

Book of Short Papers SIS 2018

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Contents

1	Preface	17
2	Plenary Sessions	19
2.1	A new paradigm for rating data models. <i>Domenico Piccolo</i>	19
2.2	Statistical challenges and opportunities in modelling coupled behaviour-disease dynamics of vaccine refusal. <i>Plenary/Chris T. Bauch</i>	32
3	Specialized Sessions	45
3.1	3.1 - Bayesian Nonparametric Learning	45
3.1.1	Bayesian nonparametric covariate driven clustering. <i>Raffaele Argiento, Ilaria Bianchini, Alessandra Guglielmi and Ettore Lanzarone</i>	46
3.1.2	A Comparative overview of Bayesian nonparametric estimation of the size of a population. <i>Luca Tardella and Danilo Alunni Fegatelli</i>	56
3.1.3	Logit stick-breaking priors for partially exchangeable count data. <i>Tommaso Rigon</i>	64
3.2	BDsports - Statistics in Sports	72
3.2.1	A paired comparison model for the analysis of on-field variables in football matches. <i>Gunther Schaubberger and Andreas Groll</i>	72
3.2.2	Are the shots predictive for the football results?. <i>Leonardo Egidi, Francesco Paoli, Nicola Torelli</i>	81
3.2.3	Zero-inflated ordinal data models with application to sport (in)activity. <i>Maria Iannario and Rosaria Simone</i>	89
3.3	Being young and becoming adult in the Third Millennium: definition issues and processes analysis	97
3.3.1	Do Social Media Data predict changes in young adults' employment status? Evidence from Italy. <i>Andrea Bonanomi and Emiliano Sironi</i>	97

3.3.2	Parenthood: an advanced step in the transition to adulthood. <i>Cinzia Castagnaro, Antonella Guarneri and Eleonora Meli</i>	106
3.4	Economic Statistics and Big Data	114
3.4.1	Improvements in Italian CPI/HICP deriving from the use of scanner data. <i>Alessandro Brunetti, Stefania Fatello, Federico Polidoro, Antonella Simone</i>	114
3.4.2	Big data and spatial price comparisons of consumer prices. <i>Tiziana Laureti and Federico Polidoro</i>	123
3.5	Financial Time Series Analysis	131
3.5.1	Dynamic component models for forecasting trading volumes. <i>Antonio Naimoli and Giuseppe Storti</i>	131
3.5.2	Conditional Quantile-Located VaR. <i>Giovanni Bonaccolto, Massimiliano Caporin and Sandra Paterlini</i>	140
3.6	Forensic Statistics	146
3.6.1	Cause of effects: an important evaluation in Forensic Science. <i>Fabio Corradi and Monica Musio</i>	146
3.6.2	Evaluation and reporting of scientific evidence: the impact of partial probability assignments. <i>Silvia Bozza, Alex Biedermann, Franco Taroni</i>	155
3.7	Missing Data Handling in Complex Models	161
3.7.1	Dependence and sensitivity in regression models for longitudinal responses subject to dropout. <i>Marco Alfo' and Maria Francesca Marino</i>	161
3.7.2	Multilevel analysis of student ratings with missing level-two covariates: a comparison of imputation techniques. <i>Maria Francesca Marino e Carla Rampichini</i>	170
3.7.3	Multilevel Multiple Imputation in presence of interactions, non-linearities and random slopes. <i>Matteo Quartagno and James R. Carpenter</i>	175
3.8	Monitoring Education Systems. Insights from Large Scale Assessment Surveys	183
3.8.1	Educational Achievement of Immigrant Students. A Cross-National Comparison Over-Time Using OECD-PISA Data. <i>Mariano Porcu</i>	183
3.9	New Perspectives in Time Series Analysis	192
3.9.1	Generalized periodic autoregressive models for trend and seasonality varying time series. <i>Francesco Battaglia and Domenico Cucina and Manuel Rizzo</i>	192
3.10	Recent Advances in Model-based Clustering	201
3.10.1	Flexible clustering methods for high-dimensional data sets. <i>Cristina Tortora and Paul D. McNicholas</i>	201
3.10.2	A Comparison of Model-Based and Fuzzy Clustering Methods. <i>Marco Alfo', Maria Brigida Ferraro, Paolo Giordani, Luca Scrucca, and Alessio Serafini</i>	208
3.10.3	Covariate measurement error in generalized linear models for longitudinal data: a latent Markov approach. <i>Roberto Di Mari, Antonio Punzo, and Antonello Maruotti</i>	216
3.11	Statistical Modelling	224
3.11.1	A regularized estimation approach for the three-parameter logistic model. <i>Michela Battauz and Ruggero Bellio</i>	224
3.11.2	Statistical modelling and GAMLSS. <i>Mikis D. Stasinopoulos and Robert A. Rigby and Fernanda De Bastiani</i>	233
3.12	Young Contributions to Statistical Learning	239
3.12.1	Introducing spatio-temporal dependence in clustering: from a parametric to a nonparametric approach . <i>Clara Grazian, Gianluca Mastrantonio and Enrico Bibbona</i>	239

3.12.2	Bayesian inference for hidden Markov models via duality and approximate filtering distributions. <i>Guillaume Kon Kam King, Omiros Papaspiliopoulos and Matteo Ruggiero</i>	248
3.12.3	K-means seeding via MUS algorithm. <i>Leonardo Egidi, Roberta Pappada', Francesco Pauli, Nicola Torelli</i>	256
4	Solicited Sessions	263
4.1	Advances in Discrete Latent Variable Modelling	263
4.1.1	A joint model for longitudinal and survival data based on a continuous-time latent Markov model. <i>Alessio Farcomeni and Francesco Bartolucci</i>	264
4.1.2	Modelling the latent class structure of multiple Likert items: a paired comparison approach. <i>Brian Francis</i>	273
4.1.3	Dealing with reciprocity in dynamic stochastic block models. <i>Francesco Bartolucci, Maria Francesca Marino, Silvia Pandolfi</i>	281
4.1.4	Causality patterns of a marketing campaign conducted over time: evidence from the latent Markov model. <i>Fulvia Pennoni, Leo Paas and Francesco Bartolucci</i>	289
4.2	Complex Spatio-temporal Processes and Functional Data	297
4.2.1	Clustering of spatio-temporal data based on marked variograms. <i>Antonio Balzanella and Rosanna Verde</i>	297
4.2.2	Space-time earthquake clustering: nearest-neighbor and stochastic declustering methods in comparison. <i>Elisa Varini, Antonella Peresan, Renata Rotondi, and Stefania Gentili</i>	304
4.2.3	Advanced spatio-temporal point processes for the Sicily seismicity analysis. <i>Marianna Siino and Giada Adelfio</i>	312
4.2.4	Spatial analysis of the Italian seismic network and seismicity. <i>Antonino D'Alessandro, Marianna Siino, Luca Greco and Giada Adelfio</i>	320
4.3	Dimensional Reduction Techniques for Big Data Analysis	328
4.3.1	Clustering Data Streams via Functional Data Analysis: a Comparison between Hierarchical Clustering and K-means Approaches. <i>Fabrizio Mauro, Francesca Fortuna, and Tonio Di Battista</i>	328
4.3.2	Co-clustering algorithms for histogram data. <i>Francisco de A.T. De Carvalho and Antonio Balzanella and Antonio Irpino and Rosanna Verde</i>	338
4.3.3	A network approach to dimensionality reduction in Text Mining. <i>Michelangelo Misuraca, Germana Scepi and Maria Spano</i>	344
4.3.4	Self Organizing Maps for distributional data. <i>Rosanna Verde and Antonio Irpino</i>	352
4.4	Enviromental Processes, Human Activities and their Interactions	353
4.4.1	Estimation of coral growth parameters via Bayesian hierarchical non-linear models. <i>Crescenza Calculli, Barbara Cafarelli and Daniela Cocchi</i>	353
4.4.2	A Hierarchical Bayesian Spatio-Temporal Model to Estimate the Short-term Effects of Air Pollution on Human Health. <i>Fontanella Lara, Ippoliti Luigi and Valentini Pasquale</i>	361
4.4.3	A multilevel hidden Markov model for space-time cylindrical data. <i>Francesco Lagona and Monia Ranalli</i>	367
4.4.4	Estimation of entropy measures for categorical variables with spatial correlation. <i>Linda Altieri, Giulia Roli</i>	373
4.5	Innovations in Census and in Social Surveys	381
4.5.1	A micro-based approach to ensure consistency among administrative sources and to improve population statistics. <i>Gianni Corsetti, Sabrina Prati, Valeria Tomeo, Enrico Tucci</i>	381
4.5.2	Demographic changes, research questions and data needs: issues about migrations. <i>Salvatore Strozza and Giuseppe Gabrielli</i>	392

4.5.3	Towards more timely census statistics: the new Italian multiannual dissemination programme. <i>Simona Mastroluca and Mariangela Verrascina</i>	400
4.6	Living Conditions and Consumption Expenditure in Time of Crises	409
4.6.1	Household consumption expenditure and material deprivation in Italy during last economic crises. <i>Ilaria Arigoni and Isabella Siciliani</i>	409
4.7	Network Data Analysis and Mining	418
4.7.1	Support provided by elderly Italian people: a multilevel analysis. <i>Elvira Pelle, Giulia Rivellini and Susanna Zaccarini</i>	418
4.7.2	Data mining and analysis of comorbidity networks from practitioner prescriptions. <i>Giancarlo Ragozini, Giuseppe Giordano, Sergio Pagano, Mario De Santis, Pierpaolo Cavallo</i>	426
4.7.3	Overlapping mixture models for network data (manet) with covariates adjustment. <i>Saverio Ranciati and Giuliano Galimberti and Ernst C. Wit and Veronica Vinciotti</i>	434
4.8	New Challenges in the Measurement of Economic Insecurity, Inequality and Poverty	440
4.8.1	Social protection in mitigating economic insecurity. <i>Alessandra Coli</i>	440
4.8.2	Changes in poverty concentration in U.S. urban areas. <i>Francesco Andreoli and Mauro Mussini</i>	450
4.8.3	Evaluating sustainability through an input-stateoutput framework: the case of the Italian provinces. <i>Achille Lemmi, Laura Neri, Federico M. Pulselli</i>	458
4.9	New Methods and Models for Ordinal Data	466
4.9.1	Weighted and unweighted distances based decision tree for ranking data. <i>Antonella Plaia, Simona Buscemi, Mariangela Sciandra</i>	466
4.9.2	A dissimilarity-based splitting criterion for CUBREMOT. <i>Carmela Cappelli, Rosaria Simone and Francesca Di Iorio</i>	474
4.9.3	Constrained Extended Plackett-Luce model for the analysis of preference rankings. <i>Cristina Mollica and Luca Tardella</i>	480
4.9.4	A prototype for the analysis of time use in Italy. <i>Stefania Capecchi and Manuela Michelini</i>	487
4.10	New Perspectives in Supervised and Unsupervised Classification	493
4.10.1	Robust Updating Classification Rule with applications in Food Authenticity Studies. <i>Andrea Cappozzo, Francesca Greselin and Thomas Brendan Murphy</i>	493
4.10.2	A robust clustering procedure with unknown number of clusters. <i>Francesco Dotto and Alessio Farcomeni</i>	500
4.10.3	Issues in joint dimension reduction and clustering methods. <i>Michel van de Velden, Alfonso Iodice D'Enza and Angelos Markos</i>	508
4.11	New Sources, Data Integration and Measurement Challenges for Estimates on Labour Market Dynamics	514
4.11.1	The development of the Italian Labour register: principles, issues and perspectives. <i>C. Baldi, C. Ceccarelli, S. Gigante, S. Pacini</i>	514
4.11.2	Digging into labour market dynamics: toward a reconciliation of stock and flows short term indicators. <i>F. Rapiti, C. Baldi, D. Ichim, F. Pintaldi, M. E. Pontecorvo, R. Rizzi</i>	523
4.11.3	How effective are the regional policies in Europe? The role of European Funds. <i>Gennaro Punzo, Mariateresa Ciommi, and Gaetano Musella</i>	531
4.11.4	Labour market condition in Italy during and after the financial crises: a segmented regression analysis approach of interrupted time series. <i>Lucio Masserini and Matilde Bini</i>	539

4.12	Quantile and Generalized Quantile Methods	547
4.12.1	Multiple quantile regression for risk assessment. <i>Lea Petrella and Valentina Raponi</i>	547
4.12.2	Parametric Modeling of Quantile Regression Coefficient Functions. <i>Paolo Frumento and Matteo Bottai</i>	550
4.12.3	Modelling the effect of Traffic and Meteorology on Air Pollution with Finite Mixtures of M-quantile Regression Models. <i>Simone Del Sarto, Maria Francesca Marino, Maria Giovanna Ranalli and Nicola Salvati</i>	552
4.12.4	Three-level M-quantile model for small area poverty mapping. <i>Stefano Marchetti and Nicola Salvati</i>	560
4.13	Recent Advances on Extreme Value Theory	560
4.13.1	Extremes of high-order IGARCH processes. <i>Fabrizio Laurini</i>	560
4.14	Spatial Economic Data Analysis	569
4.14.1	Spatial heterogeneity in principal component analysis: a study of deprivation index on Italian provinces. <i>Paolo Postiglione, M. Simona Andreano, Roberto Benedetti, Alfredo Cartone</i>	569
4.15	Spatial Functional Data Analysis	578
4.15.1	Object oriented spatial statistics for georeferenced tensor data. <i>Alessandra Menafoglio and Davide Pigoli and Piercesare Secchi</i>	578
4.15.2	A Spatio-Temporal Mixture Model for Urban Crimes. <i>Ferretti Angela, Ippoliti Luigi and Valentini Pasquale</i>	585
4.16	Statistical Methods for Service Quality	591
4.16.1	Cumulative chi-squared statistics for the service quality improvement: new properties and tools for the evaluation. <i>Antonello D'Ambra, Antonio Lucadamo, Pietro Amenta, Luigi D'Ambra</i>	591
4.16.2	A robust multinomial logit model for evaluating judges' performances. <i>Ida Camminatiello and Antonio Lucadamo</i>	600
4.16.3	Complex Contingency Tables and Partitioning of Three-way Association Indices for Assessing Justice CourtWorkload. <i>Rosaria Lombardo, Yoshio Takane and Eric J Beh</i>	607
4.16.4	Finding the best paths in university curricula of graduates to improve academic guidance services. <i>Silvia Bacci and Bruno Bertaccini</i>	615
4.17	Statistical Modelling for Business Intelligence Problems	623
4.17.1	A nonlinear state-space model for the forecasting of field failures. <i>Antonio Pievatolo</i>	623
4.17.2	Does Airbnb affect the real estate market? A spatial dependence analysis. <i>Mariangela Guidolin and Mauro Bernardi</i>	632
4.17.3	Bayesian Quantile Trees for Sales Management. <i>Mauro Bernardi and Paola Stoffi</i>	640
4.17.4	Discrimination in machine learning algorithms. <i>Roberta Pappadá and Francesco Pauli</i>	648
4.18	Statistical models for sports data	656
4.18.1	The study of relationship between financial performance and points achieved by Italian football championship clubs via GEE and diagnostic measures. <i>Anna Crisci, Sarnacchiaro Pasquale e Luigi D'Ambra</i>	656
4.18.2	Exploring the Kaggle European Soccer database with Bayesian Networks: the case of the Italian League Serie A. <i>Maurizio Carpita and Silvia Golia</i>	665
4.18.3	A data-mining approach to the Parkour discipline. <i>Paola Pasca, Enrico Ciavolino and Ryan L. Boyd</i>	673
4.18.4	Players Movements and Team Shooting Performance: a Data Mining approach for Basketball. <i>Rodolfo Metulini</i>	681

4.19	Supporting Regional Policies through Small Area Statistical Methods	689
4.19.1	Survey-weighted Unit-Level Small Area Estimation. <i>Jan Pablo Burgard and Patricia Dörr</i>	689
4.19.2	Robust and model-assisted small area estimation methods: an application to the Banca d'Italia Survey of Industrial and Service Firms. <i>Bottone Marco, Casciano Maria Cristina, Fabrizi Enrico, Filiberti Salvatore, Neri Andrea and Salvati Nicola</i> 698	
4.20	The Second Generation at School	706
4.20.1	Resilient students with migratory background. <i>Anna Di Bartolomeo and Giuseppe Gabrielli</i>	706
4.20.2	Residential Proximity to Attended Schools among Immigrant-Origin Youths in Bologna. <i>Federica Santangelo, Debora Mantovani and Giancarlo Gasperoni</i>	715
4.20.3	From school to ... future: strategies, paths and perspectives of immigrant immediate descendants in Naples . <i>Giustina Orientale Caputo and Giuseppe Gargiulo</i> 723	
4.21	Tourism Destinations, Household, Firms	731
4.21.1	The Pricing Behaviour of Firms in the On-line Accommodation Market: Evidence from a Metropolitan City. <i>Andrea Guizzardi and Flavio Maria Emanuele Pons</i> 731	
4.21.2	The Migration-Led-Tourism Hypothesis for Italy: A Survey. <i>Carla Massidda, Romano Piras and Ivan Etzo</i>	741
4.21.3	Tourism Statistics: development and potential uses. <i>Fabrizio Antolini</i>	749
4.21.4	Tourism attractiveness in Italy. Some empirical evidence comparing origin-destination domestic tourism flows. <i>Francesca Giambona, Emanuela Dreassi, and Alessandro Magrini</i>	757
4.22	What's Happening in Africa	765
4.22.1	Environmental shocks and internal migration in Tanzania. <i>Maria Francesca Marino, Alessandra Petrucci, and Elena Pirani</i>	765
4.22.2	Determinants and geographical disparities of BMI in African Countries: a measurement error small area approach. <i>Serena Arima and Silvia Polettini</i>	773
5	Contributed Sessions	781
5.1	Advanced Algorithms and Computation	781
5.1.1	Brexit in Italy. <i>Francesca Greco, Livia Celardo, Leonardo Salvatore Alaimo</i> . 782	
5.1.2	Distance based Depth-Depth classifier for directional data. <i>Giuseppe Pandolfo and Giovanni C. Porzio</i>	789
5.1.3	Approximate Bayesian Computation for Forecasting in Hydrological models. <i>Jonathan Romero-Cuéllar, Antonino Abbruzzo, Giada Adelfio and Félix Francés</i>	793
5.1.4	Customer Churn prediction based on eXtreme Gradient Boosting classifier. <i>Mohammed Hassan Elbedawi Omar and Matteo Borrotti</i>	799
5.1.5	HPC-accelerated Approximate Bayesian Computation for Biological Science. <i>Ritabrata Dutta</i>	805
5.1.6	PC Algorithm for Gaussian Copula Data. <i>Vincenzina Vitale and Paola Vicard</i> 813	
5.2	Advances in Clustering Techniques	819
5.2.1	On the choice of an appropriate bandwidth for modal clustering. <i>Alessandro Casa, José E. Chacón and Giovanna Menardi</i>	819
5.2.2	Unsupervised clustering of Italian schools via non-parametric multilevel models. <i>Chiara Masci, Francesca Ieva and Anna Maria Paganoni</i>	826
5.2.3	Chiara Masci, Francesca Ieva and Anna Maria Paganoni. <i>Laura Bocci and Donatella Vicari</i>	832
5.2.4	Robust Reduced k-Means and Factorial k-Means by trimming. <i>Luca Greco and Antonio Lucadamo and Pietro Amenta</i>	837
5.2.5	Dirichlet processes, posterior similarity and graph clustering. <i>Stefano Tonellato</i> 843	

5.2.6	Bootstrap ClustGeo with spatial constraints. <i>Veronica Distefano, Valentina Mameli, Fabio Della Marra</i>	849
5.3	Advances in Statistical Models	855
5.3.1	Regression modeling via latent predictors. <i>Francesca Martella and Donatella Vicari</i>	855
5.3.2	Analysis of dropout in engineering BSc using logistic mixed-effect models. <i>Luca Fontana and Anna Maria Paganoni</i>	862
5.3.3	dgLARS method for relative risk regression models. <i>Luigi Augugliaro and Angelo M. Mineo</i>	868
5.3.4	A Latent Class Conjoint Analysis for analysing graduates profiles. <i>Paolo Mariani, Andrea Marletta, Lucio Masserini and Mariangela Zenga</i>	874
5.3.5	A longitudinal analysis of the degree of accomplishment of anti-corruption measures by Italian municipalities: a latent Markov approach. <i>Simone Del Sarto, Michela Gnaldi, Francesco Bartolucci</i>	880
5.3.6	Modelling the effect of covariates for unbiased estimates in ecological inference methods. <i>Venera Tomaselli, Antonio Forcina and Michela Gnaldi</i>	886
5.4	Advances in Time Series	892
5.4.1	Filtering outliers in time series of electricity prices. <i>Ilaria Lucrezia Amerise</i> . . .	892
5.4.2	Time-varying long-memory processes. <i>Luisa Bisaglia and Matteo Grigoletto</i>	899
5.4.3	Statistical Analysis of Markov Switching DSGE Models. <i>Maddalena Cavicchioli</i>	905
5.4.4	Forecasting energy price volatilities and comovements with fractionally integrated MGARCH models. <i>Malvina Marchese and Francesca Di Iorio</i>	910
5.4.5	Improved bootstrap simultaneous prediction limits. <i>Paolo Vidoni</i>	916
5.5	Data Management	922
5.5.1	Using web scraping techniques to derive co-authorship data: insights from a case study. <i>Domenico De Stefano, Vittorio Fuccella, Maria Prosperina Vitale, Susanna Zaccarin</i>	922
5.5.2	Dealing with Data Evolution and Data Integration: An approach using Rarefaction. <i>Luca Del Core, Eugenio Montini, Clelia Di Serio, Andrea Calabria</i>	929
5.5.3	Monitoring event attendance using a combination of traditional and advanced surveying tools. <i>Mauro Ferrante, Amit Birenboim, Anna Maria Millito, Stefano De Cantis</i>	935
5.5.4	Indefinite Topological Kernels. <i>Tullia Padellini and Pierpaolo Brutti</i>	941
5.5.5	Data Integration in Social Sciences: the earnings intergenerational mobility problem. <i>Veronica Ballerini, Francesco Bloise, Dario Briscolini and Michele Raitano</i>	947
5.5.6	An innovative approach for the GDPR compliance in Big Data era. <i>M. Giacalone, C. Cusatelli, F. Fanari, V. Santarcangelo, D.C. Sinitó</i>	953
5.6	Developments in Graphical Models	959
5.6.1	An extension of the glasso estimator to multivariate censored data. <i>Antonino Abbruzzo and Luigi Augugliaro and Angelo M. Mineo</i>	959
5.6.2	Bayesian Estimation of Graphical Log-Linear Marginal Models. <i>Claudia Tarantola, Ioannis Ntzoufras and Monia Lupporelli</i>	966
5.6.3	Statistical matching by Bayesian Networks. <i>Daniela Marella and Paola Vicard and Vincenzina Vitale</i>	972
5.6.4	Sparse Nonparametric Dynamic Graphical Models. <i>Fabrizio Poggioni, Mauro Bernardi, Lea Petrella</i>	978
5.6.5	Non-communicable diseases, socio-economic status, lifestyle and well-being in Italy: An additive Bayesian network model. <i>Laura Maniscalco and Domenica Matranga</i>	984
5.6.6	Using Almost-Dynamic Bayesian Networks to Represent Uncertainty in Complex Epidemiological Models: a Proposal. <i>Sabina Marchetti</i>	990

5.7	Educational World	996
5.7.1	How to improve the Quality Assurance System of the Universities: a study based on compositional analysis . <i>Bertaccini B., Gallo M., Simonacci V., and Menini T.</i> .	996
5.7.2	Evaluation of students' performance at lower secondary education. An empirical analysis using TIMSS and PISA data.. <i>G. Graziosi, T. Agasisti, K. De Witte and F. Pauli</i>	1001
5.7.3	Testing for the Presence of Scale Drift: An Example. <i>Michela Battauz</i>	1007
5.7.4	The evaluation of Formative Tutoring at the University of Padova. <i>Renata Clerici, Lorenza Da Re, Anna Giraldo, Silvia Meggiolaro</i>	1012
5.7.5	Benefits of the Erasmus mobility experience: a discrete latent variable analysis. <i>Silvia Bacci, Valeria Caviezel and Anna Maria Falzoni</i>	1017
5.7.6	University choice and the attractiveness of the study area. Insights from an analysis based on generalized mixed-effect models. <i>Silvia Columbu, Mariano Porcu and Isabella Sulis</i>	1023
5.8	Environment	1029
5.8.1	The climate funds for energy sustainability: a counterfactual analysis. <i>Alfonso Carfora and Giuseppe Scandurra</i>	1029
5.8.2	Exploratory GIS Analysis via Spatially Weighted Regression Trees. <i>Carmela Iorio, Giuseppe Pandolfo, Michele Staiano, and Roberta Siciliano</i>	1036
5.8.3	A functional regression control chart for profile monitoring. <i>Fabio Centofanti, Antonio Lepore, Alessandra Menafoglio, Biagio Palumbo and Simone Vantini</i>	1042
5.8.4	Understanding pro-environmental travel behaviours in Western Europe. <i>Gennaro Punzo, Rosalia Castellano, and Demetrio Panarello</i>	1047
5.9	Family & Economic issues	1053
5.9.1	Measuring Economic Uncertainty: Longitudinal Evidence Using a Latent Transition Model. <i>Francesca Giambona, Laura Grassini and Daniele Vignoli</i>	1053
5.9.2	Intentions to leave Italy or to stay among foreigners: some determinants of migration projects. <i>Ginevra Di Giorgio, Francesca Dota, Paola Muccitelli and Daniele Spizzichino</i>	1060
5.9.3	Wages differentials in association with individuals, enterprises and territorial characteristics. <i>S. De Santis, C. Freguja, A. Masi, N. Pannuzi, F. G. Truglia</i>	1066
5.9.4	The Transition to Motherhood among British Young Women: Does housing tenure play a role?. <i>Valentina Tocchioni, Ann Berrington, Daniele Vignoli and Agnese Vitali</i>	1072
5.10	Finance & Insurance	1078
5.10.1	Robust statistical methods for credit risk. <i>A. Corbellini, A. Ghiretti, G. Morelli and A. Talignani</i>	1078
5.10.2	Depth-based portfolio selection. <i>Giuseppe Pandolfo, Carmela Iorio and Antonio D'Ambrosio</i>	1085
5.10.3	Estimating large-scale multivariate local level models with application to stochastic volatility. <i>Matteo Pelagatti and Giacomo Sbrana</i>	1091
5.11	Health and Clinical Data	1097
5.11.1	Is retirement bad for health? A matching approach. <i>Elena Pirani, Marina Ballerini, Alessandra Mattei, Gustavo De Santis</i>	1097
5.11.2	The emergency department utilisation among the immigrant population resident in Rome from 2005 to 2015. <i>Eleonora Trappolini, Laura Cacciani, Claudia Marino, Cristina Giudici, Nera Agabiti, Marina Davoli</i>	1104
5.11.3	Multi-State model with nonparametric discrete frailty. <i>Francesca Gasperoni, Francesca Ieva, Anna Maria Paganoni, Chris Jackson and Linda Sharples</i>	1111
5.11.4	A Functional Urn Model for CARA Designs. <i>Giacomo Aletti, Andrea Ghiglietti, and William F. Rosenberger</i>	1117

5.11.5	Assessment of the INLA approach on gerarchic bayesian models for the spatial disease distribution: a real data application. <i>Paolo Girardi, Emanuela Bovo, Carmen Stocco, Susanna Baracco, Alberto Rosano, Daniele Monetti, Silvia Rizzato, Sara Zamberlan, Enrico Chinellato, Ugo Fedeli, Massimo Rugge</i>	1123
5.12	Medicine	1129
5.12.1	Hidden Markov Models for disease progression. <i>Andrea Martino, Andrea Ghiglietti, Giuseppina Guatteri, Anna Maria Paganoni</i>	1129
5.12.2	A simulation study on the use of response-adaptive randomized designs. <i>Anna Maria Paganoni, Andrea Ghiglietti, Maria Giovanna Scarale, Rosalba Miceli, Francesca Ieva, Luigi Mariani, Cecilia Gavazzi and Valeria Edefonti</i>	1136
5.12.3	The relationship between health care expenditures and time to death: focus on myocardial infarction patients. <i>Luca Grasseti and Laura Rizzi</i>	1142
5.12.4	A multivariate extension of the joint models. <i>Marcella Mazzoleni and Mariangela Zenga</i>	1148
5.12.5	Multipurpose optimal designs for hypothesis testing in normal response trials. <i>Marco Novelli and Maroussa Zagoraiou</i>	1154
5.12.6	Additive Bayesian networks for an epidemiological analysis of swine diseases. <i>Marta Pittavino and Reinhard Furrer</i>	1160
5.13	Population Dynamics	1166
5.13.1	Employment Uncertainty and Fertility: a Meta-Analysis of European Research Findings. <i>Giammarco Alderotti, Daniele Vignoli and Michela Baccini</i>	1166
5.13.2	What Shapes Population Age Structures in the Long Run. <i>Gustavo De Santis and Giambattista Salinari</i>	1172
5.13.3	The impact of economic development on fertility: a complexity approach in a cross-country analysis. <i>NiccolóInnocenti, Daniele Vignoli and Luciana Lazzeretti</i>	1178
5.13.4	A Probabilistic Cohort-Component Model for Population Fore-casting - The Case of Germany. <i>Patrizio Vanella and Philipp Deschermeier</i>	1183
5.13.5	Mortality trends in Sardinia 1992-2015: an ecological study. <i>Vanessa Santos Sanchez, Gabriele Ruiu Marco Breschi, Lucia Pozzi</i>	1187
5.14	Recent Developments in Bayesian Inference	1193
5.14.1	Posterior distributions with non explicit objective priors. <i>Erlis Ruli, Nicola Sartori and Laura Ventura</i>	1193
5.14.2	A predictive measure of the additional loss of a non-optimal action under multiple priors. <i>Fulvio De Santis and Stefania Gubbiotti</i>	1200
5.14.3	Bayesian estimation of number and position of knots in regression splines. <i>Gioia Di Credico, Francesco Pauli and Nicola Torelli</i>	1206
5.14.4	The importance of historical linkages in shaping population density across space. <i>Ilenia Epifani and Rosella Nicolini</i>	1212
5.15	Recent Developments in Sampling	1218
5.15.1	Species richness estimation exploiting purposive lists: A proposal. <i>A. Chiarucci, R.M. Di Biase, L. Fattorini, M. Marcheselli and C. Pisani</i>	1218
5.15.2	Design-based exploitation of big data by a doubly calibrated estimator. <i>Maria Michela Dickson, Giuseppe Espa and Lorenzo Fattorini</i>	1225
5.15.3	Design-based mapping in environmental surveys. <i>L. Fattorini, M. Marcheselli and C. Pisani</i>	1231
5.15.4	Testing for independence in analytic inference. <i>Pier Luigi Conti and Alberto Di Iorio</i>	1237
5.15.5	On the aberrations of two-level Orthogonal Arrays with removed runs. <i>Roberto Fontana and Fabio Rapallo</i>	1243

5.16	Recent Developments in Statistical Modelling	1249
5.16.1	Quantile Regression Coefficients Modeling: a Penalized Approach. <i>Gianluca Sottile, Paolo Frumento and Matteo Bottai</i>	1249
5.16.2	Simultaneous calibrated prediction intervals for time series. <i>Giovanni Fonseca, Federica Giummolé and Paolo Vidoni</i>	1256
5.16.3	Reversibility and (non)linearity in time series. <i>Luisa Bisaglia and Margherita Gerolimetto</i>	1262
5.16.4	Heterogeneous effects of subsidies on farms' performance: a spatial quantile regression analysis. <i>Marusca De Castris and Daniele Di Gennaro</i>	1268
5.16.5	On the estimation of high-dimensional regression models with binary covariates. <i>Valentina Mameli, Debora Slanzi and Irene Poli</i>	1275
5.17	Social Indicators	1281
5.17.1	Can a neighbour region influence poverty? A fuzzy and longitudinal approach. <i>Gianni Betti, Federico Crescenzi and Francesca Gagliardi</i>	1281
5.17.2	Weight-based discrimination in the Italian Labor Market: how do ethnicity and gender interact? <i>Giovanni Busetta, Maria Gabriella Campolo, and Demetrio Panarello</i>	1288
5.17.3	The Total Factor Productivity Index as a Ratio of Price Indexes. <i>Lisa Crosato and Biancamaria Zavanella</i>	1294
5.17.4	Monetary poverty indicators at local level: evaluating the impact of different poverty thresholds. <i>Luigi Biggeri, Caterina Giusti and Stefano Marchetti</i>	1300
5.17.5	A gender inequality assessment by means of the Gini index decomposition. <i>Michele Costa</i>	1306
5.18	Socio-Economic Statistics	1312
5.18.1	The NEETs during the economic crisis in Italy, Young NEETs in Italy, Spain and Greece during the economic crisis. <i>Giovanni De Luca, Paolo Mazzocchi, Claudio Quintano, Antonella Rocca</i>	1312
5.18.2	Camel or dromedary? A study of the equilibrium distribution of income in the EU countries. <i>Crosato L., Ferretti C., Ganugi P.</i>	1319
5.18.3	Small Area Estimation of Inequality Measures. <i>Maria Rosaria Ferrante and Silvia Pacei</i>	1325
5.18.4	Testing the Learning-by-Exporting at Micro-Level in light of influence of "Statistical Issues" and Macroeconomic Factors. <i>Maria Rosaria Ferrante and Marzia Freo</i>	1330
5.18.5	The mobility and the job success of the Sicilian graduates <i>Ornella Giambalvo and Antonella Plaia and Sara Binassi</i>	1336
5.19	Statistical Analysis of Energy Markets	1342
5.19.1	Forecasting Value-at-Risk for Model Risk Analysis in Energy Markets. <i>Angelica Gianfreda and Giacomo Scandolo</i>	1342
5.19.2	Prediction interval of electricity prices by robust nonlinear models. <i>Lisa Crosato, Luigi Grossi and Fany Nan</i>	1349
5.19.3	Bias Reduction in a Matching Estimation of Treatment Effect. <i>Maria Gabriella Campolo, Antonino Di Pino and Edoardo Otranto</i>	1354
5.20	Statistical Inference and Testing Procedures	1360
5.20.1	Comparison of exact and approximate simultaneous confidence regions in nonlinear regression models. <i>Claudia Furlan and Cinzia Mortarino</i>	1360
5.20.2	Tail analysis of a distribution by means of an inequality curve. <i>E. Taufer, F. Santi, G. Espa and M. M. Dickson</i>	1367
5.20.3	Nonparametric penalized likelihood for density estimation. <i>Federico Ferraccioli, Laura M. Sangalli and Livio Finos</i>	1373
5.20.4	Rethinking the Kolmogorov-Smirnov Test of Goodness of Fit in a Compositional Way. <i>G.S. Monti, G. Mateu-Figueras, M. I. Ortego, V. Pawlowsky-Glahn and J. J. Egozcue</i>	1379

5.20.5	Stochastic Dominance for Generalized Parametric Families. <i>Tommaso Lando and Lucio Bertoli-Barsotti</i>	1385
5.21	Statistical Models for Ordinal Data	1390
5.21.1	A comparative study of benchmarking procedures for interrater and intrarater agreement studies. <i>Amalia Vanacore and Maria Sole Pellegrino</i>	1390
5.21.2	Measuring the multiple facets of tolerance using survey data. <i>Caterina Liberati and Riccarda Longaretti and Alessandra Michelangeli</i>	1397
5.21.3	Modified profile likelihood in models for clustered data with missing values. <i>Claudia Di Caterina and Nicola Sartori</i>	1401
5.21.4	Worthiness Based Social Scaling. <i>Giulio D'Epifanio</i>	1407
5.21.5	Direct Individual Differences Scaling for Evaluation of Research Quality. <i>Gallo M., Trendafilov N., and Simonacci V.</i>	1412
5.21.6	A test for variable importance. <i>Rosaria Simone</i>	1416
5.22	Statistical Models New Proposals	1422
5.22.1	Decomposing Large Networks: An Approach Based on the MCA based Community Detection. <i>Carlo Drago</i>	1422
5.22.2	On Bayesian high-dimensional regression with binary predictors: a simulation study. <i>Debora Stanzi, Valentina Mameli and Irene Poli</i>	1429
5.22.3	On the estimation of epidemiological parameters from serological survey data using Bayesian mixture modelling. <i>Emanuele Del Fava, Piero Manfredi, and Ziv Shkedy</i>	1435
5.22.4	An evaluation of KL-optimum designs to discriminate between rival copula models. <i>Laura Deldossi, Silvia Angela Osmetti, Chiara Tommasi</i>	1441
5.22.5	Variational Approximations for Frequentist and Bayesian Inference. <i>Luca Maestrini and Matt P. Wand</i>	1447
5.22.6	Node-specific effects in latent space modelling of multidimensional networks. <i>Silvia D'Angelo and Marco Alfó and Thomas Brendan Murphy</i>	1453
5.23	Statistics for Consumer Research	1459
5.23.1	A panel data analysis of Italian hotels. <i>Antonio Giusti, Laura Grassini, Alessandro Viviani</i>	1459
5.23.2	A Bayesian Mixed Multinomial Logit Model for Partially Microsimulated Data on Labor Supply. <i>Cinzia Carota and Consuelo R. Nava</i>	1466
5.23.3	Comparison between Experience-based Food Insecurity scales. <i>Federica Onori, Sara Viviani and Pierpaolo Brutti</i>	1472
5.23.4	Sovereign co-risk measures in the Euro Area. <i>Giuseppe Arbia, Riccardo Bramante, Silvia Facchinetti, Diego Zappa</i>	1478
5.23.5	Simultaneous unsupervised and supervised classification modeling for clustering, model selection and dimensionality reduction. <i>Mario Fordellone and Maurizio Vichi</i>	1484
5.23.6	Consumers' preference for coffee consumption: a choice experiment including organoleptic characteristics and chemical analysis <i>Rossella Berni, Nedka D. Niki-forova and Patrizia Pinelli</i>	1491
5.24	Statistics for Earthquakes	1498
5.24.1	How robust is the skill score of probabilistic earthquake forecasts? <i>Alessia Caponera and Maximilian J. Werner</i>	1498
5.24.2	Functional linear models for the analysis of similarity of waveforms. <i>Francesca Di Salvo, Renata Rotondi and Giovanni Lanzano</i>	1505
5.24.3	Detection of damage in civil engineering structure by PCA on environmental vibration data. <i>G. Agró, V. Carlisi, R. Mantione</i>	1511

5.25	Statistics for Financial Risks	1517
5.25.1	Conditional Value-at-Risk: a comparison between quantile regression and copula functions. <i>Giovanni De Luca and Giorgia Riviaccio</i>	1517
5.25.2	Systemic events and diffusion of jumps. <i>Giovanni Bonaccolto, Nancy Zambon and Massimiliano Caporin</i>	1523
5.25.3	Traffic Lights for Systemic Risk Detectio. <i>Massimiliano Caporin, Laura Garcia-Jorcano, Juan-Angel Jiménez-Martin</i>	1529
5.25.4	Bayesian Quantile Regression Treed. <i>Mauro Bernardi and Paola Stolfi</i>	1536
5.25.5	Model Selection in Weighted Stochastic Block models. <i>Roberto Casarin, Michele Costola, Erdem Yenerdag</i>	1541
5.26	Tourism & Cultural Participation	1545
5.26.1	The determinants of tourism destination competitiveness in 2006-2016: a partial least square path modelling approach. <i>Alessandro Magrini, Laura Grassini</i>	1545
5.26.2	Participation in tourism of Italian residents in the years of the economic recession. <i>Chiara Bocci, Laura Grassini, Emilia Rocco</i>	1552
5.26.3	Cultural Participation in the digital Age in Europe: a multilevel cross-national analysis. <i>Laura Bocci and Isabella Mingo</i>	1558
5.26.4	Tourist flows and museum admissions in Italy: an integrated analysis. <i>Lorenzo Cavallo, Francesca Petrei, Maria Teresa Santoro</i>	1565
5.26.5	Posterior Predictive Assessment for Item Response Theory Models: A Proposal Based on the Hellinger Distance. <i>Mariagiulia Matteucci and Stefania Mignani</i>	1571
5.27	Well-being & Quality of Life	1577
5.27.1	Is Structural Equation Modelling Able to Predict Well-being? <i>Daniele Toninelli and Michela Cameletti</i>	1577
5.27.2	The well-being in the Italian urban areas: a local geographic variation analysis. <i>Eugenia Nissi and Annalina Sarra</i>	1584
5.27.3	Comparing Composite Indicators to measure Quality of Life: the Italian "Sole 24 Ore" case. <i>Gianna Agró, Marianonietta Ruggieri and Erasmo Vassallo</i>	1590
5.27.4	Quality of working life in Italy: findings from Inapp survey. <i>Paolo Emilio Cardone</i>	1596
5.27.5	Well-being indices: what about Italian scenario? <i>Silvia Facchinetti and Elena Siletti</i>	1603
5.27.6	How can we compare rankings that are expected to be similar? An example based on composite well being indicators. <i>Silvia Terzi e Luca Moroni</i>	1609
6	Poster Sessions	1617
6.0.1	A distribution curves comparison approach to analyze the university moving students performance. <i>Giovanni Boscaino, Giada Adelfio, Gianluca Sottile</i>	1617
6.0.2	A Partial Ordering Application in Aggregating Dimensions of Subjective Well-being. <i>Paola Conigliaro</i>	1624
6.0.3	A note on objective Bayes analysis for graphical vector autoregressive models. <i>Lucia Paci and Guido Consonni</i>	1630
6.0.4	Bayesian Population Size Estimation with A Single Sample. <i>Pierfrancesco Alaimo Di Loro and Luca Tardella</i>	1636
6.0.5	Classification of the Aneurisk65 dataset using PCA for partially observed functional data. <i>Marco Stefanucci, Laura Sangalli and Pierpaolo Brutti</i>	1642
6.0.6	Deep Learning to the Test: an Application to Traffic Data Streams. <i>Nina Deliu and Pierpaolo Brutti</i>	1647
6.0.7	Estimating the number of unseen species under heavy tails. <i>Marco Battiston, Federico Camerlenghi, Emanuele Dolera and Stefano Favaro</i>	1653
6.0.8	How to measure cybersecurity risk. <i>Silvia Facchinetti, Paolo Giudici and Silvia Angela Osmetti</i>	1659

6.0.9	Implementation of an innovative technique to improve Sauvignon Blanc wine quality. <i>Filippa Bono, Pietro Catanaia and Mariangela Vallone</i>	1663
6.0.10	Investigating the effect of drugs consumption on survival outcome of Heart Failure patients using joint models: a case study based on regional administrative data. <i>Marta Spreafico, Francesca Gasperoni, Francesca Ieva</i>	1669
6.0.11	Mapping the relation between University access test and student's university performance. <i>Vincenzo Giuseppe Genova, Antonella Plaia</i>	1675
6.0.12	Multivariate analysis of marine litter abundance through Bayesian space-time models. <i>C. Calculli, A. Pollice, L. Sion, and P. Maiorano</i>	1681
6.0.13	Power Priors for Bayesian Analysis of Graphical Models of Conditional Independence in Three Way Contingency Tables. <i>Katerina Mantzouni, Claudia Tarantola and Ioannis Ntzoufras</i>	1685
6.0.14	Random Garden: a Supervised Learning Algorithm. <i>Ivan Luciano Danesi, Valeria Danese, Nicolo' Russo and Enrico Tonini</i>	1691
6.0.15	Spatiotemporal Prevision for Emergency Medical System Events in Milan. <i>Andrea Gilardi, Riccardo Borgoni, Andrea Pagliosa, Rodolfo Bonora</i>	1697
6.0.16	Spatial segregation immigrant households in Messina. <i>Angelo Mazza and Massimo Mucciardi</i>	1703
6.0.17	Supervised Learning for Link Prediction in Social Networks. <i>Riccardo Giubilei, Pierpaolo Brutti</i>	1707
6.0.18	Women's empowerment and child mortality: the case of Bangladesh. <i>Chiara Puglisi, Annalisa Busetta</i>	1713

Constrained Extended Plackett-Luce model for the analysis of preference rankings

Cristina Mollica and Luca Tardella

Abstract Choice behavior and preferences typically involve numerous and subjective aspects that are difficult to be identified and quantified. For this reason, their exploration is frequently conducted through the collection of ordinal evidence in the form of ranking data. Multistage ranking models, including the popular Plackett-Luce distribution (PL), rely on the assumption that the ranking process is performed sequentially, by assigning the positions from the top to the bottom one (*forward order*). A recent contribution to the ranking literature relaxed this assumption with the addition of the discrete *reference order* parameter, yielding the novel *Extended Plackett-Luce model* (EPL). In this work, we introduce the EPL with order constraints on the reference order parameter and a novel diagnostic tool to assess the adequacy of the EPL parametric specification. The usefulness of the proposal is illustrated with an application to a real dataset.

Key words: Ranking data, Plackett-Luce model, Bayesian inference, Data augmentation, Gibbs sampling, Metropolis-Hastings, model diagnostics

1 Introduction

A *ranking* $\pi = (\pi(1), \dots, \pi(K))$ of K items is a sequence where the entry $\pi(i)$ indicates the rank attributed to the i -th alternative. Data can be equivalently collected in the ordering format $\pi^{-1} = (\pi^{-1}(1), \dots, \pi^{-1}(K))$, such that the generic component $\pi^{-1}(j)$ denotes the item ranked in the j -th position. Regardless of the adopted

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format, ranked observations are multivariate and, specifically, correspond to permutations of the first K integers.

The statistical literature concerning ranked data modeling and analysis is reviewed in [3] and, more recently, in [1]. Several parametric distributions on the set of permutations \mathcal{S}_K have been developed and applied to real experiments. A popular parametric family is the *Plackett-Luce* model (PL), belonging to the class of the so-called *stagewise ranking models*. The basic idea is the decomposition of the ranking process into $K - 1$ stages, concerning the attribution of each position according to the *forward order*, that is, the ordering of the alternatives proceeds sequentially from the most-liked to the least-liked item. The implicit forward order assumption has been relaxed by [4] in the *Extended Plackett-Luce model* (EPL). The PL extension relies on the introduction of the *reference order* parameter indicating the rank assignment order. In this work, we investigate a restricted version of the EPL with order constraints for the reference order parameter representing a meaningful rank attribution process and we also introduce a novel diagnostic to assess the adequacy of the EPL assumption as the actual sampling distribution of the observed rankings.

2 The Extended Plackett-Luce model with order constraints

2.1 Model specification

The implicit assumption in the PL scheme is the forward ranking order, meaning that at the first stage the ranker reveals the item in the first position (most-liked alternative), at the second stage she assigns the second position and so on up to the last rank (least-liked alternative). [4] suggested the extension of the PL by relaxing the canonical forward order assumption, in order to explore alternative meaningful ranking orders for the choice process and to increase the flexibility of the PL parametric family. Their proposal was realized by representing the ranking order with an additional model parameter $\rho = (\rho(1), \dots, \rho(K))$, called reference order, where the entry $\rho(t)$ indicates the rank attributed at the t -th stage of the ranking process. Thus, ρ is a discrete parameter given by a permutation of the first K integers and the composition $\eta^{-1} = \pi^{-1}\rho$ of an ordering with a reference order yields the sequence $\eta^{-1} = (\eta^{-1}(1), \dots, \eta^{-1}(K))$ which lists the items in order of selection, such that the component $\eta^{-1}(t) = \pi^{-1}(\rho(t))$ corresponds to the item chosen at stage t and receiving rank $\rho(t)$. The probability of a generic ordering under EPL can be written as

$$\mathbf{P}_{\text{EPL}}(\pi^{-1} | \rho, \underline{p}) = \mathbf{P}_{\text{PL}}(\pi^{-1} \rho | \underline{p}) = \prod_{t=1}^K \frac{p_{\pi^{-1}(\rho(t))}}{\sum_{v=t}^K p_{\pi^{-1}(\rho(v))}} \quad \pi^{-1} \in \mathcal{S}_K, \quad (1)$$

Hereinafter, we will shortly refer to (1) as $\text{EPL}(\rho, \underline{p})$. The quantities p_i 's are the support parameters and are proportional to the probabilities for each item to be ranked in the position indicated by the first entry of ρ .

Differently from [4], we focus on a restriction $\tilde{\mathcal{S}}_K$ of the whole permutation space S_K for the reference order parameter. Our choice can be explained by the fact that, in a preference elicitation process, not all the possible $K!$ orders seem to be equally natural, hence plausible. Often the ranker has a clearer perception about her extreme preferences (most-liked and least-liked items), rather than middle positions. In this perspective, the rank attribution process can be regarded as the result of a sequential “top-or-bottom” selection of the positions. At each stage, the ranker specifies either her best or worst choice among the available positions at that given step. With this scheme, the reference order can be equivalently represented as a binary sequence $\underline{W} = (W_1, \dots, W_K)$ where the generic W_t component indicates whether the ranker makes a top or bottom decision at the t -th stage, with the convention that $W_K = 1$. One can then formalize the mapping from the restricted permutation ρ to \underline{W} with the help of a vector of non negative integers $\underline{F} = (F_1, \dots, F_K)$, where F_t represents the number of top positions assigned before stage t . In fact, by starting from positing by construction $F_1 = 0$, one can derive sequentially

$$W_t = I_{[\rho(t)=\rho_F(F_t+1)]} = \begin{cases} 1 & \text{at stage } t \text{ the top preference is specified,} \\ 0 & \text{at stage } t \text{ the bottom preference is specified,} \end{cases}$$

where $I_{[E]}$ is the indicator function of the event E and $F_t = \sum_{v=1}^{t-1} W_v$ for $t = 2, \dots, K$. Note that, since the forward and backward orders (ρ_F, ρ_B) can be regarded as the two extreme benchmarks in the sequential construction of ρ , this allows us to understand that $\rho_F(F_t + 1)$ corresponds to the top position available at stage t . Conversely, $B_t = (t - 1) - F_t$ is the number of bottom positions assigned before stage t and thus, symmetrically, one can understand that $\rho_B(B_t + 1)$ indicates the bottom position available at stage t .

The binary representation of the reference order suggests that, under the constraints of the “top-or-bottom” scheme, the size of $\tilde{\mathcal{S}}_K$ is equal to 2^{K-1} . The reduction of the reference order space into a finite set with an exponential size, rather than with a factorial cardinality, is convenient for at least two reasons: i) it leads to a more intuitive interpretation of the support parameters, since they become proportional to the probability for each item to be ranked either in the first or in the last position and ii) it facilitates the construction of a Metropolis-Hastings (MH) step to sample the reference order parameter.

2.2 Bayesian estimation of the EPL via MCMC

Inference on the EPL and its generalization into a finite mixture framework was originally addressed from the frequentist perspective in [4]. Here we consider the original MCMC methods recently developed by [6] to solve Bayesian inference for the constrained EPL.

In the Bayesian domain, the data augmentation with the latent quantitative variables $\underline{y} = (y_{st})$ for $s = 1, \dots, N$ and $t = 1, \dots, K$ crucially contributes to make it

tractable analytically the inference for the EPL. The auxiliary variables y_{st} 's are assumed to be conditionally independent on each other and exponentially distributed with rate parameter equal to the normalization term of the EPL, see also [5]. For the prior specification, independence of \underline{p} and ρ is assumed together with independent Gamma densities for the support parameters, motivated by the conjugacy with the model, and a discrete uniform distribution on $\tilde{\mathcal{S}}_K$ for the reference order. [6] presented a tuned joint Metropolis-within-Gibbs sampling (TJM-within-GS) to perform approximate posterior inference, where the simulation of the reference order is accomplished with a MH algorithm relying on a joint proposal distribution on ρ and \underline{p} , whereas the posterior drawings of the latent variables y 's and the support parameters are performed from the related full-conditional distributions. At the generic iteration $l + 1$, the TJM-within-GS iteratively alternates the following simulation steps

$$\begin{aligned} \rho^{(l+1)}, \underline{p}' &\sim \text{TJM}, \\ y_{st}^{(l+1)} | \pi_s^{-1}, \rho^{(l+1)}, \underline{p}' &\sim \text{Exp} \left(\sum_{i=1}^K \delta_{sti}^{(l+1)} p'_i \right), \\ p_i^{(l+1)} | \underline{\pi}^{-1}, \underline{y}^{(l+1)}, \rho^{(l+1)} &\sim \text{Ga} \left(c + N, d + \sum_{s=1}^N \sum_{t=1}^K \delta_{sti}^{(l+1)} y_{st}^{(l+1)} \right). \end{aligned}$$

3 EPL diagnostic

Simulation studies confirmed the efficacy of the TJM-within-GS to recover the actual generating EPL, together with the benefits of the SM strategy to speed up the MCMC algorithm in the exploration of the posterior distribution. However, we were surprised to verify a less satisfactory performance of the TJM-within-GS in terms of posterior exploration in the application to some real-world examples, such as the famous `song` dataset analyzed by [2]. Since the joint proposal distribution relies on summary statistics, the posterior sampling procedure is expected to work well as long as the data are actually taken from an EPL distribution. So, the unexpectedly bad behavior of the MCMC suggested to conjecture that, for such real data, the EPL does not represent the true (or in any case an appropriate) data generating mechanism. This has motivated us to develop some new tools to appropriately check the model mis-specification issue.

Suppose we have some data simulated from an EPL model. We expect the marginal frequencies of the items at the first stage to be ranked according to the order of the corresponding support parameter component. On the other hand, although computationally demanding to be evaluated in terms of their closed form formula we expect the marginal frequencies of the items at the last stage to be ranked according to the reverse order of the corresponding support parameter component. After proving such a statement one can then derive that the ranking of the marginal frequencies of the items corresponding to the first and last stage should sum up to

$(K + 1)$, no matter what their support is. Of course, this is less likely to happen when the sample size is small or when the support parameters are not so different of each other. In any case, one can define a test statistic by considering, for each couple of integers (j, j') candidate to represent the first and the last stage ranks, namely $\rho(1)$ and $\rho(K)$, a discrepancy measure $T_{jj'}(\boldsymbol{\pi})$ between $K + 1$ and the sum of the rankings of the frequencies corresponding to the same item extracted in the first and in the last stage. Formally, let $\underline{r}_j^{[1]} = (r_{j1}^{[1]}, \dots, r_{jK}^{[1]})$ and $\underline{r}_{j'}^{[K]} = (r_{j'1}^{[K]}, \dots, r_{j'K}^{[K]})$ be the marginal item frequency distributions for the j -th and j' -th positions, to be assigned respectively at the first [1] and last [K] stage. In other words, the generic entry $r_{ji}^{[s]}$ is the number of times that item i is ranked j -th at the s -th stage. The proposed EPL diagnostic relies on the following discrepancy

$$T_{jj'}(\boldsymbol{\pi}) = \sum_{i=1}^K |(\text{rank}(\underline{r}_j^{[1]})_i + \text{rank}(\underline{r}_{j'}^{[K]})_i - (K + 1))|,$$

implying that the smaller the test statistics, the larger the plausibility that the two integers (j, j') represent the first and the last components of the reference order. To globally assess the conformity of the sample with the EPL, we consider the minimum value of $T_{jj'}(\boldsymbol{\pi})$ over all the possible rank pairs satisfying the order constraints

$$T(\boldsymbol{\pi}) = \min_{(j, j') \in \mathcal{D}} T_{jj'}(\boldsymbol{\pi}), \quad (2)$$

where $\mathcal{D} = \{(j, j') : j \in \{1, K\} \text{ and } j \neq j'\}$.

3.1 Applications to real data

We fit the EPL with reference order constraints to the `SPORT` dataset of the `Rankcluster` package, where $N=130$ students at the University of Illinois were asked to rank $K=7$ sports in order of preference: 1=Baseball, 2=Football, 3=Basketball, 4=Tennis, 5=Cycling, 6=Swimming and 7=Jogging. We estimated the Bayesian EPL with hyperparameter setting $c = d = 1$, by running the TJM-within-GS for 20000 iterations and discarding the first 2000 samplings as burn-in phase. We show the approximation of the posterior distribution on the reference order in Figure 1, where it is apparent that the MCMC is mixing sufficiently fast and there is some uncertainty on the underlying reference order. The modal reference order is (7,1,2,3,4,6,5), with slightly more than 0.4 posterior probability. However, when we compared the plausibility of the observed diagnostic statistic with the reference distribution under the fitted EPL, we got a warning with a bootstrap classical p -value approximately equal to 0.011. This should indeed cast some doubt on the use of PL or EPL as a suitable model for the entire dataset. In fact, we have verified that, after suitably splitting the dataset into two groups according to the EPL mixture methodology suggested by [4] (best fitting 2-component EPL mixture

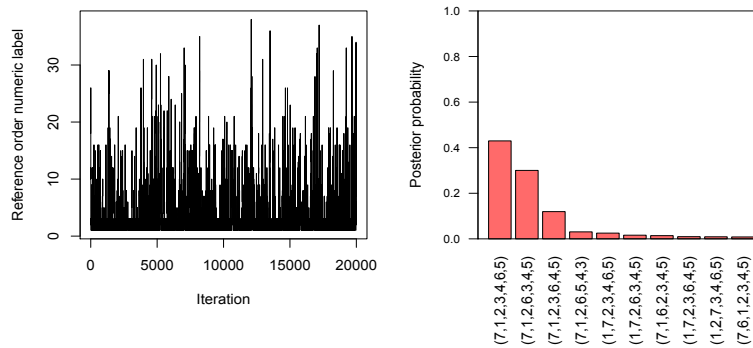


Fig. 1: Traceplot (left) and top-10 posterior probabilities (right) for the reference order parameter.

with $BIC=2131.20$), we have a different more comfortable perspective for using the EPL distribution to separately model the two clusters. The modal reference orders are $(1,2,3,4,5,6,7)$ and $(1,2,3,7,4,5,6)$ and the estimated Borda orderings are $(7,6,4,5,3,1,2)$ and $(1,2,3,4,6,7,5)$, indicating opposite preferences in the two subsamples towards team and individual sports. In this case, no warning by the diagnostic tests applied separately to the two subsamples is obtained, since the resulting p -values are 0.991 and 0.677.

4 Conclusions

We have addressed some relevant issues in modelling choice behavior and preferences. In particular, we have further explored the idea in [4] related to the use of the reference order specifying the order of the ranks sequentially assigned by introducing monotonicity restrictions on the discrete parameter to describe a “top-or-bottom” attribution of the positions. Our contribution allows to gain more insights on the sequential mechanism of formation of preferences, whether or not it is appropriate at all and whether it privileges a more or less natural ordered assignment of the most extreme ranks. Additionally, some issues experienced when implementing a well-mixing MCMC approximation motivated us to derive a diagnostic tool to test the appropriateness of the EPL distribution, whose effectiveness has been checked with an application to a real example.

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