on incoming tourism in Sicily Stefano De Cantis, Mauro Ferrante The Use of Administrative Data for Short Term Business Statistics: Lessons from a Cross-Country Experience Ciro Baldi, Francesca Ceccato, Silvia Pacini, Donatella Tuzi Price transmission and market power in the food market Maria Caterina Bramati Data imputation processes based on statistical analysis: the case of Kosovo census data Marco Scarnò, Bekim Canolli, Servete Muriqi, Hisni Ferizi Dimension reduction for measuring the multidimensional demographic convergence Maria Rita Sebastiani Is financial fragility a matter of illiquidity? An appraisal for Italian households Marianna Brunetti Burnout, learning and self-esteem at school: an empirical study. Cristiana Ceccatelli Autocorrelated non-normal data in control charts Claudio Giovanni Borroni, Manuela Cazzaro, Paola Maddalena Chiodini Social welfare orderings of the Generalized-Lorenz Type: applications of an extended equivalence theorem Alessandra Giovagnoli Timely Indices for Residential Construction Sector Attilio Gardini, Enrico Foscolo Dimensions of well-being and their statistical measurements Carla Ferrara, Francesca Martella, Maurizio Vichi The diagnostics of the mean squared error of the Eblup in small area estimation models Renato Salvatore, Maria Chiara Pagliarella

-- SIS SCIENTIFIC MEETING 2012 --

## On a predictive measure of discrepancy between classical and Bayesian estimators

Pierpaolo Brutti, Fulvio De Santis and Stefania Gubbiotti

**Abstract** In the presence of prior information on an unknown parameter of a statistical model, Bayesian and frequentist estimates based on the same observed data do not coincide. However it is well known that, in many standard parametric problems, their discrepancy tends to be reduced as the sample size increases. In this paper we consider a measure of discrepancy,  $D_n$ , between a frequentist and a Bayesian point estimator and we study its predictive distribution. In some specific examples we analyze the main characteristics of this predictive distribution for increasing sample sizes. We also consider the use of the predictive density of  $D_n$  for the assessment of a prior distribution informativeness. Some explicit results are given for the normal model.

Key words: Clinical trials; Conflict between estimators; Predictive approach.

## **1** Introduction

Bayesian methods offer the theoretical framework for combining experimental data and pre-experimental information on an unknown parameter, that is formalized by a prior probability distribution. In the presence of prior information, frequentist and Bayesian procedures, such as point or interval estimates based on the same observed sample, do not coincide. However, in many standard parametric problems, the discrepancy between frequentist and Bayesian procedures tends to disappear as the sample size increases. This is typically shown in most of introductory books on Bayesian inference (see, among others, [1]).

Let us consider the estimation problem for the expected value  $\theta$  of a normal distribution. Given *n* observations from i.i.d. normal random variables, the standard

Pierpaolo Brutti e-mail: pierpaolo.brutti@uniroma1.it · Fulvio De Santis e-mail: fulvio.desantis@uniroma1.it · Stefania Gubbiotti e-mail: stefania.gubbiotti@uniroma1.it Sapienza Università di Roma, Dipartimento di Scienze Statistiche

Bayesian estimate of  $\theta$  is a linear combination of the sampling mean,  $\bar{x}_n$ , and of a prior guess on  $\theta$ ,  $\mu_A$ , i.e.  $\omega_n \bar{x}_n + (1 - \omega_n)\mu_A$ , where  $\omega_n$  tends to one as *n* diverges. Therefore, for a sufficiently large sample size, the sample mean provides a good approximation of the Bayesian estimate.

In this paper, we are interested in analysing a measure of discrepancy between two competing estimators. This measure is random before observing the data. In Section 2, we introduce a specific measure of discrepancy,  $D_n$ , between a frequentist and a Bayesian estimator and in Section 2.1 we derive its explicit expression, its predictive cumulative distribution function (cdf) and its expected value for the normal model with conjugate priors. After briefly discussing the asymptotic behaviour of  $D_n$ , in Section 2.2 we focus on a fixed sample size, optimal with respect to a given criterion, and we assess the informativeness of the prior by evaluating  $D_n$ .

## 2 A discrepancy between estimators

Let  $\mathbf{X}_n = (X_1, X_2, ..., X_n)$  be a random sample from a probability distribution  $f_n(\cdot|\theta)$ , where  $\theta$  is an unknown real-valued parameter that belongs to the parameter space,  $\Theta \subseteq \mathbb{R}$ . Let  $\mathbf{x}_n = (x_1, x_2, ..., x_n)$  be an observed sample,  $\pi_A(\cdot)$  the prior density function of  $\theta$ ,  $f_n(\mathbf{x}_n|\theta)$  the likelihood function and  $\pi_A(\theta|\mathbf{x}_n)$  the posterior distribution. We will refer to  $\pi_A$  as to the *analysis-prior*. It models pre-experimental knowledge/uncertainty on  $\theta$  taken into account in posterior analysis.

We denote a Bayesian estimator of  $\theta$  as  $\hat{\theta}_B(\mathbf{X}_n)$ , whereas  $\hat{\theta}_F(\mathbf{X}_n)$  is a generic classical estimator. Let  $D_n(\mathbf{X}_n)$  be a measure of discrepancy between  $\hat{\theta}_B$  and  $\hat{\theta}_F$ . Specifically, we consider the standard squared difference between estimators, i.e.

$$D_n(\mathbf{X}_n) = [\hat{\theta}_B(\mathbf{X}_n) - \hat{\theta}_F(\mathbf{X}_n)]^2$$

Before observing the data,  $\hat{\theta}_B$ ,  $\hat{\theta}_F$  and  $D_n$  are random variables (functions of  $\mathbf{X}_n$ ). For instance, in the following we consider the posterior expectation of the parameter  $\theta$ ,  $\mathrm{E}(\theta|\mathbf{X}_n) = \int_{\Theta} \theta \pi(\theta|\mathbf{x}_n) \mathrm{d}\theta$ , as  $\hat{\theta}_B$ , and the maximum likelihood estimator (MLE) as  $\hat{\theta}_F$ , although the methodology could be extended to other estimators. We want to evaluate the probability of observing a small/large discrepancy between  $\hat{\theta}_B$  and  $\hat{\theta}_F$ . As for any other pre-posterior Bayesian analysis, to this purpose two alternative distributions for the data can be used. The *conditional* approach prescribes the use of the sampling distribution  $f_n(\cdot|\theta)$ , with  $\theta = \mu_D$ , a "design value" for the unknown parameter, whereas the *predictive* approach implies the use of the predictive distribution  $m_D(\mathbf{x}_n) = \int_{\Theta} f_n(\mathbf{x}_n|\theta)\pi_D(\theta)\mathrm{d}\theta$ , where  $\pi_D$  (design-prior) is a density function that accounts for uncertainty on the design value of  $\theta$ . Note that the conditional approach is a special case of the predictive one, when  $\pi_D$  is a point-mass prior on  $\mu_D$ ; for this reason in the following we adopt the most general approach. See [4] and [2] for a detailed discussion on this point. On a predictive measure of discrepancy between classical and Bayesian estimators

### 2.1 Results for the normal model

Let  $\mathbf{X}_n$  be a random sample from a  $N(\theta, \sigma^2)$  distribution. The MLE of  $\theta$  is  $\hat{\theta}_F = \bar{x}_n$ . Assume for  $\theta$  a normal prior density  $\pi_A(\theta) = N(\theta|\mu_A, \sigma^2/n_A)$ , where  $n_A$  is given the standard interpretation of *prior sample size*. From standard results on conjugate analysis [1], the posterior distribution of  $\theta$  is a normal density of mean  $(n+n_A)^{-1}(n\bar{x}_n+n_A\mu_A)$  and variance  $(n+n_A)^{-1}\sigma^2$ . Hence  $\hat{\theta}_B = \omega_n \bar{x}_n + (1-\omega_n)\mu_A$ , with  $\omega_n = n(n+n_A)^{-1}$ .

Letting  $\pi_D(\theta) = N(\theta | \mu_D, \sigma^2/n_D)$ , the predictive density function of  $\bar{x}_n$  is  $m_D(\bar{x}_n) = N(\bar{x}_n | \mu_D, \psi_n^2)$ , where  $\psi_n^2 = b_n \sigma^2$  and  $b_n = (n + n_D)(nn_D)^{-1}$ . Given the above assumptions, letting  $a_n = 1 - \omega_n$  the explicit expression of  $D_n$  is as follows

$$D_n = a_n^2 (\bar{X}_n - \mu_A)^2.$$

It is straightforward to check that the predictive expected value of  $D_n$  is

$$e_n = a_n^2 [b_n \sigma^2 + \delta^2],$$

where  $\delta = \mu_A - \mu_D$ , while the cdf of  $D_n$  is

$$p_n(d) = \Phi\left[b_n^{-1/2}(\delta + a_n^{-1}d^{1/2})\sigma^{-1}\right] - \Phi\left[b_n^{-1/2}(\delta - a_n^{-1}d^{1/2})\sigma^{-1}\right],$$

where  $\Phi(\cdot)$  is the standard Normal cdf.

Noting that  $b_n = O(1)$  and  $a_n = o(n^{-1})$ , it follows that  $e_n = o(n^{-2})$  and that, as *n* diverges,  $D_n$  converges in probability to zero as fast as  $n^{-2}$ . Both  $e_n$  and  $p_n$  depend on the prior means only through the absolute difference  $|\delta|$ .

## 2.2 Quantifying the informativeness of the prior

Let us consider the set up of an efficacy clinical trial, with positive values of  $\theta$  indicating an effective treatment. Let us suppose for instance to select the minimum sample size  $n^*$  such that the frequentist conditional power reaches a desired level (see among others [3]). For a normal model, under the assumptions of the previous section the power is  $\beta = \Phi\left(\frac{\theta\sqrt{n}}{\sigma} + z_{\alpha/2}\right)$ , where  $z_{\alpha}$  denotes the quantile of a standard normal at level  $\alpha$ . If we set for instance a design value for  $\theta$  equal to 0.5, when  $\sigma = 2$  and  $\alpha = 0.05$ , the optimal sample size required to reach a 0.80 power is  $n^* = 126$ . Let us assume a design prior of parameters  $\mu_D = 0.5$ ,  $n_D = 20$ . Based on  $n^*$ , we can compute  $e_{n^*}$  for a given analysis prior. The predictive expected discrepancy thus provides a measure of the conflict between the two alternative estimators and, at the same time, it represents the level of informativeness of the prior. In fact, the larger  $e_{n^*}$ , the stronger the impact of the prior in  $\hat{\theta}_B$ . In this way it is also possible to compare different choices for the analysis prior in terms of their informativeness level. In Table 1a we report the values of  $e_{n^*}$  for several choices of

the analysis prior parameters. For illustrative purposes we may consider a threshold value such as d = 0.2 (values exceeding 0.2 are bolded in the table): when a  $e_{n^*}$  is below this threshold the corresponding analysis prior can be considered relatively non informative, otherwise its impact on the Bayes estimator is remarkable. As expected, for increasing values of  $n_A$ , the analysis prior becomes more informative and, consequently, the expected discrepancy is larger. The increments of the conflict measure appear to be smaller when the analysis prior mean coincides with  $\theta_D$ . Similar considerations can be drawn by computing  $p_{n^*}(d)$ , but in this case a threshold on a probability scale can be set: for instance in Table 1b the values of  $p_{n^*}(d)$  below a given level, say 0.5, identify the analysis prior parameters with stronger impact on the Bayesian estimator.

	$n_A$					
$\mu_A$	1	10	20	50	100	200
(a)						
-2	0	0.035	0.122	0.523	1.269	2.440
-1	0	0.013	0.047	0.200	0.486	0.934
0	0	0.003	0.009	0.039	0.094	0.181
0.5	0	0.001	0.004	0.019	0.045	0.087
(b)						
-2	1	1	0.944	0.027	0.001	0.000
-1	1	1	1	0.561	0.155	0.055
0	1	1	1	0.987	0.855	0.677
0.5	1	1	1	0.999	0.964	0.870

**Table 1**  $e_{n^*}$  and  $p_{n^*}$  for several choices of the analysis prior, with  $n^* = 126$ .

•  $\mu_D = 0.5, n_D = 20$ 

In summary, in this work we have introduced a measure of conflict between classical and Bayesian point estimators. A similar methodology could be considered extending the idea of discrepancy both to different objects to be compared (such as interval estimators, Bayes factors, etc.) and to more complex models.

### References

- 1. Bernardo, J.M. and Smith, A.F.M. (1994). Bayesian Theory. Wiley.
- De Santis, F. (2006). Sample size determination for robust Bayesian analysis. Journal of the American Statistical Association, 101, n. 473, 278-291.
- 3. Spiegelhalter, D.J, Abrams, K.R. and Myles, J.P. (2004). Bayesian approaches to clinical trials and health-care evaluation. Wiley.
- Wang, F., and Gelfand, A.E. (2002). A simulation-based approach to Bayesian sample size determination for performance under a given model and for separating models. Statistical Science, 17, n. 2, 193-208.