Level Set Method in Medical Imaging Segmentation



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Authored by

Ayman El-Baz and Jasjit S. Suri



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CRC Press Taylor & Francis Group 6000 Broken Sound Parkway NW, Suite 300 Boca Raton, FL 33487-2742

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Printed on acid-free paper

International Standard Book Number-13: 978-1-138-55345-3 (Hardback)

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Library of Congress Cataloging-in-Publication Data

Names: El-Baz, Ayman S., editor. | Suri, Jasjit S. editor. Title: Level set method in medical imaging segmentation / [edited by] Ayman El-Baz and Jasjit S. Suri. Description: Boca Raton : Taylor & Francis, 2019. | Includes bibliographical references. Identifiers: LCCN 2019005809 | ISBN 9781138553453 (hardback : alk. paper) | ISBN 9781315148595 (ebook) Subjects: | MESH: Image Interpretation, Computer-Assisted—methods | Image Processing, Computer-Assisted—methods | Mathematical Computing Classification: LCC RC78.7.D53 | NLM WN 182 | DDC 616.07/54—dc23 LC record available at https://lccn.loc.gov/2019005809

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With love and affection to my mother and father, whose loving spirit sustains me still

Ayman El-Baz

To my late loving parents, my wife, and loving children Jasjit S. Suri



Contents

Pref	faceix
Biog	graphies xi
Ack	xnowledgementsxiii
Cor	ntributorsxv
1.	Tomography Reconstructions With Stochastic Level-Set Methods 1 Bruno Sixou, Lin Wang, and Françoise Peyrin
2.	Application of 3D Level Set Based Optimization in MicrowaveBreast Imaging for Cancer Detection23Hardik N. Patel and Deepak K. Ghodgaonkar
3.	A Modified Global and Elastic ICP Shape Registration for Medical Imaging Applications
4.	Robust Nuclei Segmentation Using Statistical Level Set Method with Topology Preserving Constraint
5.	Level Set Methods in Segmentation of SDOCT Retinal Images 99 Padmasini N, Umamaheswari R, Mohamed Yacin Sikkandar, and Manavi D Sindal
6.	Numerical Techniques for Level Set Models: an Image Segmentation Perspective
7.	Level Set Methods for Cardiac Segmentation in MSCT Images 157 <i>Ruben Medina, Sebastian Bautista, Villie Morocho,</i> <i>and Alexandra La Cruz</i>
8.	Deformable Models and Image Segmentation
9.	Cardiac Image Segmentation Using Generalized Polynomial Chaos Expansion and Level Set Function

10.	Medical Image Segmentation Approach That Uses Level Sets with Statistical Shape Priors Ahmed ElTanboly, Mohammed Ghazal, Hassan Hajjdiab, Ali Mahmoud, Ahmed Shalaby, Jasjit S. Suri, Robert Keynton, and Ayman El-Baz	289
11.	Level Set Method in Medical Imaging Segmentation	315
12.	Image Segmentation With B-Spline Level Set	341
Ind	ex	383

Preface

In the medical imaging field, accurate segmentation of structures is crucial in many applications; for example, in detecting lesions and abnormalities. However, segmentation is highly challenging due to such factors as the low contrast between different tissues types that makes it difficult to even segment the desired object manually, and the motion artifacts associated with the scans which adds noise to images. This book covers the state-of-the-art approaches for medical imaging segmentation based on the level set technique that was implemented by Osher and Sethian. The level set technique mainly relies on the theory of curve and surface evolution, in addition to the link between front propagation and hyperbolic conservation laws. This makes it easy to follow shapes that change topology.

Among numerical techniques, level sets are significantly powerful at interpreting interface motion. Level set methods have provided great advances to clinicians in assessing abnormalities through computer-aided diagnostic (CAD) systems that can analyze images from these different modalities; for example computed tomography (CT), magnetic resonance imaging (MRI), and optical coherence tomography (OCT). Different modalities will be discussed in this book for different applications.

In summary, the main aim of this book is to survey an illustrative subset of past and current applications of level set technique in medical imaging segmentation. It focuses on major trends and challenges in this area, identifies new techniques and presents their use in biomedical image analysis.

> Ayman El-Baz Jasjit S. Suri



Biographies



Ayman El-Baz is a professor, university scholar, and Chair of the Bioengineering Department at the University of Louisville, Kentucky. Dr. El-Baz earned his B.Sc. and M.Sc. degrees in electrical engineering in 1997 and 2001, respectively. He earned his Ph.D. in electrical engineering from the University of Louisville in 2006. In 2009, Dr. El-Baz was named a Coulter Fellow for his contributions to the field of biomedical translational research. Dr. El-Baz has 17 years of hands-on experience in the fields

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Jasjit S. Suri is an innovator, scientist, visionary, industrialist and an internationally known world leader in biomedical engineering. Dr. Suri has spent over 25 years in the field of biomedical engineering/devices and its management. He received his Ph.D. from the University of Washington, Seattle and his Business Management Sciences degree from Weatherhead, Case Western Reserve University, Cleveland, Ohio. Dr. Suri was awarded the President's Gold medal in 1980 and made Fellow of the

American Institute of Medical and Biological Engineering for his outstanding contributions. In 2018, he was awarded the Marquis Life Time Achievement Award for his outstanding contributions and dedication to medical imaging and its management.



The completion of this book could not have been possible without the participation and assistance of many people; all of whose names may not be enumerated. Their contributions are sincerely appreciated and gratefully acknowledged. However, the editors would like to express their deep appreciation and indebtedness particularly to Dr. Ali H. Mahmoud and Ahmed ElTanboly for their endless support.

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Tomography Reconstructions With Stochastic Level-Set Methods

Bruno Sixou, Lin Wang, and Françoise Peyrin

CONTENTS

1.1	Intro	duction		2		
1.2	Preliminaries					
	1.2.1	Level-S	Set Regularization of Inverse Problems	3		
	1.2.2	Some N	Notions of Stochastic Calculus	4		
1.3	Binary Tomography Reconstructions of Bone Microstructure from					
	Few	Projectio	ons with Stochastic Level-Set Methods	5		
	1.3.1	The Bir	nary Tomography Problem	5		
	1.3.2 Global Optimization with Stochastic Level-Set Evolution					
	and Simulated Annealing					
		1.3.2.1	Stochastic Level-Set Evolution	6		
		1.3.2.2	Classical Simulated Annealing	7		
	1.3.3	Compa	rison of the Algorithms: Results and Discussion	8		
		1.3.3.1	Simulation Details	8		
		1.3.3.2	Numerical Results	9		
1.4	Stoch	nastic Le	vel-Set Reconstruction in Nonlinear Phase Contrast			
	Tomo	ography		11		
	1.4.1 Nonlinear Phase Contrast Tomography					
	142 Level-Set Regularization in In-Line Phase Contrast					
		Tomog	raphy	12		
	1.4.3 Stochastic Level-Set Methods for Phase Contrast Tomography					
	1.4.4	Numer	ical Results and Discussion	15		
		1.4.4.1	Simulation Details	15		
		1.4.4.2	Numerical Results for Deterministic Level-Set			
			Method	16		
		1443	Deterministic Level-Set versus Stochastic Level-Set	10		
		1.1.1.0	Algorithm	17		
				1/		

1.4.5	Conclusion	 	 	20
References		 	 	20

1.1 Introduction

The level-set methods are now a well-known tool for the computation of evolving boundaries since their introduction by Osher and Sethian [1]. They have been designed newly to reconstruct solutions of inverse problems with non-smooth and piecewise constant solutions [2–4]. The numerical results indicate their sucess. Yet, inverse problems with piecewise constant solution are non-convex and the reconstructed solution is a local minimum of the regularization functional. It may be interesting to escape this local minimum with global optimization methods. Stochastic algorithms based on stochastic differential equations have been proposed for the global optimization of non-convex functions [5–9]. Let (Ω, \mathcal{F}, P) be a probability space, in order to obtain the global minimum of a function $g : \mathbb{R}^m \to \mathbb{R}^m$, a random trajectory X(t) governed by the following diffusion process is often used [5–9]:

$$dX(t) = -\nabla g(X(t))dt + \mu(t)dW(t)$$
(1.1)

where $W = (W_1(t), ..., W_m(t))$ is the standard *m*-dimensional Brownian motion and $\mu(t)$ the noise strength. For an appropriate annealing schedule $\mu(t)$ and under appropriate condition on *g*, the probability law of X(t) converges weakly to a probability law which has its support on the set of the global minimizers of *g* [5–9]. In the field of image processing, stochastic partial differential equations applied to level-set functions have been used for segmentation tasks [10]. The right way to study stochastic evolutions in the level-set framework is through the Stratonovich integral so that evolution of the boundary curve is independent of the level-set function used for its representation [10]. The aim of this chapter is to show that this type of approach can be generalized to inverse problems with piecewise constant solutions.

In the first section, we summarize some results about stochastic calculus and the level-set regularization of inverse problems. Then, the stochastic level-set approach is applied to the binary tomography and to the phase contrast tomography inverse problem.

1.2 Preliminaries

In this first section, we present the level-set regularization approach of inverse problems and some aspects of stochastic calculus.

1.2.1 Level-Set Regularization of Inverse Problems

In this section, we detail the level-set regularization approach of inverse problems. Let $R : H_1 \rightarrow H_2$, a linear operator mapping two Hilbert spaces H_1 and H_2 , and $g \in H_2$. Our aim is to find a piecewise constant solution f of the inverse problem:

$$Rf = g \tag{1.2}$$

For Ω a bounded Lipschitz open subset in \mathbb{R}^2 , we assume that the function to be reconstructed *f* is the characteristic function of a regular set $\Omega_1 \subset \Omega$, $f = \chi_{\Omega_1}$. It can be represented with the Heaviside distribution and with a levelset function $\theta \in H_1(\Omega)$ as $f = H(\theta)$, where $H_1(\Omega)$ is the first-order Sobolev space and with $H(\theta) = 1$ if $\theta > 0$ and 0 otherwise.

Assuming that the noisy data are such that $||g^{\delta} - g|| \le \delta$, where δ is the noise level, the reconstruction problem becomes nonlinear and consists in determining the level-set function θ minimizing the regularization functional:

$$E(\theta) = \frac{\|RH(\theta) - g^{\delta}\|_{2}^{2}}{2} + F(\theta)$$
(1.3)

where *F* is a regularization term for the level-set function. We have considered here a Total Variation- H_1 regularization functional [2,3]:

$$F(\theta) = \beta_1 |H(\theta)|_{TV} + \beta_2 ||\theta||_{H_1}^2$$
(1.4)

where $|.|_{TV}$ is the Total Variation semi-norm. The regularization parameters β_1, β_2 determine the relative weights of the stabilizing terms.

Since *H* is discontinuous, it is necessary to consider generalized minimizers of the regularization functional [2, 3]. These minimizers can be approximated by minimizers of smoothed regularization functional with an approximation H_{ϵ} . The following smooth approximations of the Heaviside function *H* has been used $H_{\epsilon}(x) = \frac{1+2\epsilon}{2}(erf(x/\epsilon) + 1) - \epsilon$ where ϵ is a real positive constant. The smoothed regularization functional is given by:

$$E_{\epsilon}(\theta) = \frac{\left\| RH_{\epsilon}(\theta) - g^{\delta} \right\|_{2}^{2}}{2} + \beta_{1} |H_{\epsilon}(\theta)|_{TV} + \beta_{2} \|\theta\|_{H_{1}}^{2}$$
(1.5)

The minimizers of the Tikhonov functionals are found with a first-order optimality condition for the smoothed functionals, $E'_{\epsilon}(\theta) = 0$, with:

$$E_{\epsilon}'(\theta) = H_{\epsilon}' R^* \left(R H_{\epsilon}(\theta) - g^{\delta} \right) + \beta_2 (I - \Delta)(\theta) + \beta_1 \frac{\partial |H_{\epsilon}(\theta)|_{TV}}{\partial \theta}$$
(1.6)

where R^* denotes the adjoint of the forward operator. From the current estimate θ_k , the update $\theta_{k+1} = \theta_k + \delta\theta$ is obtained with a classical Gauss-Newton method with a linearization of the condition $G(\theta_k + \delta\theta) = 0$ [22].

This method can be generalized to nonlinear operators and *R* must be replaced by the Fréchet derivative of the direct operator. For high noise levels, the solution θ may be trapped in a local minima. In that case, the data term

 $||RH_{\epsilon}(\theta) - g^{\delta}||$ at the end of the optimization is largely higher than the noise level δ and the many reconstruction errors are still present. In order to escape from these stationary points, we propose stochastic global optimization methods.

1.2.2 Some Notions of Stochastic Calculus

The stochastic evolution of the level-set function is based on the Stratonovich integral. In this first section, we summarize some useful notions of stochastic calculus [11, 12]. We explain the difference between the Itô and Stratonovich stochastic integrals. Let $(\Omega, \mathcal{F}, \mathcal{F}_t, P)$ represent a probability space and $W_{t\geq 0}$ a one-dimensional Brownian motion. The paths of the Brownian motion are only $\frac{1}{2}$ -Hölder continous and nowhere differentiable, and in order to define dW(t), it is usual to start with the stochastic integral. Given a square integrable process $(\phi(s, \omega))_{s\geq 0}$ and a subdivision $\Delta = \{0 = t_1 < \ldots < t_n = t\}$, the stochastic Itô integral $\int_0^t \phi(s, \omega) dW(s)$ with respect to the Brownian motion is defined as the limit of the Riemann sum:

$$\sum_{1 \le i \le n} \phi(t_i, \omega) (W(t_{i+1}) - W(t_i))$$
(1.7)

when $|\Delta| = min|t_{i+1} - t_i| \rightarrow 0$. The limit obtained $\{I(\phi)\}_{t\geq 0}$ is a square integrable martingale. This definition can be extended to an arbitrary dimension.

Considering a process $X = (X_t)_{t \ge 0}$ and a smooth function α of class C^2 , the process $Y_t = (\alpha(X_t))$ satisfies the Itô formula:

$$dY(t) = \alpha'(X(t))dt + \frac{1}{2}\alpha''d < X, X > (t)$$
(1.8)

The drift term involves the quadratic variation $\langle X, X \rangle$ of the process X which depends on the stochastic part of the dynamics. For a stochastic process, $X(t) = \int_0^t f(s) dW(s) + A(t)$, where f is a continuous square integrable function and A(t) is continuous and increasing, the quadratic variation can be calculated as:

$$\langle X, X \rangle (t) = \int_{0}^{t} f(s)^{2} ds$$
 (1.9)

It is possible to give another definition of the stochastic integral so that the classical chain rule is satisfied. Considering two processes X(t) = M(t) + B(t), Y(t) = N(t) + C(t) where M, N are local continuous martingales and B, C are increasing processes, the Stratonovich integral of Y with respect to X is given by the formula

$$\int_{0}^{t} Y(s) dX(s) = \int_{0}^{t} Y(s) dX(s) + \frac{1}{2} < M, N > (t)$$
(1.10)

Then, it can be shown that the classical chain rule formula is satisfied [11,12]:

$$\alpha(X_t) = \alpha(X_0) + \int_0^t \alpha'(X(s)) o dX(s)$$
(1.11)

The principle of the stochastic level-set evolution framework is to transfer the contour evolution to the level-set function. The dynamics of the level-set contour should not be modified by a change of the level-set function. This invariance property is not guaranted by the Itô rule. If the Itô integral is replaced by the Stratonovich for the stochastic evolution, the additional drift term disappears and the invariance property is verified.

The Stratonovich evolution equation can be implemented with an implicit scheme. The Stratonovich integral with respect to the Brownian motion *W* can be approximated as:

$$\int_{0}^{T} Y(s) odW(s) = \lim_{|\Delta| \to 0} \sum_{1 \le i \le n} Y\left(\frac{t_i + t_{i+1}}{2}\right) (W(t_{i+1}) - W(t_i))$$
(1.12)

with $W(t_{i+1}) - W(t_i) \sim \sqrt{(t_{i+1} + t_i)} \mathcal{N}(0, 1)$, where $\mathcal{N}(0, 1)$ is a Gaussian of standard deviation 1.

In [10], it was proposed to simulate the Stratonovich evolution with the Itô formalism and an additional drift term. Using the formula Eq. 1.10, it can be shown that, for a level-function θ :

$$\begin{aligned} |\nabla\theta(x,t)|odW(t) &= |\nabla\theta(x,t)|dW(t) \\ &+ \frac{1}{2}(\Delta\theta(x,t) - |\nabla\theta(x,t)|div\left(\frac{\nabla\theta(x,t)}{|\nabla\theta(x,t)|}\right) \end{aligned} \tag{1.13}$$

This evolution equation has been used for image segmentation tasks leading to stochastic active contours [10]. It is the basis of the approaches presented in the following. Some proper type of solutions can be defined for these equations with stochastic viscosity solutions [10].

1.3 Binary Tomography Reconstructions of Bone Microstructure from Few Projections with Stochastic Level-Set Methods

1.3.1 The Binary Tomography Problem

The tomographic reconstruction from few projections is a very ill-posed problems with many applications in medical imaging or material science. The binary tomography methods can be used to set a simpler inverse problem [13]. The binary tomography problem can be formulated as an under-determined linear system of equations with the linear Radon projection operator R and binary constraints:

$$Rf = p^{\delta} \quad f = (f_1, \dots, f_n) \in \{0, 1\}^n \tag{1.14}$$

relating the pixel values $(f_i)_{1 \le i \le n}$ of the image and the noisy projection data p^{δ} . Very often it is assumed that the non-noisy projections p are corrupted by an additive Gaussian noise.

Various approaches have been investigated to solve this reconstruction problem [14, 15, 19, 20]. The minimization of a functional with a data term and a binary constraint may be performed with stochastic techniques [16] or convex analysis optimization [17, 18]. A variational method based on Total Variation regularization can also be used for this reconstruction problem [21–23].

Yet, the discrete tomography problem is non-convex and the reconstructed solution may be trapped in local minima of the regularization functional. The reconstruction errors are very often localized on the boundaries [22]. We use here stochastic level-set methods for the discrete tomography problem to improve the reconstruction obtained with a deterministic level-set scheme [22, 23]. The reconstruction results obtained with this new approach are compared with the ones obtained with the classical simulated annealing method [24–26] in terms of reconstruction quality and convergence speed.

1.3.2 Global Optimization with Stochastic Level-Set Evolution and Simulated Annealing

1.3.2.1 Stochastic Level-Set Evolution

We use here the level-set regularization and represent the function f with a level-set function θ , $f = H(\theta)$. Let Ω be the domain of the image to be reconstructed, we propose to improve the reconstruction image with the following stochastic partial differential equation for the level-set function θ , for $x \in \Omega$, given by:

$$d\theta(x,t) = \delta\theta(x,t) + \mu(t)|\nabla\theta(x,t)|odW(t)$$
(1.15)

where *o* denotes the Stratanovich convention [12] and $\delta\theta$ is the gradient calculated as explained in Section II.A, Eq. 1.6.

As explained in Section II.B, using the definition of the Stratonovich integral, the equation can be transformed to get the following Itô stochastic differential equation:

$$d\theta(x,t) = \delta\theta + |\nabla\theta(x,t)|dW(t) + \frac{1}{2}(\Delta\theta(x,t) - |\nabla\theta(x,t)|div\left(\frac{\nabla\theta(x,t)}{|\nabla\theta(x,t)|}\right)$$
(1.16)

The level-set and stochastic level-set schemes are applied successively on random time intervals. In the framework of the intermittent diffusion algorithm, the coefficient for the intermittent diffusion is defined as:

$$\mu(t) = \sum_{j} \mu_{j} I_{[S_{j}, T_{j}]}(t)$$
(1.17)

where $I_{[S_j,T_j]}$ is the characteristic function of the interval $[S_j, T_j]$. The time intervals length and the diffusion strengths μ_j are chosen at random in the range [0, T] and $[0, \mu_{max}]$ where μ_{max} is the scale for the diffusion strength and T is the scale for the diffusion time [8]. With probability arbitrarily close to 1, the intermittent diffusion method can find the global minimum of the regularization functional in a finite simulation time.

1.3.2.2 Classical Simulated Annealing

Simulated annealing methods are reviewed extensively in [24–26]. Let f_b be the binary reconstructed image, and U the data term $U = ||Rf_b - p^{\delta}||$, our aim is to minimize the objective function U on a finite configuration space E which is the set of binary images:

$$E = \{ f_b = (f_k)_{1 \le k \le N} \quad f_k \in \{0, 1\} \quad \forall k \in [1, N] \}$$
(1.18)

The classical simulated annealing algorithm is based on the definition of a Markov chain, $(f^n)_{n \in \mathbb{N}}$ on the finite state space E. Each point f^n in the state space is defined by the set $(f_k^n)_{0 \le k \le N}$ of the pixel values. A stochastic search is performed on E with a "cooling down" algorithm. The boundary between the 0 and the 1 regions is first calculated with a Sobel filter. Then one pixel is selected at random on the boundary and is changed and this rule defines the neighborhood system $N(f_b)$ of a point $f_b \in E$:

$$g_b \in N(f_b) \iff \exists !k, f_k \neq g_k \tag{1.19}$$

It is thus possible to define a communication kernel $q_0(f,g)$, in which all the new states in the neighbourhood of f are equiprobable:

$$q_0(f_b, g_b) = \begin{cases} \frac{1}{|N(f_b)|} & \text{if } g_b \in N(f_b) \\ 0 & \text{otherwise} \end{cases}$$
(1.20)

The classical simulated annealing algorithm defines an inhomogeneous Markov chain, with transitions constructed recursively as follows: $P(f^{n+1} = g|f^n = f) = q(f,g)$ with

$$q(f,g) = \begin{cases} q_0(f,g)exp(-\beta_n(U(g) - U(f))^+ & \text{if } g \neq f \\ 1 - \sum_{h \neq f} q(f,h) & \text{if } g = f \end{cases}$$
(1.21)

where [a]+=max(a,0), $(\beta_n)_{n \in \mathbb{N}}$ the cooling schedule, f^0 an arbitrary initial point.

From the current state f^n , a test image f_{test} is sampled randomly according to Eqs. 1.20 and 1.21. If $U(f_{test}) > U(f^n)$ the proposal f_{test} may be accepted. In the beginning of the simulation, the temperature is high and the state space is explored freely. As β increases, the images distribution is more and more concentrated around the minima of U [24–26]. Under some restricting conditions on the cooling schedule, the convergence towards the global minimum is obtained by the convergence rate may be very slow. Several techniques have been used to speed up the simulated annealing method but the modifications are rather empirical [27, 28] and the results obtained seems to be very dependent on the complexity of the objective function. They will not be considered here.

1.3.3 Comparison of the Algorithms: Results and Discussion

1.3.3.1 Simulation Details

The simulated annealing algorithm and stochastic level-set methods have applied to simulated projections of an experimental bone cross-section acquired with synchrotron micro-CT (voxel size:15 μ m) [29]. Figure 1.1 displays the 256×256 bone cross-section *f*^{*} reconstructed from 400 projections with 400 rays per projections with Filtered Back Projection (FBP). The discrete approximation of the Radon transform is the operator implemented in the Matlab Toolbox.

First, the deterministic level-set scheme regularization is applied. To obtain a good accuracy, the ϵ was set to $\epsilon = 0.03$. The initial level-set function chosen is $\theta_0 = 0$. The regularization parameters were chosen to obtain the best decrease of the regularization functional. The iterations are stopped when the iterates stagnate, $||f_{k+1} - f_k||_2 < 0.01$. At the end of this first optimization step,



FIGURE 1.1 Reconstruction of the bone cross-section from 400 projections with the FBP algorithm. The bone fraction is 14.20%.

the Morozov discrepancy principle [30] is not satisfied. The discrepancy term is much higher than the noise level, $||p^{\delta} - Rf|| >> \delta$. This image is the initial image used for the application of the stochastic algorithms. For the simulated annealing algorithm, the initial temperature value is chosen so that most transitions are accepted, with an acceptance ratio around 0.8.

For the simulation of Eq. 1.16, we use an explicit scheme with finite differences, the WENO scheme with $\Delta x = 0.5$ and $\Delta t = 0.1$. The noise strength μ and the number of iterations *T* are chosen randomly with a uniform distribution in [0.01, 0.1] and [1, 100]. A binary image is then obtained by thresholding and a signed distance is then used for reinitializations before the stochastic level-set step. The optimization method was applied for *M* equally spaced noisy projections, with M = 10 and M = 15, with N = 367 rays per projections and with a Gaussian noise added to the projections with a standard deviation $\sigma_p = 3$ (PSNR=20 dB) and $\sigma_p = 6.5$ (PSNR=7 dB). The noise level δ can estimated by $\delta = \sqrt{MN}\sigma_p$.

1.3.3.2 Numerical Results

The reconstructed cross-sections obtained with 10 projections and 367 rays per projection, for the standard deviation $\sigma_p = 3$ after the level-set algorithm and after the stochastic level-set algorithm are displayed in Figure 1.2a and Figure 1.3a respectively. The difference maps are displayed in Figure 1.2b and Figure 1.3b. The reconstruction errors on the boundaries of the homogeneous regions are reduced.

At the end of the deterministic optimization, the discrepancy term $||Rf - p^{\delta}||$ is well-above the noise level for different number of projections. A local minimum is obtained and the level-set algorithm can not escape this



FIGURE 1.2

(a) Reconstruction of the bone cross-section from 10 noisy projections ($\sigma_p = 3$) with the levelset regularization method. The misclassification rate is 3.29% and the bone fraction is 12.27% (b) Error map.



FIGURE 1.3

(a) Reconstruction of the bone cross-section from 10 noisy projections ($\sigma_p = 3$) with the stochastic level-set regularization method. The misclassification rate is 2.56% and the bone fraction is 14.14% (b) Error map.

local minimum. With the iterations, a significant decrease of the data term is obtained towards these noise levels for both stochastic methods.

The decrease of the misclassification rate as a function of the number of iterations is displayed in Figure 1.4 for the same number of projections and noise levels. The misclassification rates obtained at the end of the simulations are summarized in Table 1.1. Better reconstruction results are obtained with



FIGURE 1.4

Evolution of the misclassification rate with the iteration number (i) M = 15, $\sigma_p = 6.5$ (ii) M = 10, $\sigma_p = 6.5$ (iii) M = 15, $\sigma_p = 3$ (iv) M = 10, $\sigma_p = 3$. The dotted lines corresponds to the simulated annealing and the plain lines to the stochastic level method.

TABLE 1.1

Misclassification Rates Obtained with the Stochastic Algorithms

	Simulated Annealing	Stochastic Level-Set
$\sigma_p = 3, M = 15$	1.89	1.56
$\sigma_p = 3, M = 10$	3.12	2.55
$\sigma_{v} = 6.5, M = 15$	2.9	2.48
$\sigma_p = 6.5, M = 10$	4.23	3.97

the stochastic level-set algorithm than with the simulated annealing minimization, for all noise levels and numbers of projections. At the end of the simulations, the errors on the boundary of the images are much lower.

1.4 Stochastic Level-Set Reconstruction in Nonlinear Phase Contrast Tomography

In this section, we detail the results obtained with stochastic level-set methods for phase contrast tomography. The inverse problem considered is nonlinear but the optimization methodology is very similar to the one applied to the binary tomography problem.

1.4.1 Nonlinear Phase Contrast Tomography

X-ray in-line phase contrast tomography is a very sensitive technique for soft tissues within dense materials. This imaging technique is based on a coupling of tomography and phase retrieval [31, 32] and it aims at reconstructing the complex refractive index [33]. For coherent X-rays obtained with synchrotrons, the Fresnel intensity is recorded for one or several propagation distances and for several projection angles after interaction of the X-rays with the object [34,35]. The inverse problem set by the reconstruction of the refractive index is nonlinear.

For volumes with several homogeneous materials, the imaginary and real part of the index are piecewise constant [33], and the level-set regularization can account for this a priori on the index map. Assuming that the discrete real and imaginary parts of the index are known, the inverse problem is then formulated as a shape optimization problem. Yet, the nonlinear phase contrast tomography problem is non-convex and the reconstructed solution obtained with the deterministic level-set regularization is a local minimum. We investigate here stochastic perturbations of the boundaries performed with tools similar to the ones used for binary tomography in [36] to improve the reconstruction and escape the critical point of the cost functional obtained with the deterministic method.

1.4.2 Level-Set Regularization in In-Line Phase Contrast Tomography

The real and imaginary parts of the complex refractive index to reconstruct from the Fresnel intensity measurements, denoted as δ and β are defined on a 3D bounded domain (Σ) with spatial coordinates (x, y, z). We denote (x_{θ} , y_{θ} , z) be the rotated spatial coordinate system for an angle θ around the z-axis (Figure 1.5). The sample is irradiated with a monochromatic, coherent, parallel X-ray beam propagating in the y_{θ} direction with the wavelength λ . The complex refractive index is given by [37, 38]:

$$n(x, y, z) = 1 - \delta(x, y, z) + i\beta(x, y, z)$$
(1.22)

where δ is the refractive index decrement and β is the absorption index. Let $X_{\theta} = (x_{\theta}, z)$, the intensity detected at a distance *D* after the sample is given by the squared modulus of the following convolution product [33]:

$$I_{D,\theta}(X_{\theta}) = |T_{\theta}(X_{\theta}) * P_D(X_{\theta})|^2$$
(1.23)

where the Fresnel propagator is written:

$$P_D(X_{\theta}) = \frac{1}{i\lambda D} exp\left(i\frac{\pi}{\lambda D}|X_{\theta}|^2\right).$$
(1.24)

The transmittance function T_{θ} is given by:

$$T_{\theta}(X_{\theta}) = \exp[-B_{\theta}(X_{\theta}) + i\varphi_{\theta}(X_{\theta})]$$
(1.25)



FIGURE 1.5

Experimental set-up in propagation based phase contrast tomography with a single propagationdistance showing the X-ray beam, the rotated coordinate system (x_{θ} , y_{θ} , z) for a rotation angle θ , the sample, and the detector. with

$$B_{\theta}(X_{\theta}) = \frac{2\pi}{\lambda} \int \beta(y_{\theta}, X_{\theta}) dy_{\theta}$$
(1.26)

and

$$\varphi_{\theta}(X_{\theta}) = \frac{2\pi}{\lambda} \int (1 - \delta(y_{\theta}, X_{\theta})) dy_{\theta}$$
(1.27)

Let $L(\theta, x_{\theta})$ the line defined by $L(\theta, x_{\theta}) = \{y_{\theta}\bar{\theta}^* + x_{\theta}\bar{\theta} : \tau \in \mathbb{R}\}$, with $\bar{\theta} = (\cos(\theta), \sin(\theta))$ and $\bar{\theta}^* = (-\sin(\theta), \cos(\theta))$, for parallel beam projection, with a beam parallel to the X = (x, y) plane and $f \in L^1(\Sigma)$, the Radon transform of f is defined as:

$$Rf(\theta, x_{\theta}, z) = R_{\theta} f(x_{\theta}) = \int_{t \in L(\theta, x_{\theta}, z) \cap \Sigma} f(t) dt$$
(1.28)

where $L(\theta, x_{\theta}, z)$ is the $L(\theta, x_{\theta})$ line for the coordinate z. The intensity $I_{D,\theta}$ can be reformulated with the Radon transform R.

For simplicity, we assume that δ and β are piecewise constant and that they can take two values δ_1 , δ_2 and β_1 , β_2 on disjoint subsets Σ_1 , Σ_2 such that $\Sigma = \Sigma_1 \cup \Sigma_2$. In order to represent the unknown functions δ and β , we have used a level-set function of the first order Sobolev space $\eta \in H_1(\Sigma)$:

$$\beta = \beta_1 + H(\eta)(\beta_2 - \beta_1)$$
(1.29)

$$\delta = \delta_1 + H(\eta)(\delta_2 - \delta_1) \tag{1.30}$$

A variational approach is considered with the following regularization functional:

$$F[\eta] = \|I_{D,\theta}[\eta] - I_{\delta_{\eta}}\|_{2}^{2} + \alpha_{1} \left(\|\eta\|_{L_{2}}^{2} + \||\nabla\eta|\|_{L_{2}}^{2}\right)$$
(1.31)

where I_{δ_n} are the noisy intensity data and α_1 a regularization parameter.

The minimizers of the regularization are found numerically with first order optimality conditions for the smoothed functional where the Heaviside function is replaced by its approximation:

$$I_{D,\theta}^{\prime*}[\eta][I_{D,\theta}[\eta] - I_{\delta_n}] + \alpha_1(I - \Delta)[\eta] = 0$$
(1.32)

where I_D^{**} denotes the adjoint of the Fréchet derivative of the intensity operator with respect to L_2 spaces. *I* represent identity and Δ the Laplacian operator. The solutions of the optimality system are obtained with a Gauss-Newton method. The update is given by $\eta_{k+1} = \eta_k + \delta \eta$ and $\delta \eta$ is obtained with the linear system:

$$\left(\left[I_{D,\theta}^{\prime*}[\eta^{k}]I_{D,\theta}^{\prime}[\eta^{k}]\right)\delta\eta + \alpha_{1}(I-\Delta)\delta\eta = -F^{\prime}[\eta^{k}]\right)$$
(1.33)

An explicit formula can be derived for the Fréchet derivative of the intensity $I_D[\delta, \beta]$ and its adjoint are given in [39].

1.4.3 Stochastic Level-Set Methods for Phase Contrast Tomography

<u>Stochastic level-set evolution</u> The deterministic optimization of the level-set function is often stopped in local minima. We propose to improve the reconstruction image obtained with the deterministic level-set evolution with the following stochastic partial differential equation for the level-set function η , for $\vec{r} \in \Sigma$ by:

$$d\eta(\vec{r},t) = \delta\eta(\vec{r},t) + \rho(t)|\nabla\eta(\vec{r},t)|odW(t)$$
(1.34)

where *o* denotes the Stratanovitch convention and $\delta\eta$ is the deterministic change calculated with the Gauss-Newton method of Eqs. 1.32, 1.33 as explained in the former section. We obtain the following Itô stochastic differential equation with the definition of the Stratonovich integral:

$$d\eta(\vec{r},t) = \delta\eta + \rho(t) |\nabla\eta(\vec{r},t)| dW(t) + \frac{1}{2}\rho(t)(\Delta\eta(\vec{r},t)) - |\nabla\eta(\vec{r},t)| div \left(\frac{\nabla\eta(\vec{r},t)}{|\nabla\eta(\vec{r},t)|}\right)$$
(1.35)

The deterministic level-set and stochastic level-set schemes are applied successively on random time intervals with an intermittent diffusion similar to the one proposed for the binary tomography. For the stochastic evolution, the time interval lengths and the diffusion strengths ρ are chosen at random with a uniform distribution in the range $[0, T_{max}]$ and $[0, \rho_{max}]$ where ρ_{max} is the scale for the diffusion strength and T_{max} is the scale for the diffusion time.

The minimization scheme is summarized in Algorithm 1:

Algorithm 1

Let Δt be the time step of the discretization of Eq. 1.35, For k=1 to Maxiter:

Step 1: chose a projection angle θ at random with a uniform distribution, chose at random $t \in [0, T_{max}]$, and $\rho \in [0, \rho_{max}]$, for the iteration number $N_{iter,sto} = t/\Delta t$, use the discrete version of Eq. 1.35.

Step 2: calculate $\delta \eta$ with Eqs. 1.32, 1.33, for $N_{iter,deterministic} = 100$ iterations.

Step 3: reinitialize the level-set function η with the signed distance function.

end

The derivative in Eq. 1.32 and Eq. 1.33 describes the sensitivity of the regularization functional with respect to deterministic changes of shape of the boundary between the regions of constant values of the index. The equation Eq. 1.35 corresponds to stochastic perturbations of the geometry. Topology changes like splitting and merging of domains can be obtained with the levelset approach [40]. It has also been proposed to add some new components or small holes far from the boundaries to modify the topology of the reconstructed images [39].

1.4.4 Numerical Results and Discussion

In the following, we compare the deterministic level-set algorithm with the modified algorithms with the stochastic evolution.

1.4.4.1 Simulation Details

The deterministic and intermittent stochastic level-set algorithms and the deterministic algorithm are compared in this section on one multi-material object made up of two homogeneous materials. It is possible to extend these results to objects with more than two materials with multi-level regularization.

The simulated test object (O_1) consists of an Al cylinder of 20 μm in diameter and 110 μm in height embedded in PMMA. Some horizontal sections of the β and δ maps of the simulated object (O_1) are displayed in Figure 1.6.

Let $\mu = \frac{4\pi\beta}{\lambda}$, the δ and μ values used for PMMA and Al for 24 keV X-rays are summarized in Table 1.2. The β and δ values were discretized on a regular grid with a pixel size of 1.5 μ m. The cylinder is included in a rectangular volume of size $N_1 \times N_1 \times N_2$ pixels with $N_1 = 74$ and $N_2 = 109$ used for the simulations. The number of projection angles N_{θ} used for the simulation are $N_{\theta} = 75,125$ and 180. A single sample-to-detector distance D = 100 mm is considered. The Radon transform is the projection operator implemented in the Mablab Toolbox. The intensity data were corrupted with additive Gaussian white noise. This noise distribution corresponds to the noise measured experimentally. The signal to noise ratio was measured with the peak-to-peak signal to noise ratio (PPSNR). To obtain a good accuracy, the ϵ parameter of the smooth approximation of the Heaviside function was fixed to $\epsilon = 0.03$.



FIGURE 1.6 Ground truth β and δ maps for the object (O_1).

TABLE 1.2

Values of the δ and μ Values for the Materials in the Object, at 24 keV X-rays from http://henke.lbl.gov/optical_constants Material $\delta(10^{-7})$ $\mu(m^{-1})$

ð(10 ⁻⁷)	$\mu(m^{-1})$	
4.628	41.2	
9.396	502.6	
	4.628 9.396	

In order to evaluate the efficiency of the reconstruction, the relative mean square errors (RMSE) using the $L_2(\Sigma)$ norm, $\|\delta^* - \delta\|_2 / \|\delta^*\|_2$ and $\|\beta^* - \beta\|_2 / \|\beta^*\|_2$ have been studied. Let $D_k = \frac{\|I_{D,\theta}[\eta_k] - I_{\delta_n}\|}{\|I_{\delta_n}\|}$ the value of the data term for the projection angle θ and the value η_k . The iterations are stopped when the average value of the variation of the data term $D_{k+1} - D_k$ evaluated on 10 iterations is below 0.05.

1.4.4.2 Numerical Results for Deterministic Level-Set Method

For piecewise constant δ and β maps, the reconstruction results are improved with the level-set regularization with respect to Tikhonov regularization because some a priori information on the possible values of δ and β is included. Some simulations have been performed to reconstruct the object (O_1) with an initial diameter of the central Al cylinder equal to 40 μm , twice the diameter of the cylinder to be reconstructed and noise levels of 30 and 48 dB. With this starting map for the refractive index, the inverse problem is an easier shape optimization problem in which only the possible discrete values of the real and imaginary parts of the refractive index are known but not the shape of the regions where the refractive index takes constant values.

Figure 1.7 displays the horizontal section of the initial β and δ maps. Figure 1.8 presents some horizontal sections of the errors for the real and imaginary part of the reconstructed index map for a PPSNR of 48 dB after 500 iterations. These figures show that the reconstruction errors have been significantly reduced. Some errors are still present on the boundaries between the



FIGURE 1.7 Horizontal section of the initial β and δ maps for the object (0₁).



FIGURE 1.8

Horizontal section of the final error map for β and δ for a PPSNR of 48 dB.

two materials. Similar results are obtained for the other sections and the noise level of 30 dB with reconstruction errors at the interface between the different regions.

In order to have more quantitative information about the convergence of the method, the evolution of the relative mean square errors (RMSE) $\|\delta^* - \delta\|_2 / \|\delta^*\|_2$ and $\|\beta^* - \beta\|_2 / \|\beta^*\|_2$, are displayed as a function of the number of iterations for a PPSNR of 30 dB and 48 dB in Figures 1.9 and 1.10. The relative mean square errors on the two components β and δ of the refractive index are much decreased.

1.4.4.3 Deterministic Level-Set versus Stochastic Level-Set Algorithm

For higher noise levels and initializations maps with very different shape from the ground truth, the level-set regularization algorithm may be stuck in local optima. The stochastic level-set algorithm improves the reconstruction results. In order to perform a comparison of the deterministic and stochastic level-set algorithm, a first reconstruction is performed on the simulated



FIGURE 1.9

Evolution of the RMSE on δ with the iterations for the noise levels 30 dB (dotted line) and 48 dB (plain line).



FIGURE 1.10

Evolution of the RMSE on β with the iterations for the noise levels 30 dB (dotted line) and 48 dB (plain line).

object (O_1). The initial guess is a large cylinder with a diameter twice the diameter of the object (O_1). Then algorithm 1 is applied to this initial reconstruction for PPSNR of 24 and 18 dB. Following algorithm 1, the numbers of stochatic iterations are chosen randomly with a uniform distribution between 1 and 50 and the noise strength in the range [$1, 10^{-3}$]. For the simulation of Eq. 1.35, we use an explicit scheme with finite differences, the WENO scheme [41] with $\Delta x = 0.1$ and $\Delta t = 0.01$. An iterated deterministic minimization is performed for comparison with periodic reinitialization of the level-set function and projection angles chosen at random.

The evolutions of the data term, $||I_{D,\theta}[\eta] - I_{\delta_n}|| / ||I_{\delta_n}||$ are displayed in Figure 1.11 for the deterministic and intermittent stochastic algorithms



FIGURE 1.11

Evolution of the data term for the deterministic level-set algorithm for 24 dB (black line), for the intermittent stochastic level-set algorithm for 24 dB (blue line) and for the intermittent stochastic level-set algorithm for 18 dB (dotted line).


FIGURE 1.12

TABLE 1.3

Evolution of the RMSE for β and δ for the deterministic level-set algorithm for 24 dB (black line), for the intermittent stochastic level-set algorithm for 24 dB (blue line) and for the intermittent stochastic level-set algorithm for 18 dB (dotted line).

starting from the initial reconstruction for the noise levels 18 dB and 24 dB. The deterministic algorithm is not efficient to achieve lower reconstruction errors. Different behaviours are obtained depending on the random projection angles θ for similar noise levels. Yet, after hundred iterations, only small fluctuations are observed on the real and imaginary parts of the refractive index, β and δ , and the uncertainty on the RMSE given in the Tables is below 5% for a given noise level.

The evolution of the normalized mean square error, $\|\delta^* - \delta\|_2 / \|\delta^*\|_2$ and $\|\beta^* - \beta\|_2 / \|\beta^*\|_2$, are displayed as a function of the number of iterations for the deterministic and stochastic algorithms in Figure 1.12. The iterated deterministic minimization can not escape the local minimum corresponding to the initial reconstructed δ and β volumes. A larger decrease is obtained with the stochastic scheme. Table 1.3 presents the reconstruction quality results for different noise levels and the different algorithms. The results correspond to an average over three trials. This table shows the efficiency of the stochastic optimization.

Some horizontal sections of the difference image between the ground truth image and the reconstructed real index map obtained for the minimum of the discrepancy term for 24 dB with the stochastic or the deterministic methods are displayed in Figure 1.13. These figures show that the

	RMSE β , LS	RMSE δ,LS	RMSE β , Stochastic LS	RMSE δ, Stochastic LS
PPSNR=18 dB	0.28	0.85	0.15	0.55
PPSNR=24 dB	0.22	0.80	0.06	0.26

RMSE for β and δ for Deterministic Level-Set and Stochastic Level-Set



FIGURE 1.13

Horizontal section of the difference image between the ground truth and the reconstructed β maps with the stochastic and the deterministic level-set algorithms for the noise level 24 dB.

reconstruction errors have been significantly reduced. Similar results are obtained for the imaginary part of the refractive index.

1.4.5 Conclusion

We have studied some aspects of the nonlinear inverse problem associated with the reconstruction of the real and imaginary parts of the refractive index in phase contrast tomography and with the binary tomographic reconstruction problem. Both are regularized with level-set functions and with Total-Sobolev penalty term. The deterministic optimization of the regularization functional leads to local minima with large reconstruction errors. The reconstruction results are improved with a stochastic perturbation of the shape of the reconstructed regions with a stochastic level-set evolution. The evolution is based on a stochastic partial differential equation with the Stratonovich formulation. The stochastic algorithm leads to a decreased reconstruction errors localized on the boundaries for different noise levels. The method gives better reconstruction results than the classical simulated annealing method.

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Level Set Methods for Cardiac Segmentation in MSCT Images

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Deformable Models and Image Segmentation

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Cardiac Image Segmentation Using Generalized Polynomial Chaos Expansion and Level Set Function

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11

Level Set Method in Medical Imaging Segmentation

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Image Segmentation With B-Spline Level Set

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