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## Superconductivity in metastable phases of phosphorus-hydride compounds under high pressure

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Hydrogen-rich compounds have been extensively studied both theoretically and experimentally in the quest for novel high-temperature superconductors. Reports on sulfur hydride attaining metallicity under pressure and exhibiting superconductivity at temperatures as high as 200 K have spurred an intense search for room-temperature superconductors in hydride materials. Recently, compressed phosphine was reported to metallize at pressures above 45 GPa, reaching a superconducting transition temperature (T<sub>C</sub>) of 100 K at 200 GPa. However, neither the exact composition nor the crystal structure of the superconducting phase have been conclusively determined. In this work, the phase diagram of PH<sub>n</sub> (n = 1,2,3,4,5,6) was extensively explored by means of *ab initio* crystal structure predictions using the minima hopping method (MHM). The results do not support the existence of thermodynamically stable PH<sub>n</sub> compounds, which exhibit a tendency for elemental decomposition at high pressure even when vibrational contributions to the free energies are taken into account. Although the lowest energy phases of PH<sub>1,2,3</sub> display T<sub>C</sub>'s comparable to experiments, it remains uncertain if the measured values of T<sub>C</sub> can be fully attributed to a phase-pure compound of PH<sub>n</sub>.

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In December 2014, Drozdov *et al.* reported a superconducting critical temperature ( $T_C$ ) of 203 K in an ultradense phase of sulfur hydride (SH<sub>3</sub>) [1], identified by *ab initio* crystal structure searches [2], breaking the record- $T_C$  previously held by the cuprates. Subsequent experimental and theoretical studies have confirmed that superconductivity is of conventional nature and occurs in the predicted bcc phase [1,3], demonstrating the potential of *ab initio* crystal structure search methods to identify new superconductors. Several studies have meanwhile appeared in literature, discussing different aspects underlying the exceptional  $T_C$ , such as the role of bonding, Coulomb screening, phonon anharmonicty, etc. [4–11].

High-T<sub>C</sub> superconductivity based on a conventional electron-phonon (*ep*) coupling mechanism has been suggested by Ashcroft almost fifty years ago. He originally proposed that this could be achieved if hydrogen was sufficiently compressed, a prediction that has not yet been verified due to the required extreme pressures [12–17]. More recently, he suggested that the chemical precompression of hydrogen in hydrogen-rich compounds could be an effective route to reach metallization and high-T<sub>C</sub> superconductivity at experimentally accessible pressures [18], stimulating an intense activity of *ab initio* searches and predictions for high-T<sub>C</sub> superconducting hydrides [2,19–31]. Until 2014, however, all high-pressure phases which have been synthesized experimentally exhibited rather low T<sub>C</sub> [32–35].

Eventually, the discovery of  $SH_3$  showed that high- $T_C$  in hydrogen-rich solids can indeed be achieved. Thus, all stable hydrogen-containing molecules which can be placed into the compressing chamber of a diamond anvil cell are potential candidates for high- $T_C$  superconductors, as long as they remain stable against decomposition, amorphization, and the possible formation of metal hydrides during the measurement of  $T_C$  [32–35].

In fact, less than one year after the discovery of superconductivity in SH<sub>3</sub>, Drozdov et al. have very recently reported high-T<sub>C</sub> superconductivity in a second hydrogen-rich compound at extreme pressures: resistivity measurements on phosphine (PH<sub>3</sub>) show that the samples, which are semiconducting at ambient pressure, metallize above 40 GPa and become superconducting at around 80 GPa, exhibiting a maximum T<sub>C</sub> of 100 K at about 200 GPa [36]. Neither the exact composition of the superconducting phase and its crystal structure, nor the mechanism responsible for the high- $T_{\rm C}$ have been conclusively determined at this point. Analogies with superconducting SH<sub>3</sub>, which was obtained from SH<sub>2</sub> precursor, suggest that the superconductivity in the P-H system is of conventional nature, but that the composition of the superconducting phase might be different from the original PH<sub>3</sub> stoichiometry.

To shed light on this matter we used *ab initio* techniques to map out the high-pressure phase diagram of the P-H binary system by exploring the compositional and configurational space of  $PH_n$  with a sophisticated structure prediction method, and estimated the superconducting properties of the most promising phases. We found that all high-pressure binary phases of P and H are metastable with respect to elemental decomposition in the pressure range 100–300 GPa. However, the critical temperatures of the three phases closest to the convex hull (PH, PH<sub>2</sub>, and PH<sub>3</sub>) reproduce to a good approximation the experimental T<sub>C</sub> values. Possible ways to reconcile our results with experiments are discussed at the end of this manuscript.

To sample the enthalpy landscape, we employed the minima hopping method (MHM) [38,39], which has been successfully

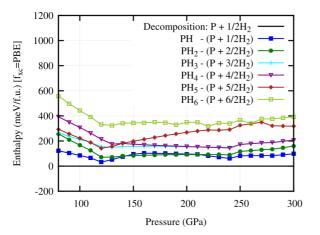
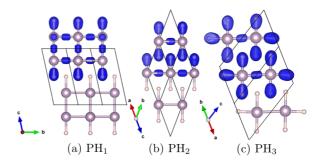


FIG. 1. Calculated enthalpies for PH<sub>n</sub> (n = 1,2,3,4,5,6) for the low-lying structures found in this work. Values are given with respect to the elemental decomposition (P + 1/2H<sub>2</sub>). The reference structures for hydrogen are  $P6_3m$  (0–120 GPa) and C2/c (120–300 GPa) from Ref. [37]. The reference phases for phosphorus are  $Pm\bar{3}m$  (0–10 GPa), R3m (20–110 GPa), P6mm (120–240 GPa),  $Im\bar{3}m$  (250–270 GPa), and  $I\bar{4}3d$  (280–300 GPa). The change in slope at around 120 GPa is due to the phase transition in elemental hydrogen.

used for global geometry optimization<sup>1</sup> in a large variety of applications [40–42], including superconducting materials at high pressure [6,31]. The enthalpies as a function of pressure for the ground-state structures<sup>2</sup> at each composition are shown in Fig. 1 with respect to elemental decomposition. The ground-state structures were determined by the MHM at 100, 150, 200, and 300 GPa, and further relaxed at intermediate pressures to obtain a smooth phase diagram. An additional search was carried out at zero pressure. The various phases of



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FIG. 2. Low-lying enthalpy structures found for different compositions under pressure at 120 GPa. The large and small spheres denote the P and H atoms, respectively. The ELF at a fixed value of 0.8 is shown in the upper part of each structure.

pure H and P for the convex hull construction were obtained from a structural search, and for hydrogen they coincide with the ones reported by Needs et al. [37]: P6<sub>3</sub>m (0-120 GPa) and C2/c (120–300 GPa). The complex phase diagram of elemental phosphorus [43,45], with at least six structural transition between 0 and 300 GPa, is closely reproduced by our calculations, see Ref. [44]. At zero pressure, molecular phosphine (PH<sub>3</sub>), as well as the crystalline phases of PH, PH<sub>2</sub>, and PH<sub>3</sub> identified by our MHM runs, are all stable with respect to elemental decomposition (see Ref. [44]). Moreover, we found two compositions (PH and PH3) forming the convex hull with enthalpies of formation between -50and -60 meV/atom. In the crystalline phases, the molecules retain their geometry and are held together by van der Waals interactions; these molecular crystals are semiconducting with gaps of 0.9 (PH), 2.1 (PH<sub>2</sub>), and 3.7 eV (PH<sub>3</sub>), respectively. Given the complexity of the phase diagram of elemental phosphorus, it is likely that the binary phases considered here will undergo several phase transitions between ambient pressure and 100 GPa, but analyzing these transitions is well beyond the scope of this work. Assuming that the PH<sub>3</sub> zero-pressure structure is representative at higher pressures, we estimate a metallization pressure of  $\sim$ 35 GPa, which is in accordance with experiments, see Ref. [44] for details.

In the following, we will focus on high pressures (80–200 GPa), which are relevant for superconductivity. The formation enthalpies of all the identified structures are positive and in a range of 30-200 meV/f.u. for hydrides with low hydrogen contents (PH, PH<sub>2</sub>, and PH<sub>3</sub>), and larger for higher H content up to PH<sub>6</sub>.

The ground-state structures at 120 GPa of pressure for PH (14/mmn), PH<sub>2</sub> (14/mmn), and PH<sub>3</sub> (C2/m) are shown in Fig. 2. The bond lengths are ~1.4 Å for the P-H bonds and ~2.1 Å for the P-P bonds in all three structures. Figure 2 clearly shows the dominating tendency of P atoms to form polymers with hydrogen saturating the dangling bonds, resulting in 1D chains or 2D layers. This picture is confirmed when looking at the isosurfaces of the electron localization function (ELF), clearly showing that electrons are localized to form P-P and P-H bonds. No or only weak interactions are observed between the polymeric chains, which is in strong contrast to other hydrogen-rich materials that are stable against decomposition and exhibit a 3D network of strongly interacting host atoms and hydrogen [31,46]. With increasing hydrogen content, the dimensionality of the polymers decreases from layers and

<sup>&</sup>lt;sup>1</sup>The MHM was designed to thoroughly scan the low-lying enthalpy landscape of any compound and identify stable phases by performing consecutive short molecular dynamics escape steps followed by local geometry relaxations. The enthalpy surface is mapped out efficiently by aligning the initial molecular dynamics velocities approximately along soft mode directions [66,67], thus exploiting the Bell-Evans-Polanyi [68] principle to steer the search towards low energy structures.

<sup>&</sup>lt;sup>2</sup>We explored phases with 1, 2, 3, and 4 formula units of  $PH_n$  for stoichiometries n = 1, 2, 3, 4, 5, 6 at selected pressures in the range 100-300 GPa. The relaxations to local minima were performed by the fast inertia relaxation engine [69] by taking into account both atomic and cell degrees of freedom. Energy, atomic forces, and stresses were evaluated at the density functional theory (DFT) level with the Perdew-Burke-Erzernhof (PBE) [70] parametrization to the exchange-correlation functional. A plane-wave basis set with a high cutoff energy of 1000 eV was used to expand the wave function together with the projector augmented wave (PAW) method as implemented in the Vienna ab initio simulation package VASP [71]. Very dense k meshes were set for the different compositions, at 120 GPa the grids were PH:  $20 \times 20 \times 20$ , PH<sub>2</sub>:  $20 \times 20 \times 16$ , PH<sub>3</sub>: 12×12×12, PH<sub>4</sub>: 14×12×10, PH<sub>5</sub>: 12×12×8, PH<sub>6</sub>: 10×14×20, and for the polymeric phases of PH<sub>2</sub> (6 f.u.):  $8 \times 4 \times 12$ . Geometry relaxations were performed with tight convergence criteria such that the forces on the atoms were less than 2 meV/Å and the stresses were less than 0.1 meV/Å<sup>3</sup>.

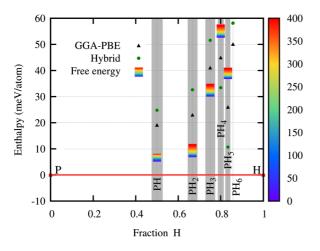


FIG. 3. Predicted formation enthalpies of  $PH_n$  with respect to decomposition into P and H at 120 GPa. The solid red line denotes the convex hull of stability. Black triangles show PBE and green squares hybrid functional values (HSE06). The color-gradient scale indicate the free-energy within the harmonic approximation at temperatures up to 400 K (color bar in Kelvin on the right) as computed on top of PBE energies.

sheets (PH, PH<sub>2</sub>) to chains (PH<sub>3</sub>, PH<sub>4</sub>), until oversaturation is reached and  $H_2$  molecules precipitate, intercalating the P-H polymers in PH<sub>5</sub> and PH<sub>6</sub>.

Figure 1 shows that, although none of the binary phases are thermodynamically stable, some lie very close to the convex hull at around 120 GPa. Therefore an in-depth investigation was conducted to assess whether effects going beyond those included in our MHM searches could stabilize any of these phases in the range between 100 and 150 GPa.

A detailed analysis of the phase stability at 120 GPa is shown in Fig. 3. We first investigated how the use of different exchange-correlation functionals influences the stability of the various compounds. PBE values are shown as black triangles in Fig. 3. In the local density approximation (not shown) we obtain fairly similar phase stabilities. We also report results obtained by means of the more demanding Heyd-Scuseria-Ernzerhof (HSE) hybrid functional [47–50]. Although hybrids are considered to give better results than semilocal functionals for structural and electronic properties in semiconductors [48] and intermetallic alloys [51], they have not been systematically validated for metallic systems, where severe anomalies in the lattice stability and electronic properties have been recently reported [52]. The HSE results, plotted as green squares in Fig. 3, show nevertheless a similar trend as obtained with PBE and LDA. HSE predicts slightly higher formation enthalpies than PBE for PH, PH<sub>2</sub>, PH<sub>3</sub>, and PH<sub>6</sub>, and lower values for PH<sub>4</sub> and PH<sub>5</sub>. Finally, the semiempirical DFT-D2 method of Grimme [53], which takes into account van der Waals interactions, consistently predicted a lower stability of the binary phases compared to PBE. The positive formation enthalpies predicted by all four exchange-correlation functionals strongly suggest that none of the binary  $PH_n$  phases are in fact thermodynamically stable.

Next, we investigated the influence of vibrational entropy and zero-point energy (ZPE) on the phase stability. Phonon calculations were carried out with the frozen phonon approach as implemented in the PHONOPY package [54] with sufficiently

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large supercells. The ZPE and free energy within the harmonic approximation at temperatures between 0 and 400 K shown as colored gradients in Fig. 3. There is a clear distinction in the vibrational effect on the stability for  $PH_n$  phases with high and low hydrogen content: PH, PH<sub>2</sub>, and PH<sub>3</sub> increase in stability, whereas  $PH_4$  and  $PH_5$  decrease. This behavior can be attributed to the existence of  $H_2$  molecules in the crystal lattice of the hydrogen-rich phases, which induce high-energy vibrational modes responsible for an increased ZPE.

For PH, the formation energy is less than 5 meV/atom at 0 K, whereas for PH<sub>2</sub> and PH<sub>3</sub>, it is about 7 and 30 meV/atom, respectively. Comparing the free energies at finite temperatures reveals that all phases are destabilized by vibrational entropy by a few meV, pushing them away from the convex hull with increasing temperature. Since anharmonic effects become increasingly important at higher temperatures, we recomputed the free energy for PH, PH<sub>2</sub>, and PH<sub>3</sub> within the quasiharmonic approximation, taking into account the thermal lattice expansion. These calculations, however, showed only minor effects on the stabilities and the distance from the convex hull of all three binary phases slightly increased by a few meV per atom.

Having ruled out that any of the standard corrections to the electronic enthalpy can stabilize our phases in the experimentally relevant regime, we are left with the question of which phase and chemical composition was experimentally observed by Drozdov *et al.* We can rule out that the superconductivity observed is due to some residual elemental phase, as hydrogen is not metallic at these pressures and elemental phosphorus displays much lower critical temperatures [55], not higher than a few Kelvin.

On the other hand, our phonon calculations show that the ground states at fixed compositions of PH<sub>1</sub>, PH<sub>2</sub>, and PH<sub>3</sub> are all dynamically stable, i.e., with no imaginary modes in the whole Brillouin zone. Therefore one of these metastable phases might have been synthesized through a nonequilibrium process or possibly through anisotropic stress in the anvil cell, as the order of magnitude of the relevant energy barriers in these cases could be in the range of few tens of meV. In fact, the compositions closest to the hull are PH and PH<sub>2</sub>, indicating a possible decomposition of the original phosphine molecules (PH<sub>3</sub>) under pressure into PH and PH<sub>2</sub>, similarly to what is observed in sulfur hydrides where the initial, molecular SH<sub>2</sub> decomposes under pressure to form SH<sub>3</sub>.

To assess whether any of these three metastable phases could be a reasonable candidate for superconductivity, we calculated the Eliashberg spectral functions for the electron-phonon (ep) interaction:

$$\alpha^2 F(\omega) = \frac{1}{N_{E_F}} \sum_{\mathbf{kq},\nu} |g_{\mathbf{k},\mathbf{k}+\mathbf{q},\nu}|^2 \delta(\epsilon_{\mathbf{k}}) \delta(\epsilon_{\mathbf{k}+\mathbf{q}}) \delta(\omega - \omega_{\mathbf{q},\nu}), \quad (1)$$

where  $N_{E_F}$  is the DOS at the Fermi level,  $\omega_{\mathbf{q},\nu}$  is the phonon frequency of mode  $\nu$  at wave vector  $\mathbf{q}$  and  $|g_{\mathbf{k},\mathbf{k}+\mathbf{q},\nu}|$  is the electron-phonon matrix element between two electronic states with momenta  $\mathbf{k}$  and  $\mathbf{k} + \mathbf{q}$  at the Fermi level.

From the Eliashberg function, we also obtained the electron-phonon coupling constant  $\lambda$  and the logarithmic average phonon frequency  $\omega_{ln}$  [56,57] (which, in the McMillan-Allen-Dynes parametrization for T<sub>C</sub>, sets the energy scale for

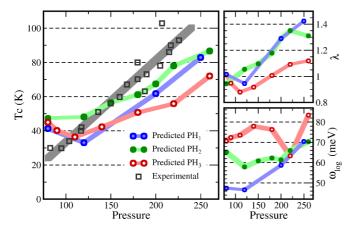


FIG. 4. (Left) SCDFT calculated critical temperatures  $T_C$  for PH (blue), PH<sub>2</sub> (green), and PH<sub>3</sub> (red) as a function of pressure. Experimental  $T_C$  by resistivity measurements from Drozdov *et al.* [36] are shown in black squares. Overall a good agreement is found between the experimental values and those for PH, PH<sub>2</sub>, and PH<sub>3</sub>. Although the PH<sub>2</sub> composition shows significantly better agreement. (Right) Trend in pressure of the (BCS-like) electron phonon coupling coefficient  $\lambda$  (top panel) and of the phononic characteristic frequency  $\omega_{ln}$  (bottom panel) as a function of pressure.

the phononic pairing). In order to avoid using the empirical  $\mu^*$  parameter and bias the theoretical predictions towards the experiments, we computed the critical temperatures within density functional theory for superconductors (SCDFT), which uses as input the Eliashberg function in an isotropic approximation, while the residual Coulomb forces in the Cooper pairing are included within the static random phase approximation [58–61], as used in Refs. [6,62].

The values of  $T_C$  are shown in Fig. 4 and are compared to the experimental values reported by Drozdov *et al.* [36]. In the two right panels of the same figure, we show  $\lambda$  and  $\omega_{ln}$  for the three phases as a function of pressure.<sup>3</sup>

Our calculated behavior of  $T_C$  with respect to pressure shows a fair agreement with experiments for all three structures (PH, PH<sub>2</sub>, and PH<sub>3</sub>); the best agreement is found for PH<sub>2</sub>, which has a  $T_C$  of 40 K at 100 GPa that increases under pressure and reaches a maximum value of 78 K at 220 GPa. The PH system shows the best agreement in the rate at which  $T_C$  grows with pressure in the 120–260 GPa window  $(dT_c/dP \simeq 0.4$  K/GPa), while showing a high pressure shift of about 20 GPa with respect to the experimental data.

The similar superconducting behavior of the three compounds results from the compensation of different behaviors

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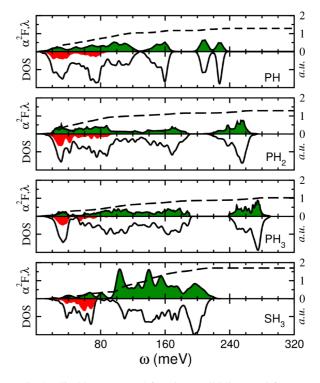


FIG. 5. Eliashberg spectral function (solid line) and frequencydependent *ep* coupling parameters  $\lambda(\omega)$  (dashed line)—top panels and phonon density of states (DOS)—bottom panels—for the three PH<sub>n</sub> compounds considered in the present study and SH<sub>3</sub> at 200 GPa. The shaded area (red) in the DOS panels is the P/S partial phonon DOS.

of  $\lambda$  and  $\omega_{\text{ln}}$ , shown in the right panels of the same figure. These reflect different features of the three Eliashberg functions, shown in Fig. 5, together with that of SH<sub>3</sub> for reference. The PH<sub>1,2,3</sub> spectra have an overall similar shape, i.e., they are roughly proportional to the phonon density of states, dominated by P modes at low frequencies (<80 meV), and hydrogen modes at high frequencies.

A gap separates the hydrogen bond-bending vibrations from the rest of the spectrum; this part moves to higher energies with increasing hydrogen content, but has very little influence on  $T_C$  due to the high frequencies involved. The spectrum of SH<sub>3</sub> is more compact, extending up to 200 meV, with higher peaks in  $\alpha^2 F(\omega)$ , thus resulting in a large value of  $\lambda(\simeq 1.9)$ .

As more and more theoretical predictions of new superconducting hydrides are available, there is an increasing effort towards a systematic understanding of the factors leading to high  $T_C$  [26,46]. It is becoming clear that the original idea of Ashcroft [18], that the heavier atoms merely exert chemical pressure on the hydrogen lattice, is oversimplified, and other factors, such as the formation of strong atomic bonds between H and the heavier elements, play a crucial role. A good indicator for the tendency of a material to follow one or another behavior is the electronegativity of the heavy atom. Atoms which are less electronegative than H tend to form solids which contain H<sub>2</sub> units with large characteristic vibration frequencies, but relatively weak matrix elements (electron-phonon coupling). More electronegative atoms, on the other hand, tend to form polar-covalent bonds, which couple strongly to phonons [9,46].

<sup>&</sup>lt;sup>3</sup>Electronic bands, vibrational frequencies, and electron-phonon matrix elements were computed within density functional perturbation theory [72–74], as implemented in the QUANTUM ESPRESSO and ABINIT code. We employed norm-conserving pseudopotentials for H and P, with a plane-wave cutoff of 80 Ry; phonon frequencies and electron-phonon were computed on coarse ( $8^3$ ,  $6^3$ , and  $4^3$  k points for PH, PH<sub>2</sub>, and PH<sub>3</sub>, respectively), and interpolated on denser grids using force constants; for the electronic integration, we employed Monkhorst-Pack grids of  $8^3$  k points for the self-consistent calculations; much denser (up to  $30^3$  points) grids were used for Fermi-surface integrations.

Phosphorus, with an electronegativity equal to that of hydrogen, lies on the border between the two regions and for the three hydrides considered in this study the electronic structure indicates a strong P-H hybridization in the whole energy range (see Ref. [44]). The values of the electronic density of state (DOS) at the Fermi level— $N_{E_F}$ —are comparable (0.31–0.38 st/eVf.u.), and sensibly lower than those in SH<sub>3</sub> (0.54). The ratio  $\eta = \lambda/N_{E_F}$ , which can give an indication of the "stiffness" of the underlying lattice, ranges from 3 in PH<sub>3</sub> to 3.8 in PH, and is 3.6 in SH<sub>3</sub>.

In practice,  $PH_{1,2,3}$  and  $SH_3$  have a quite similar bonding and lattice stiffness to each other: what makes the latter exhibit a yet unmatched record  $T_C$  is the extremely high value of its  $N_{E_F}$ , due to the presence of the van Hove singularity close to the Fermi level [10,11]. As the Fermi level of  $PH_2$  and  $PH_3$  falls in a shallow minimum of the density of states (see Ref. [44]), the same effect could be used to increase their  $T_C$ , by doping a small fraction of S or Si impurities into the samples.

In conclusion, the phase stability and superconducting properties of the recently reported PH<sub>3</sub> compound under pressure have been investigated with *ab initio* calculations. Our extensive structural searches show that the hydrogen-rich phosphorus phases are thermodynamically unstable in the high-pressure regime of the phase diagram. Although including vibrational zero-point effects in our calculations improves the stability of PH, PH<sub>2</sub>, and PH<sub>3</sub>, they remain metastable. Nevertheless, in view of their small distance from the convex hull, any of these structures may have been synthesized through nonequilibrium or by anharmonic effects, as discussed in Refs. [5,63]. Several of them were predicted to be good phonon-mediated superconductors and could thus in principle account for the measured high-T<sub>C</sub> in experiments. In our opinion, the phase/composition that yields the best agreement with experiments are PH and PH<sub>2</sub>, which are both close to the convex hull (<7 meV/atom) and would show a pressure

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dependence in  $T_C$  similar to the experimental measurements. It is still unclear if the experimentally observed high- $T_C$  can be fully attributed to a phase of a binary phosphorus hydride, and further experiments are called for to validate both our predictions and the results reported by Drozdov *et al.* [36]. Finally, our calculations give a strong indication that the observed critical temperatures are those to be expected for the low energy, low-H content phases of the P-H system.

Note added. While writing the present manuscript, we became aware of two works, which report structural searches of phosphorus hydrides, employing evolutionary algorithms [64,65]. Both studies agree with our conclusions that none of the predicted phases are thermodynamically stable in the pressure range of 100–200 GPa. Shamp *et al.* [64] also suggest an I4/mmm PH<sub>2</sub> structure as a possible candidate for the high-T<sub>C</sub> phase. They also report a *polymeric* PH<sub>2</sub> structure, which is more stable at low pressures. Based on our calculations, however, the *polymeric* structures for PH<sub>2</sub> show higher enthalpies than the I4/mmm structure.

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