

# A comparative analysis of implicit models for real-time short-term traffic predictions



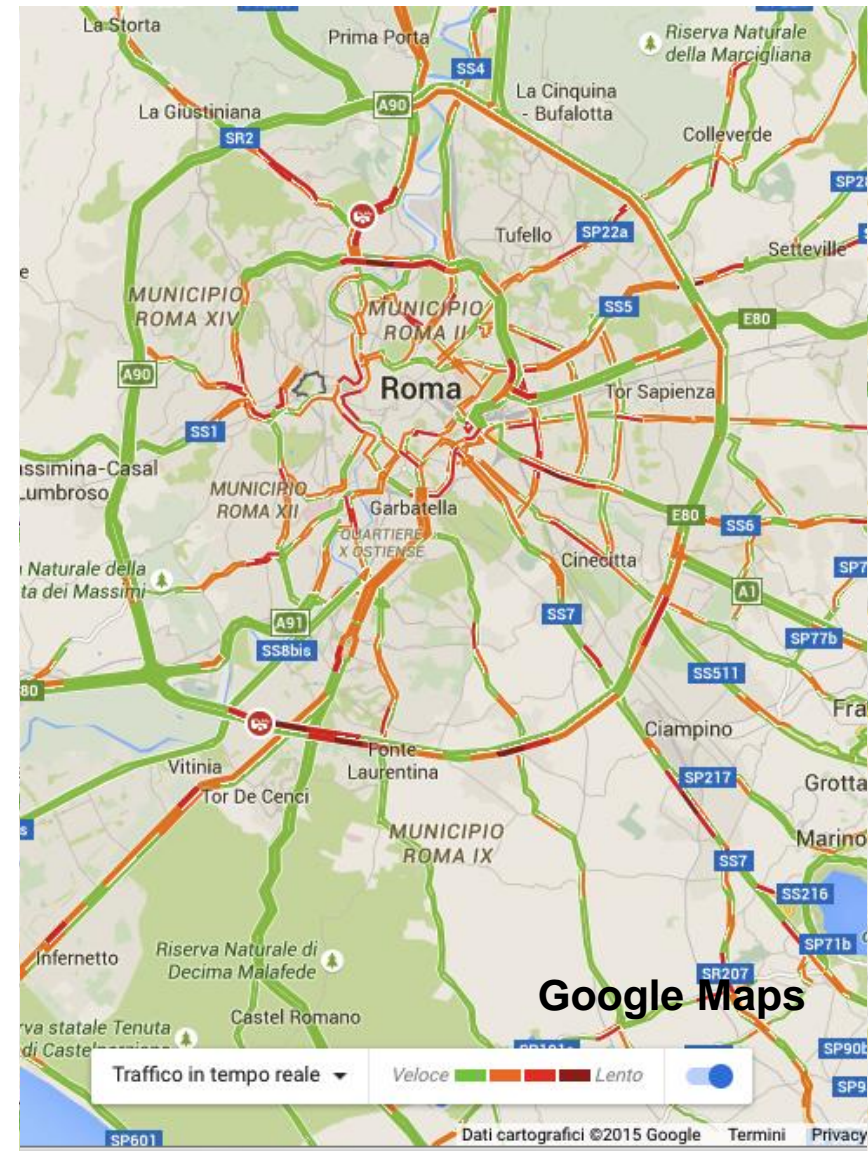
SAPIENZA  
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# Introduction

- Traffic maps are becoming familiar to most travelers.
- Tracking connected personal devices allows major web providers (Google, Apple) and specialized companies (TomTom, Inrix) supplying real-time traffic information.



# Introduction

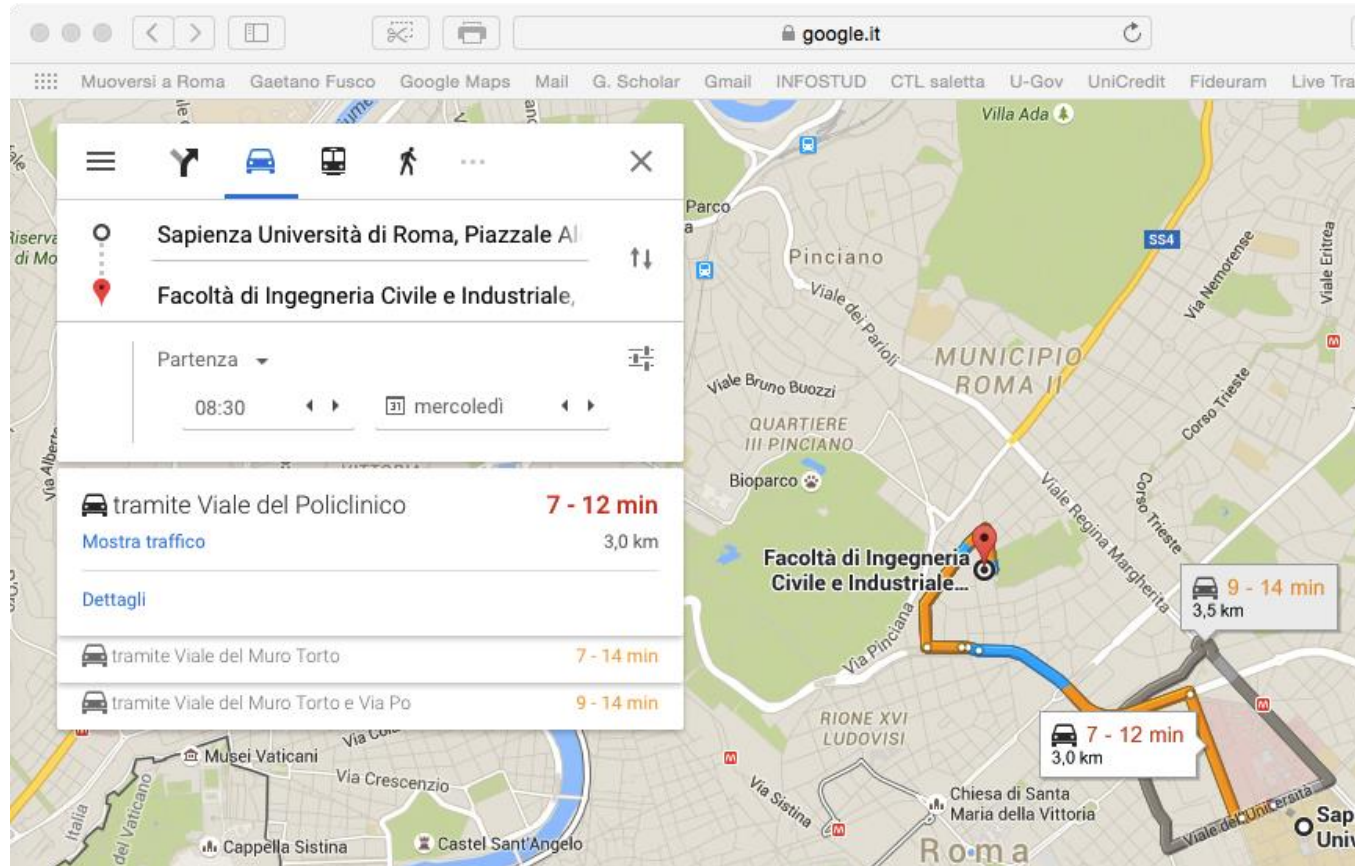
- On-board and web traffic information services display both real-time and usual traffic conditions.
- They also supply users with route suggestions based on the desired departure time.
- However, methods for predicting future travel times are not known.





# Introduction

- Precision of prediction methods is not yet fully satisfactory.



# Introduction

- Since '70s, academics developed many prediction methods to allow Intelligent Transportation Systems proactive features.
- Explicit models simulate demand-supply interactions: they can estimate unobserved conditions and prevent overreaction.
- Implicit models extrapolate short-term predictions from observed trend (data-driven): they are often applied to short-term predictions on freeways, because of their simple physical structure.

# Introduction

- However, these models are not used in commercial applications.
- TomTom doesn't supply dynamic traffic predictions.

**TOMTOM**

Home Products Maps Services Live Traffic

Route Planner Link Legend

Plan a route Find a location

From: Piazzale Aldo Moro 5, Rome, IT  
e.g., '1 Bridge St, London'

To: Facoltà di Ingegneria, Rome, IT

Traffic:  Minimise delays

Leave **Minimise traffic delays**

If you choose to leave now (or within 30 minutes), current traffic conditions are taken into account when planning your route.

Leave Now Close

Leave Monday from **5 Piazzale Aldo Moro, Roma** 08:30 am  
3.2 km - 11 min.

Arrive Monday at **Via Eudossiana, Roma** 08:41 am

## Minimise traffic delays

If you choose to leave now (or within 30 minutes), current traffic conditions are taken into account when planning your route.

Leave Now

Close

# Object of the study

- We want to assess implicit models in short-term traffic predictions on urban networks.
- Advantages of implicit models:
  - Standard automatable calibration methods
  - Fast computation for real-time applications
  - Easy parallelization for dealing with large graphs
  - Independence from specific conditions for **easy generalization**
- Drawbacks of implicit models:
  - Lack of correspondence with the physics of vehicle traffic
- Specific goal:
  - **Relate model structure to network topology**

# State of the art of implicit models

- Time-series models (AR, ARMA, ARIMA, SARIMA)
- Artificial Neural Networks (ANN): Feed-Forward, Kohonen Maps, Fuzzy NN, NAR, NARX)
- Bayesian networks
- Non-parametric estimates (clustering, nearest neighbor, fuzzy classifiers)
- Combination of different methods (Bayesian committee, Bayesian combination, ARIMA-NN)



# Definitions

- Short-term implicit prediction model

$$\hat{v}_{t+1}^a = f\left(v_t^a, v_{t-s}^a, v_{t-2s}^a, \dots, v_{t-hs}^a\right) \quad \begin{array}{l} - a: \text{prediction link}; \quad t: \text{current time} \\ - h: \text{rolling horizon}; \quad s: \text{rolling step} \end{array}$$

- Multi-input model (data from different links)

$$\hat{v}_{t+1}^a = f\left(\mathbf{v}_t, \mathbf{v}_{t-s}, \mathbf{v}_{t-2s}, \dots, \mathbf{v}_{t-hs}\right); \quad \mathbf{v}_t = \{v_t^a, v_t^b, \dots, v_t^m\}; \quad a, b, \dots, m \hat{=} L$$

- Multi-input with exogenous variables

$$\hat{v}_{t+1}^a = f\left(\mathbf{v}_t, \mathbf{v}_{t-s}, \mathbf{v}_{t-2s}, \dots, \mathbf{v}_{t-hs}; \mathbf{X}_t, \mathbf{X}_{t-s}, \mathbf{X}_{t-2s}, \dots, \mathbf{X}_{t-h's}\right)$$

$$\mathbf{X}_t = \left\{x_t^a, x_t^b, \dots, x_t^m; y_t^a, y_t^b, \dots, y_t^m; \dots; z_t^a, z_t^b, \dots, z_t^m\right\}$$

- Multi-step prediction

$$\left\{\hat{v}_{t+1}^a, \hat{v}_{t+2}^a, \dots, \hat{v}_{t+p}^a\right\} = f\left(\mathbf{v}_t, \mathbf{v}_{t-s}, \mathbf{v}_{t-2s}, \dots, \mathbf{v}_{t-hs}; \mathbf{X}_t, \mathbf{X}_{t-s}, \mathbf{X}_{t-2s}, \dots, \mathbf{X}_{t-h's}\right)$$

# Feed-Forward Neural Network

- Well known A.I. paradigm inspired by natural brain biology

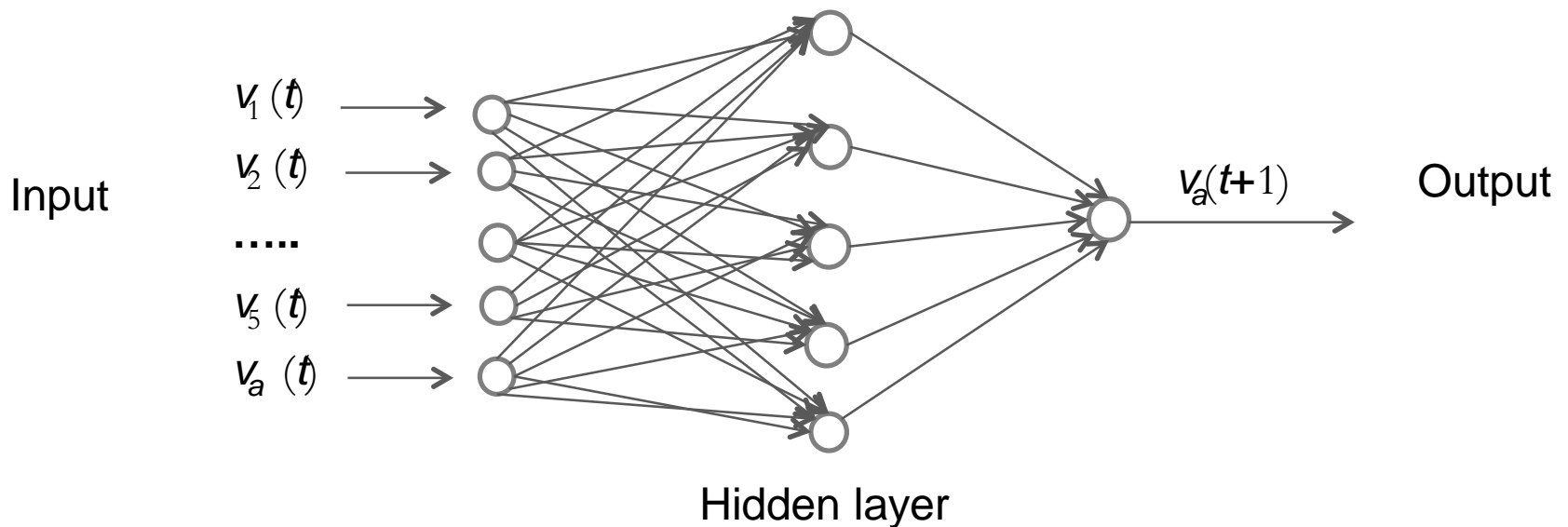
$$\hat{V}_a(t+1) = f(\mathbf{Cz} + J_C)$$

–  $f$ : nonlinear function

□  $\mathcal{G}_C, \mathcal{G}_D$ : thresholds

$$\mathbf{z} = f(\mathbf{Bv}(t, t-1, \dots, t-h) + J_D)$$

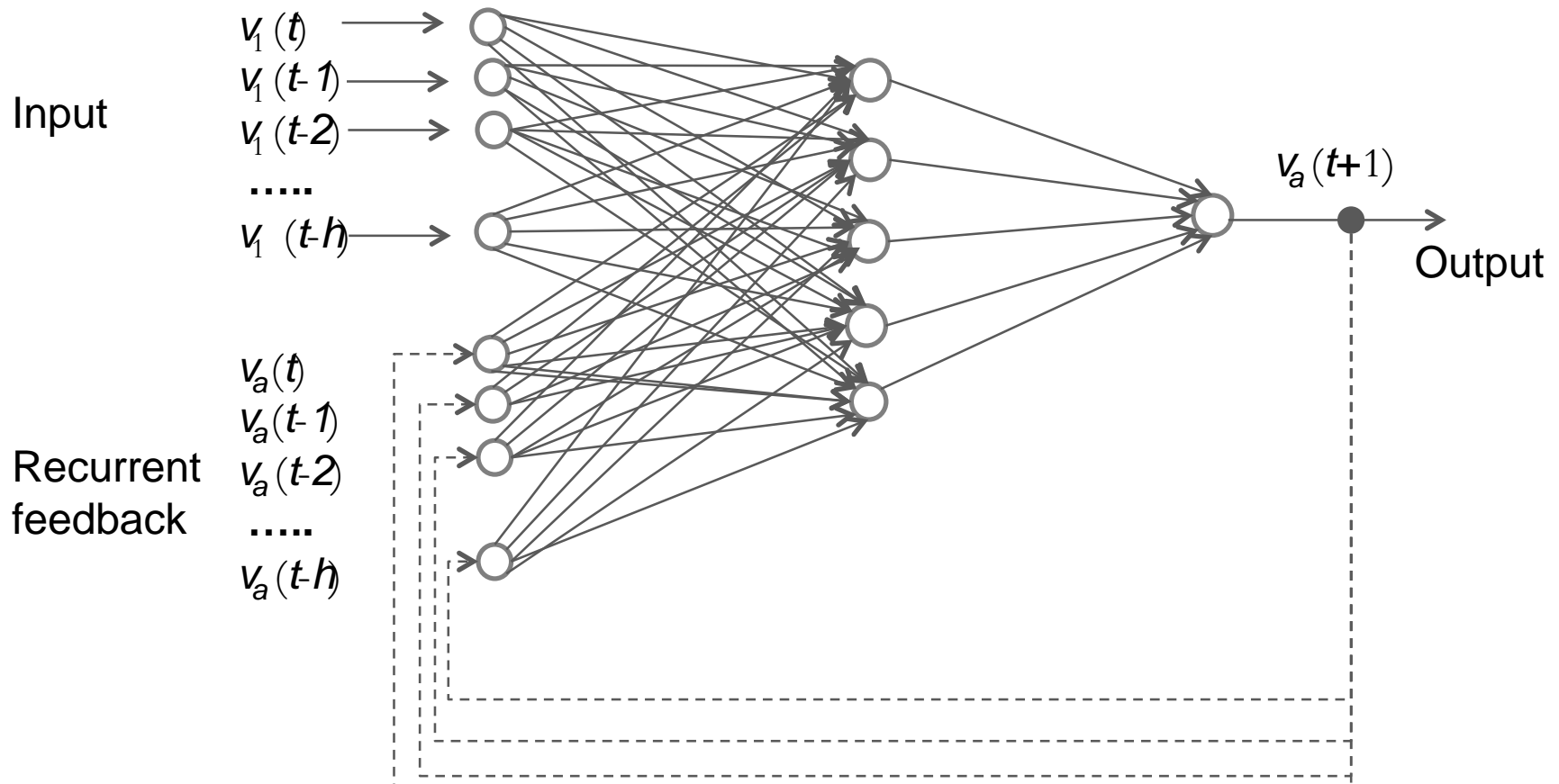
–  $\mathbf{B}, \mathbf{C}$ : weight matrices



# Time dependent Neural Network

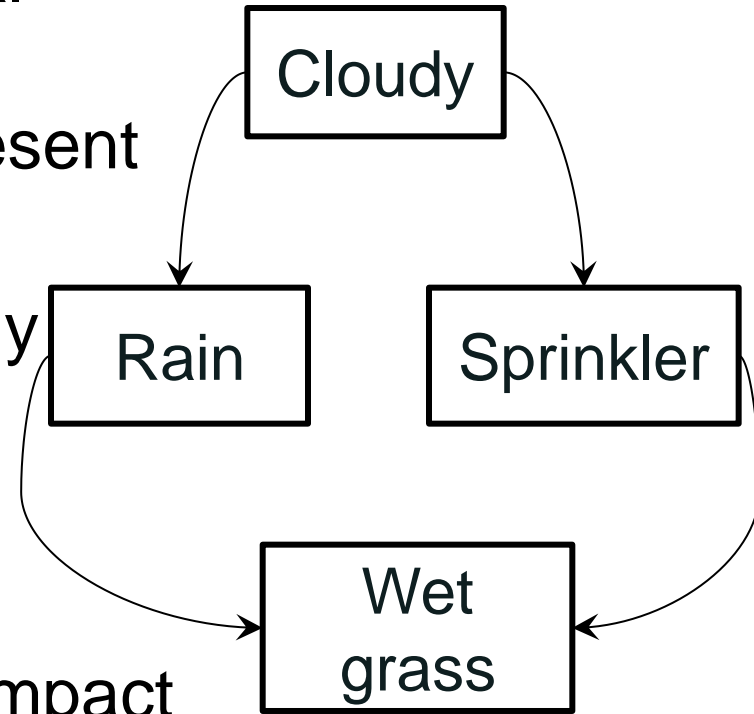
$$\hat{v}_a(t+1) = f(\hat{v}_a(t), \hat{v}_a(t-1), \dots, \hat{v}_a(t-h); \mathbf{v}(t), \mathbf{v}(t-1), \dots, \mathbf{v}(t-h))$$

Non AutoRegressive eXogenous model (NARX)



# Bayesian Networks (BN)

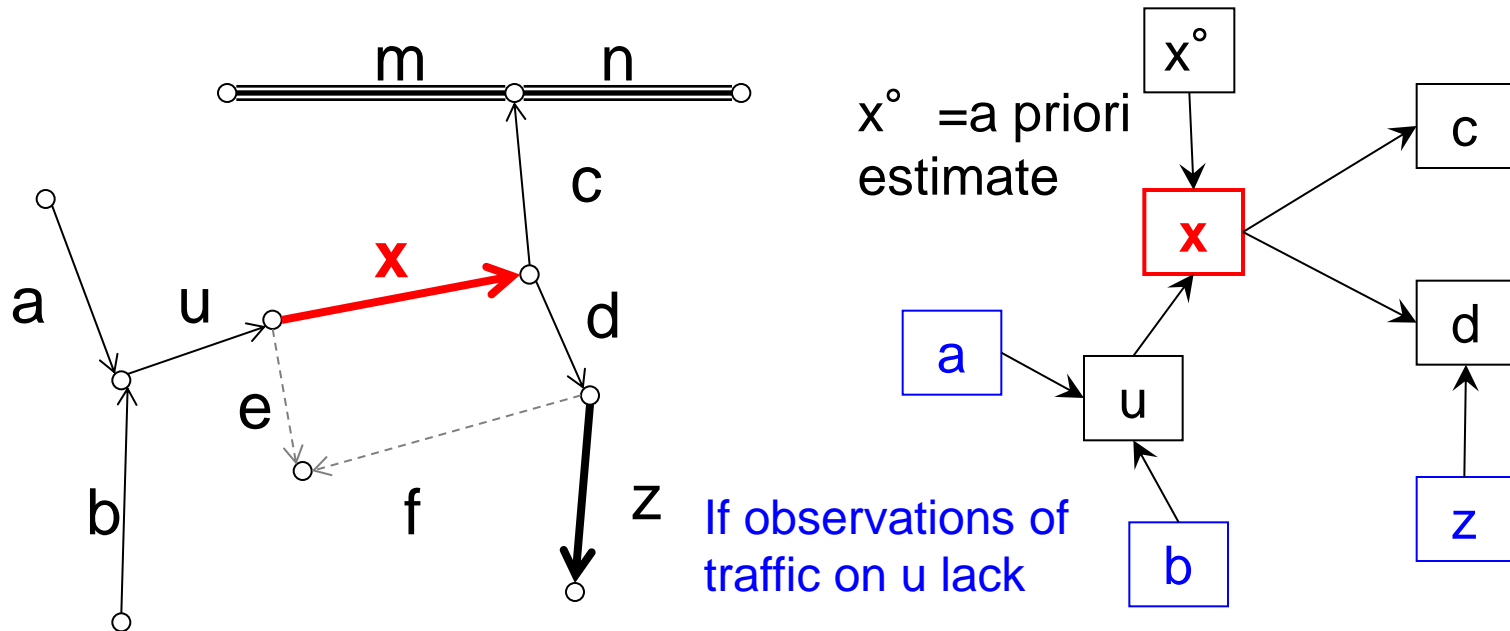
- Bayesian Networks are graphical models whose nodes represent random variables and arcs represent conditional assumptions.
- Unlinked nodes are stochastically independent variables.
- Link direction indicate cause-effect relationship.
- Network structure provides a compact representation of joint probability:



$$P(C, S, R, W) = P(C) \cdot P(S|C) \cdot P(R|C) \cdot P(W|S, R)$$

# Application of BN to traffic prediction

- Nodes of the Bayesian Network are traffic variables
  - Bayesian Network architecture should reproduce traffic interaction on the road network
  - Cause-effect mechanisms are hidden and stochastic independence prevails
- “z” affects “x” because it is parent of its children





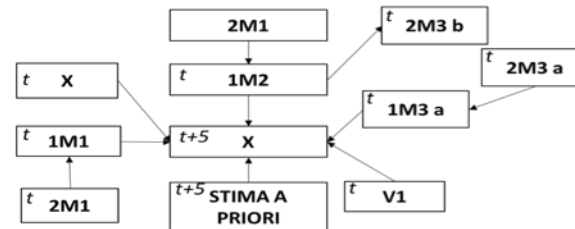
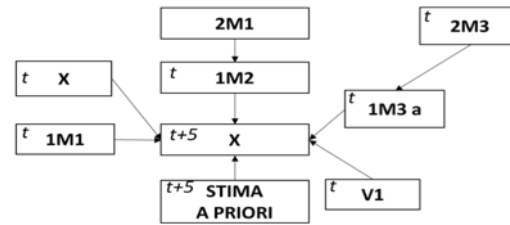
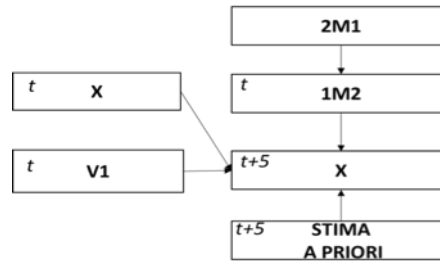
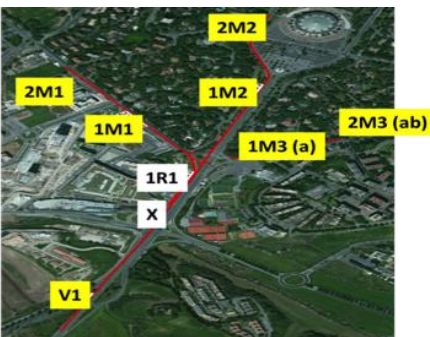
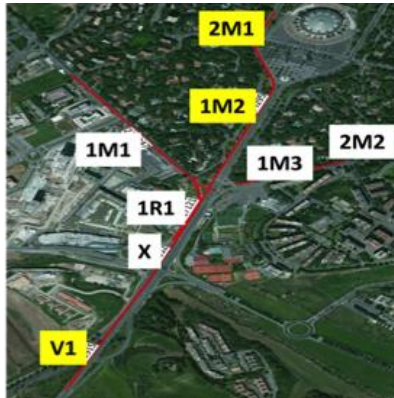
# Experimental application

- TomTom HD data (speed):
  - 6 sub-areas in the town of Rome
  - 3 months of observations (March 2014 – May 2014)
  - 5-min. intervals speed aggregation
  - qData reliability expressed by “confidence factor”
- Forecasts for 5-15-30-45-60 minutes:
  - ANN NARX
  - ANN Feed Forward
  - Bayesian Network
  - Naïve method
  - Historical Average
- Research project with DUEL SpA (funded by FILAS)





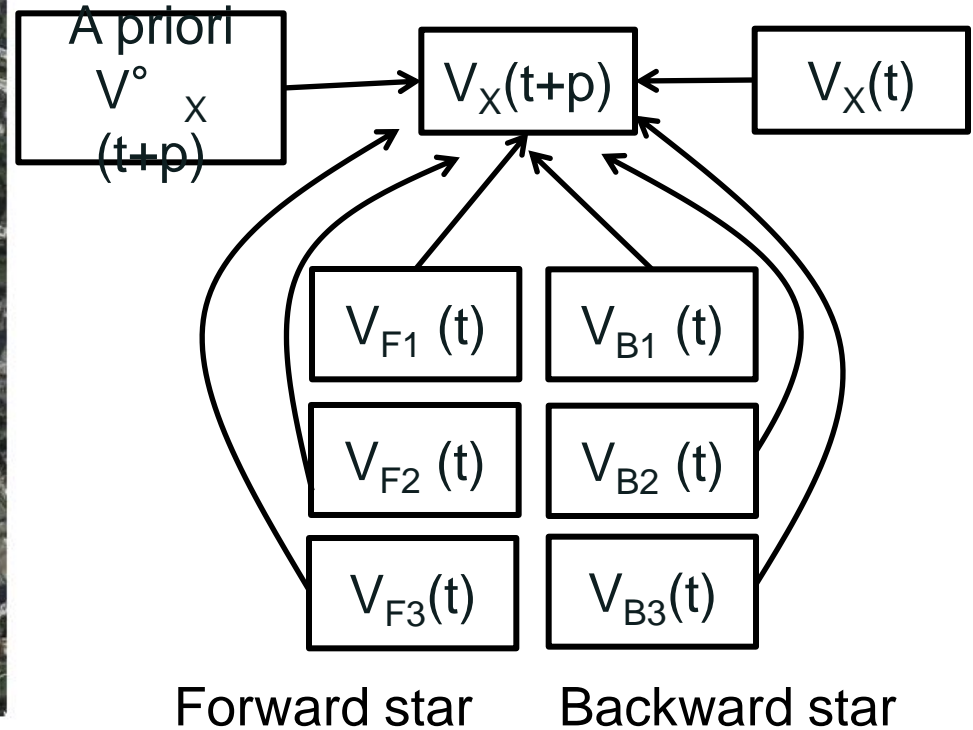
# Bayesian Network Architecture



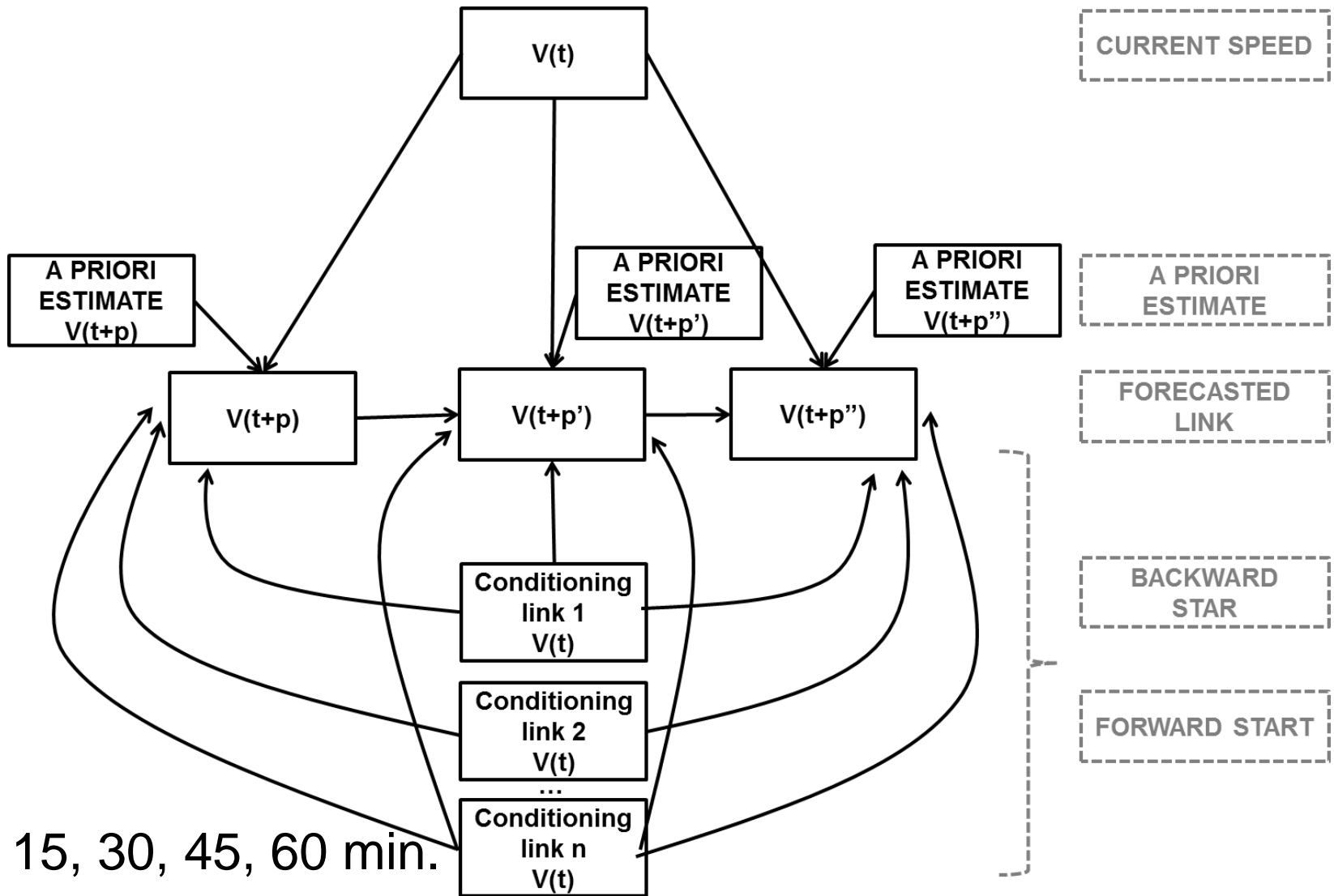
- Different architectures were tested to reflect physical relationships between close links.
- Serial links are useful when some data of a parent node are missing

# Model test

- Different model network architecture related to road network topology
- Different number of parameters and training algorithms



# Multistep BN prediction horizon



$p=5, 15, 30, 45, 60$  min.

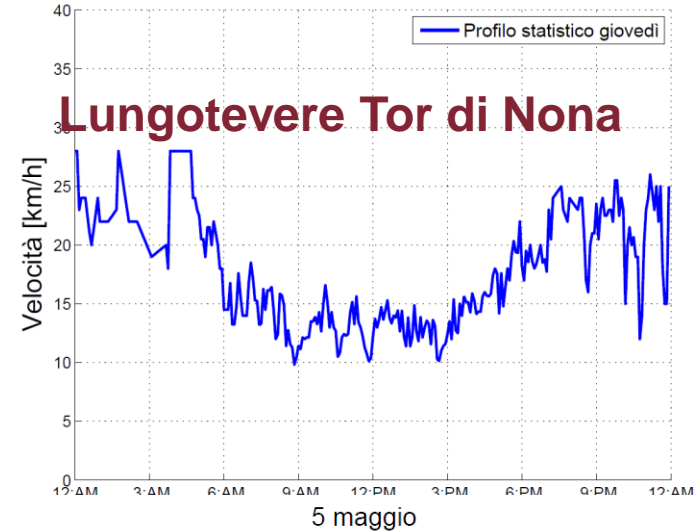
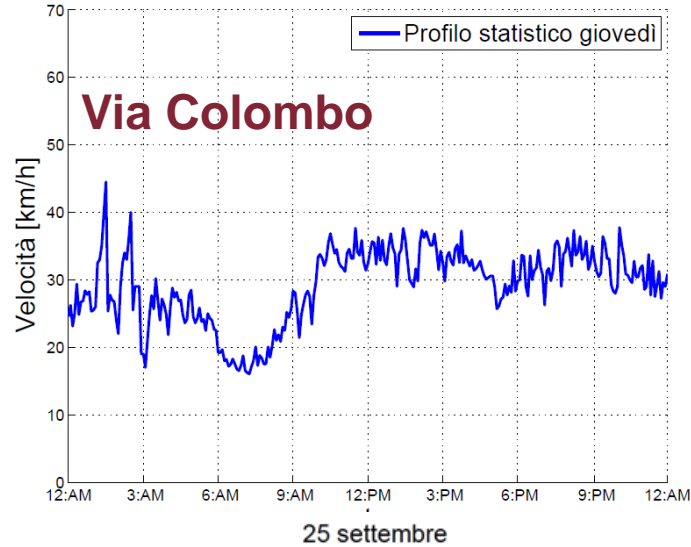


# Application of Neural Networks

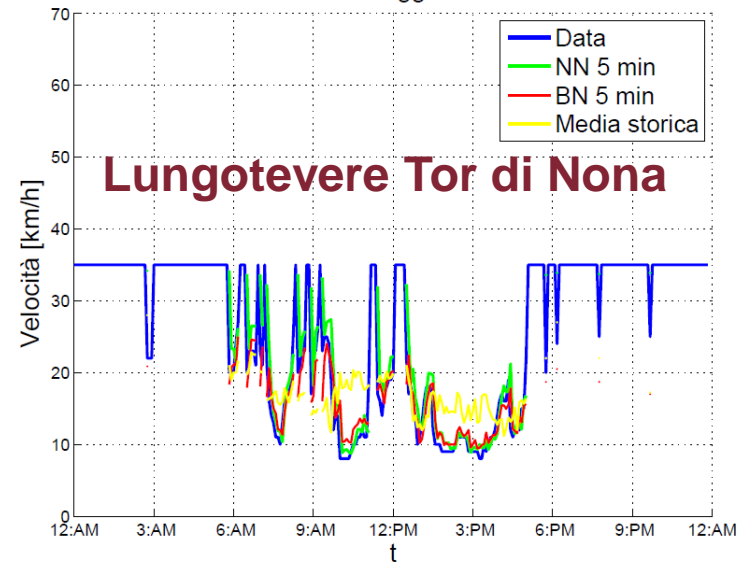
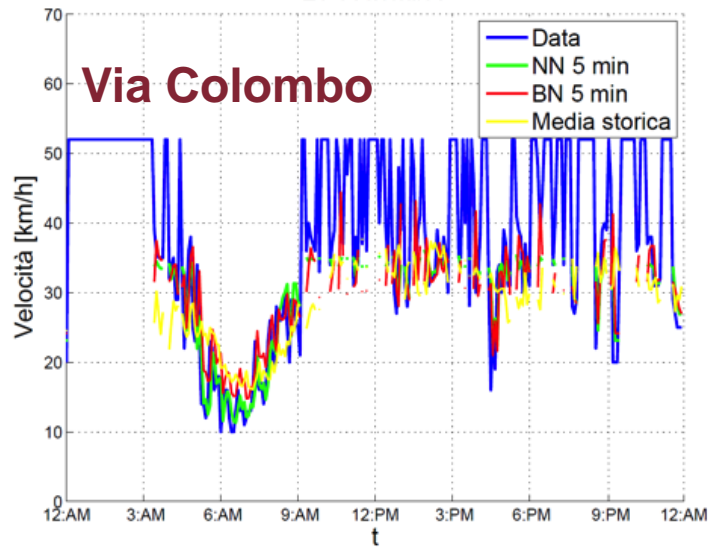
- Neural Network architecture:
  - One hidden layer;
  - 2-40 hidden neurons;
  - 4 different architectures considered;
  - Training algorithms: classical Levenberg-Marquardt and Levenberg-Marquardt with Bayesian regularization;
  - Input-output correlation, convergence and autocorrelation examined.
- The final structure: 12 hidden neurons; input data collected in 6 previous time intervals on forward and backward star links

# From a priori to a posteriori

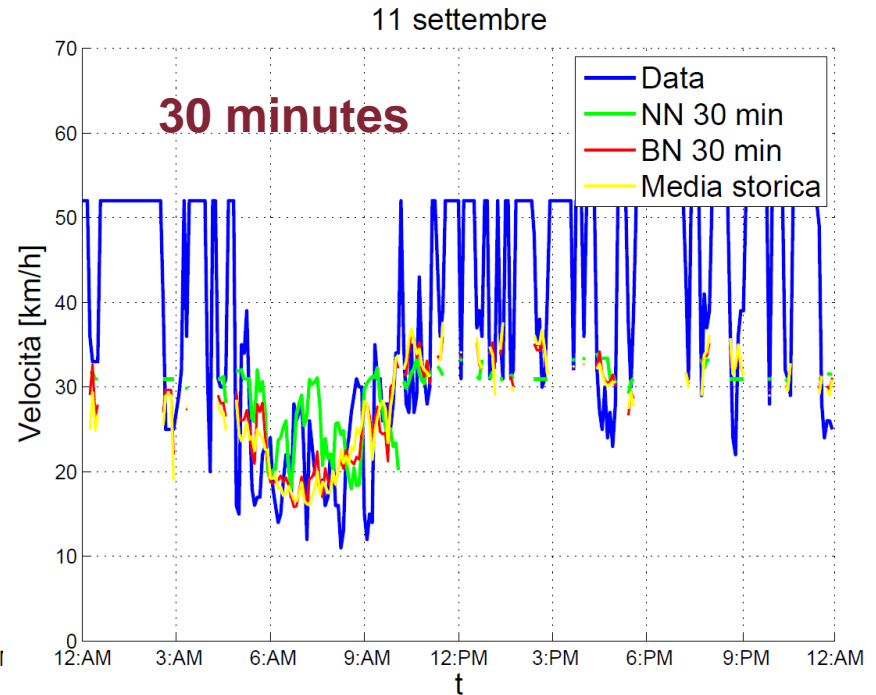
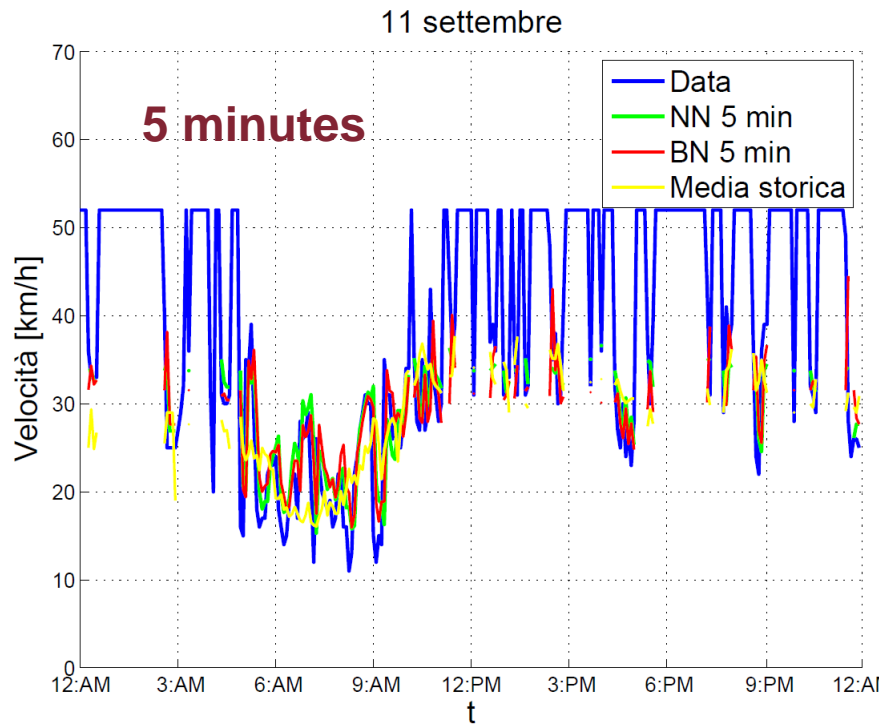
A priori estimate



A posteriori estimate



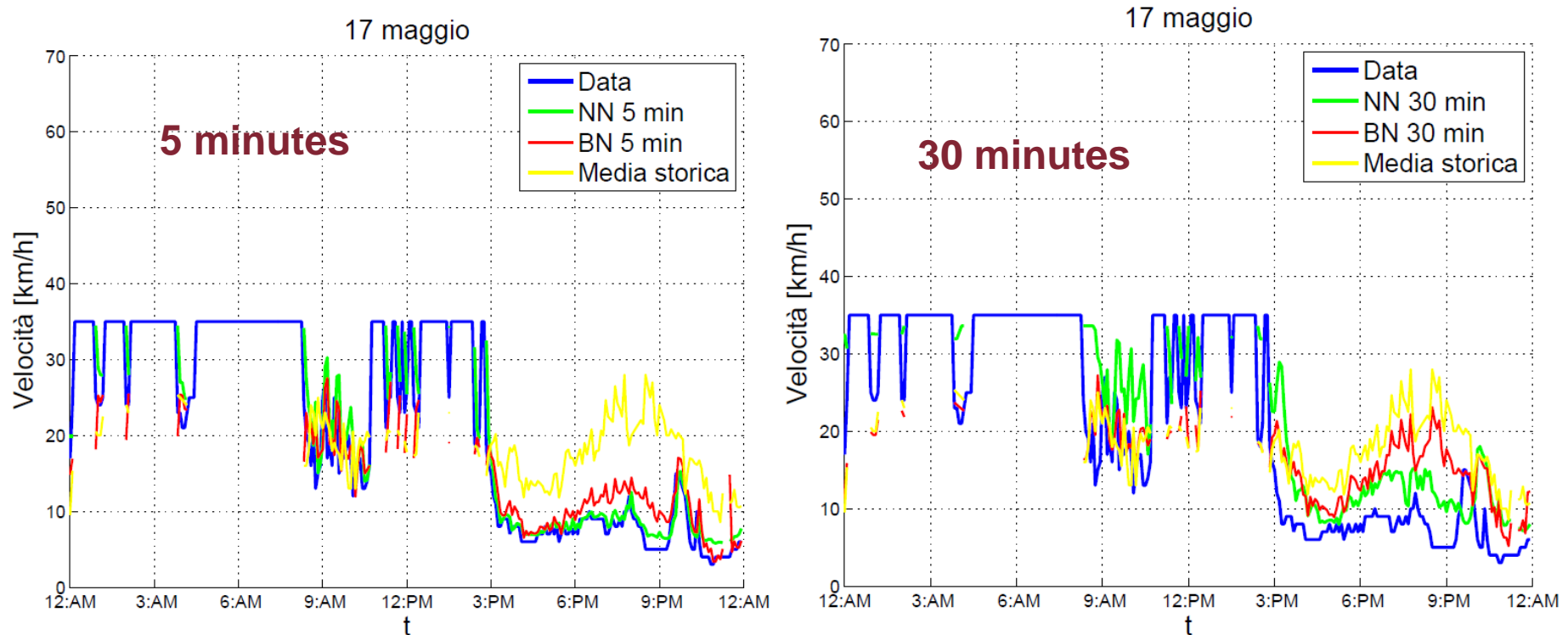
# Results: recurrent noisy congestion



- for 5 min. interval both models provide good estimates
- for 30 min. noisy data lead to overestimate by Neural Network.

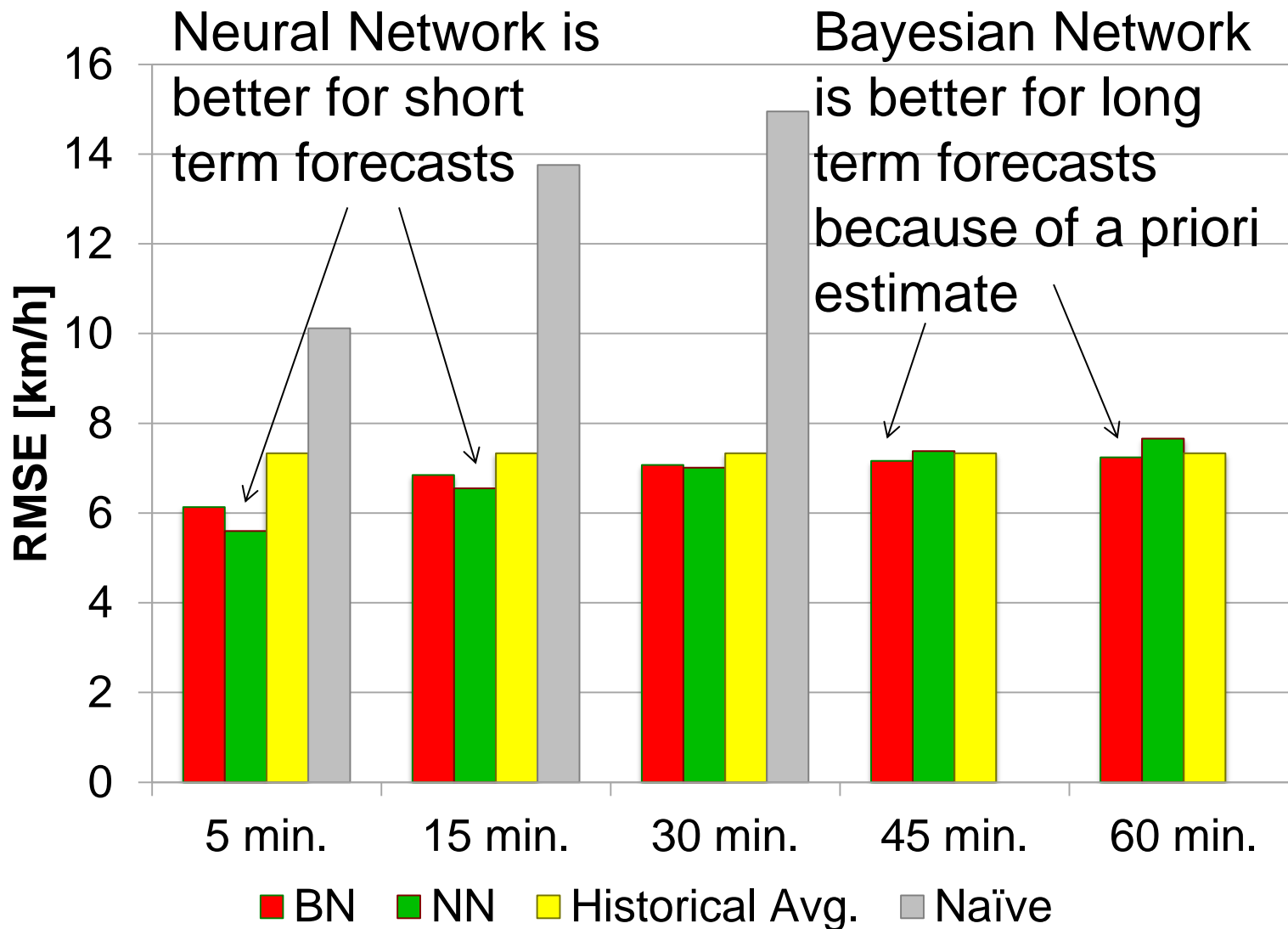
# Results: non-recurrent congestion

## Lungotevere Tor di Nona



- for 5 minutes interval both models provide good estimates;
- for 30 minutes only Neural Network follows the actual speed trend.

# Error evaluation (via C.Colombo)





# Conclusions

- Application of Neural and Bayesian Networks shows that an appropriate graph structure of models can improve forecast performances with respect to historical average or naïve predictions
- Accuracy worsens as prediction horizon increases:
- FFW Neural networks can be applied up to 15-minute predictions
- Bayesian Network with statistical a priori forecast is better in standard conditions for longer predictions
- Time-dependent Neural Network outperforms BN in anomalous conditions
- A supervisor can be introduced to choose the best model depending on observed data pattern