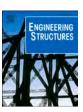
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Issues related to typological fragility curves derivation starting from observed seismic damage

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ABSTRACT

In this study typological fragility curves are proposed with a macro-seismic approach. To this scope, a stock of 56.338 residential masonry buildings struck by L'Aquila 2009 seismic sequence is analyzed, whose *AeDES* forms are archived within *Da.D.O.* platform, that is a web-gis database collecting the observed seismic damage data related to buildings surveyed after several Italian earthquakes.

Moreover, issues significantly influencing the fragility curves derivation are in depth discussed. In particular, a criterion for the buildings stock completion adding undamaged and not surveyed buildings is proposed, based on the distributions known of the residential building typologies. Comparisons highlight that the database completion affects the resulting fragility curves, and in particular for low damage levels. Furthermore, it is shown how the fundamental parameters estimation, by using the *Maximum Likelihood Estimation (MLE)* method, is conspicuously influenced by the *PGA* intervals number $(n_{\rm int})$, that is an issue often ignored when fragility curves are derived. The numerical investigations show that, although a non-monotonic trend is observed, the fundamental parameters tend to converge to the asymptotic values as the $n_{\rm int}$ of *PGA* increases, and that they are markedly dispersed when $n_{\rm int}$ is low.

1. Introduction

In recent years many methods have been developed for designing and assessing seismic performance of a structure in a probabilistic manner. These methods, such as for instance the *Performance-Based Earthquake Engineering (PBEE)* further developed in *ATC-58* project [42, 43], require the application of fragility curves in order to evaluate damage and losses due to seismic scenarios. Contrarily to the vulnerability curve providing a seismic loss (in terms of the direct damage cost, casualties, or downtime), a fragility curve measures a probability of exceeding a certain *Damage Level (DL)* or *Limit State (LS)* for a given *Intensity Measure (IM)* expressing the ground shaking [46]. Moreover, when a good quality of empirical loss data is not available, it is also possible to indirectly derive a vulnerability curve starting from a fragility curve by means of damage-to-loss functions [50].

Fragility curves have become undoubtedly an essential tool to

compute and to prevent economic and social losses [13] within a probabilistic approach, where uncertainties of model (epistemic due to lack of knowledge) and aleatory (typically including record-to-record variability) may be taken into account [22].

To date, several approaches have been proposed in order to obtain structural fragility curves, essentially derived with two different approaches: numerical approaches, by using structural models to predict seismic damage [2,23,47,6,9]; macro-seismic approaches, based on damage survey (observational criterion) of a buildings stock after a certain seismic sequences (one or more) [11,14,24,39,59,60,68]. Recently, also a hybrid approach has been proposed by combining the information derived from observed damage with numerical analyses [36].

As regards numerical approaches, *Non-linear Dynamic Analysis (NDA)* with the *Incremental Dynamic Analysis (IDA)* procedure may be utilized [61]. To this scope, a set of accelerograms is chosen, amplified or scaled

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to estimate the structural response for each shaking intensity. Similar results can be obtained with the *Multiple Stripe Analysis (MSA)* method, where accelerograms records are scaled in relation to a common *IM* [34], or with the *Cloud* method, where unscaled accelerations and linear regressions are used [12,35]. However, given complexity and high computational costs required, simplified tools for fragility curves construction have been proposed, too. Among these, in Baltzopoulos et al. [6] the *SPO2FRAG* approach has been presented, including the *SPO2IDA* presented [62] for deriving approximated *IDA* results from *Static Push-Over (SPO)* curves of *Non-linear Static Analyses (NSA)*.

As for the macro-seismic approach, pioneer works were proposed since early 70's, in which the buildings seismic behaviour was expressed in probabilistic terms by means of Damage Probability Matrices (DPMs), derived from the observed damage. DPMs express in a discrete form the occurrence probability of certain DL conditioned to an IM. Among the others, in Whitman, Reed, & Hong [63] DPMs were defined for 9 damage categories due to San Fernando 1971 earthquake. Braga, Dolce, & Liberatore [8] defined DPMs according to the Medvedev-Sponheuer-Karnik (MSK-76) macro-seismic scale [44] of about 36.000 buildings surveyed after the Irpinia 1980 earthquake. In Sabetta, Goretti, & Lucantoni [55] the limitation due to the use of macro-seismic IM was eliminated, by applying the MSK scale with different parameters for deriving fragility curves starting from a stock of about 50.000 buildings struck by different Italian earthquakes. More recently, Zuccaro & Cacace [65] proposed DPMs by analysing about 170.000 buildings damaged by several Italian earthquakes, from Irpinia 1980 to Etna 2002. In order to permit the comparison among the different building stocks, in this study a new synthetic parameter was proposed, considering typological classes basically based on the vertical structure types.

Recently, rather than using *DPMs*, fragility curves are preferred because of they express a damage probability measure in a continuous form. To date, in literature a huge number of fragility curves are proposed starting from the seismic damage observed in past earthquakes, differing each other for several aspects such as: characteristics of buildings stocks considered, number and type of information, reference *IM* chosen. Among the others, one may mention the recent works of Rota, Penna, & Strobbia [54], Chieffo & Formisano [10], Del Gaudio et al. [16], Rosti, Rota, & Penna [53], Zuccaro et al. [66] and Biglari & Formisano [7].

As known, when macro-seismic approach is applied for deriving typological fragility curves buildings stock data completeness represents an important issue. This is due to the fact that, during the postearthquake phase, seismic damage surveys are reasonably carried out on the totality of buildings only in the epicentral area. Conversely, far from the epicentre, post-earthquake surveys tend not to regard all buildings, but only the damaged ones. Therefore, an epistemic uncertainty (bias) is obtained on the observed data since information on undamaged buildings, since not surveyed, is unknown. Several Authors in literature have faced the building stock data completeness issue, proposing completion procedures in order to derive more reliable fragility curves. In Del Gaudio et al. [15] fragility curves are proposed considering only residential buildings located in municipalities with I_{MCS} higher than VI and surveyed according to Dolce & Goretti [18], by assuming that these municipalities were completely surveyed after L'Aquila 2009 earthquake. Procedures for including also municipalities affected by an earthquake, but not surveyed, are proposed in Del Gaudio et al. [16] and Rosti, Rota, & Penna [53]. In Zuccaro et al. [66], the database completion is performed considering a completeness index evaluated as a function of the Peak Ground Acceleration (PGA). Currently, in D'Amato et al. [14] and Laguardia et al. [39] a completion procedure is proposed based on the L'Aquila 2009 buildings stock and regarding municipalities having $I_{MCS} \leq VI$. The procedure assumes that the completion of undamaged and not surveyed buildings follows the breakdown distribution of some reference municipalities, assumed completely surveyed.

To this it should be added that procedure adopted may significantly

affect the fragility curves derived. As known, fundamental parameters estimation is done by maximizing the occurrence probabilities product of the observed seismic damages with *Maximum Likelihood Estimation (MLE)* method [5,40]. To date, although this method is largely applied in the scientific literature, influence of buildings stock damage partitioning for a given *IM* has not been duly argued yet, and how it may affect the fragility curves is frequently ignored. Concerning this topic, few indications may be found in literature. In Spence et al. [58] and Karababa & Pomonis [37] a minimum number of 20 buildings for each sub-sample of building damage is suggested. Whereas, Del Gaudio et al. [15] assumes that the sub-samples number is linked to the buildings stock size, so that the same buildings number is guaranteed in each sub-sample and for any *IM* range.

In this paper typological fragility curves with the macro-seismic approach are derived, by referring to the masonry buildings stock of L'Aquila 2009 earthquake available in Da.D.O. (Observed Damage Database) web-gis database ([21] Dipartimento della Protezione Civile; [20]). Starting from 74.049 buildings of 129 municipalities having AeDES forms [4] typological fragility curves are derived, by analysing only 56.338 buildings with a residential destination declared. Typological fragility curves are derived not only by referring to typological classes defined according to AeDES forms, but also considering the mixed ones having different horizontal structural elements. At first, a completion database procedure is proposed and applied, requiring additional information available in the Italian national census. This procedure provides a breakdown of undamaged and not surveyed masonry buildings belonging to all the structural typologies considered in the AeDES form. Moreover, attention is also paid to the choice of the sub-samples number when the buildings stock seismic damage is partitioned by varying a given IM. Finally, comparisons are illustrated and commented in order to highlight the importance of these issues in deriving the fragility curves with the macro-seismic approach.

2. Buildings stock of L'Aquila 2009 earthquake

On 6th April 2009, at 03:32 a.m. an earthquake of moment magnitude $M_w = 6,1$ [29] occurred, with the epicentre site near the city of L'Aquila (Italy) at a depth of 8,8 km in the Italian Abruzzi region [18]. The earthquake had in the epicentral area a macro-seismic intensity $I_{MCS} = \text{IX-X}$ [57] according to Mercalli-Cancani-Sieberg (MCS) scale.

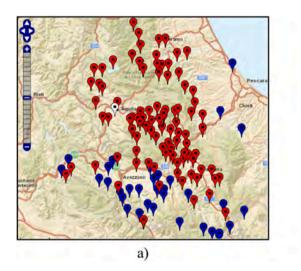
Survey activities were coordinated by the Italian Civil Protection Department (D.P.C.), starting from 7th April 2009. At first, strategic buildings were surveyed for immediate safe occupation in case of aftershocks [18]. Afterwards, surveys were extended also to residential buildings by using the rapid post-earthquake damage first level evaluation form, named AeDES form [4]. They were aimed at detecting seismic damage occurred, and at evaluating the usability of ordinary buildings after the earthquake. The AeDES forms compiled during L'Aquila 2009 surveys are nowadays available on Da.D.O. platform (Observed Damage Database, D.P.C., 2015; [20]), that is a web-gis database collecting the seismic damage data related to buildings surveyed during, or after, a seismic sequence having a national impact. Currently, Da.D.O. collects AeDES forms for the following earthquakes: Friuli 1976, Irpinia 1980, Abruzzo 1984, Umbria-Marche 1997, Pollino 1998, Molise 2002, Emilia 2003, L'Aquila 2009, Emilia 2012, Garfagnana-Lunigiana 2013, Centro Italia 2016-2017 and Mugello 2019.

AeDES form consists of several sections and, in particular, elaborations shown in this work are performed starting from data reported from *Section 1* to Section 4 of *AeDES* form.

In detail, Section 1 contains information concerning the building identification and its survey.

Section 2 collects data concerning age, construction period, metrical data, any building renovation, building use and its exposure (isolated or within an aggregate).

Section 3 is a fundamental section focused on some vulnerability indicators that may influence the seismic response of a building, mainly



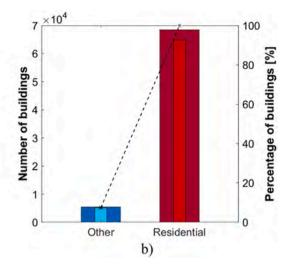
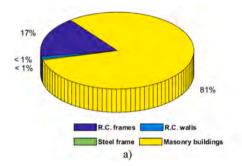


Fig. 1. (a) Municipalities where *AeDES* forms refer to residential buildings (red pins) and only to non-residential buildings (i.e. having public destinations, blue pins) respect to the mainshock epicenter (white pin); (b) Number and percentage of surveyed buildings: residential buildings (red histograms) and others (blue histograms).



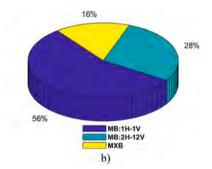


Fig. 2. (a) Percentage distribution for construction material of residential buildings surveyed after the L'Aquila 2009 earthquake; (b) Percentage distribution of residential masonry buildings surveyed by considering the type of vertical and horizontal structural element.

depending on the combination between vertical and horizontal structures. In this section a building may be classified in Reinforced Concrete (RC) or steel, only if the entire load-bearing structures are in one of these building materials. As for masonry buildings, it is possible to identify at the most two combinations of predominant horizontal and vertical structural components (the second should be reported only if present with a significant extent). Whereas, mixed masonry buildings are buildings having a combination of masonry and RC/steel elements. Section 3 considers five types of masonry for vertical structural elements: unidentified (type A); irregular texture and masonry of poor quality without (types B) and with (type C) tie-rods and tie-beams; or regular texture and masonry of good quality without (types D) and with (type E) tie-rods and tie-beams. This classification reflects the expected seismic behaviour, by assigning increasing seismic vulnerability to the masonry types for vertical structures considered. In particular, a regular texture tends to show a monolithic behaviour under seismic loads, excluding a local disaggregation of the masonry. While the presence of tie-rods and tie-beams contrast out-of-plane overturing failure mechanisms. According to the Section 3, the masonry vertical elements can be combined with six types of horizontal structural elements, that are: undefined members (type 1); vaults with/without tie-rods (type 2, type 3); and beams with flexible, semi-rigid and rigid slabs (type 4, type 5, and type 6). Even in the case of horizonal structural elements classification reflects different vulnerability levels of masonry buildings. As for vaulted floors, presence of tie-rods reduces as known the vertical loads thrust. As for slabs, they are differentiated with respect to their in-plane deformability and capacity to provide global box-like behaviour, in

which out-of-plane overturning is prevented and seismic forces are distributed according to the in-plane stiffness of masonry walls. Horizontal structures having slabs from *type 4* to *type 6* tend progressively to provide a global box-like behaviour, with a reducing vulnerability passing from *type 4* to *type 6*. Finally, through the combination between vertical and horizontal structural elements previously defined it is possible to classify each building considered, identifying a specific structural typology to which correspond a certain level of seismic vulnerability. Therefore, typological classification provides useful information on the expected seismic vulnerability of a building.

Section 4 reports the damage detected with the visual inspection, that could be pre-existing or due to the seismic event. For each structural component (vertical structural elements, horizontal structural elements, stairs, roof and vertical partitions) a damage intensity is assigned according to the *EMS-98* scale [28], that are: D_0 (null damage), D_1 (low damage), D_2 - D_3 (moderate or heavy damage), and D_4 - D_5 (very heavy damage or collapse). Moreover, in this section damage level extent may be assigned, according to three percentage ranges of damage, such as >2/3, 1/3–2/3, and <1/3, evaluated on the elements total number of the same type. For a more detailed description of the *AeDES* form sections the reader is referred to [4].

In total, as for the L'Aquila 2009 earthquake *Da.D.O.* collects *AeDES* forms of 74.049 buildings, located in 129 municipalities. More in detail, this stock consists of 68.556 buildings having an *AeDES* form with a declared residential destination. They fall in 95 of 129 municipalities suffered the earthquake swarm considered. While, the remaining 5.493 (74.049 – 68.556) buildings have a public destination, i.e. different from

Table 1Masonry structures typologies (reported in *AeDES* form Section 3).

| Vertical structural element | Unidentified (A) | Irregular ter poor quality | | | Regular texture and good quality | | |
|---------------------------------------|---------------------|--|--|--|--|--|--|
| Horizontal structural element | | Without tie-rods and tie- beams (B) | With tie-rods and tie- beams (C) | Without tie-rods and tie- beams (D) | With tie-rods and tie- beams (E) | | |
| Unidentified (1) | 1A | 1B | 1C | 1D | 1E | | |
| Vaults without tie- rods (2) | 2A | 2B | 2C | 2D | 2E | | |
| Vaults with tie-rods (3) | 3A | 3B | 3C | 3D | 3E | | |
| Beams with deformable slabs (4) | 4A | 4B | 4C | 4D | 4E | | |
| Beams with semi-rigid slabs (5) | 5A | 5B | 5C | 5D | 5E | | |
| Beams with rigid slabs (6) | 6A | 6B | 6C | 6D | 6E | | |

the residential one, located in 34 (129-95) municipalities. Fig. 1a depicts the 95 municipalities where residential buildings were surveyed (red pins), and the remaining 34 (129-95) ones where, instead, only other destinations were found (i.e., buildings having an AeDES form not reporting a residential destination, indicated with a blue pin). All inspections were coordinated by the Italian Civil Protection Department, that before building inspections defined 27 non-accessible zones, named "red zones" located in the L'Aquila historical centre and in the surrounding zones. Then, survey activities were initially extended to less damaged areas in order to limit the risks for surveyors in case of after-shocks, with the aim of identifying immediately usable buildings [27]. A higher priority was given to public buildings (schools, hospitals, industrial activities, etc.) than to residential ones, which were investigated only in municipalities with $I_{MCS} \ge VI$ and only upon request in other cases [18]. For completeness, Fig. 1b reports the corresponding buildings numbers (larger histograms), the related percentage (inner tighter histograms) and the cumulative percentage (dashed line).

The total number of residential buildings (68.556) represent about 93% of the buildings stock surveyed (74.049), whose breakdown percentage in terms of construction materials is indicated in Fig. 2a. It is easy to note that: the dominant typology is represented by masonry structures having 81% of occurrence percentage (56.338); the *RC* frame structures represent the 17% of the stock considered (11.715); whereas for steel frames and *RC* walls a percentage less than 1% is observed. An interesting result is obtained if one divides the sub-stock of masonry

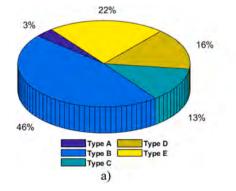
residential buildings (56.338) between buildings with only one type of vertical and horizontal structural element, and those having instead a mixed type of horizontal and/or vertical structural element, according to the typologies indicated in the Section 3 of the *AeDES* form (and reported in Table 1, where the number indicates the horizontal structural element and the letter the vertical one).

In this case it is found that (Fig. 2b):

- 56% of Masonry residential Buildings (MBs) has one type of horizontal and vertical structural element, briefly indicated in Fig. 2b as MB:1H-1V:
- 28% of MBs has a combination of two types of horizontal structural element and one or two types of vertical structural element, indicated as MB:2H-12V. It is considered that MB:2H-12V = MB:2H-1V + MB:2H-2V where MB:2H-1V and MB:2H-2V refer to buildings with one or two types of vertical structural element;
- 16% of buildings with mixed types of vertical structural element (e.g. masonry-RC, masonry-steel, reinforced masonry, etc.), and one or two horizontal structural elements (MXB).

56.338 residential buildings may be further analysed by considering the vertical structural element occurrence. To this scope, Fig. 3a shows the percentage distribution of masonry buildings with one vertical and horizontal structural element (buildings MB:1H-1V with 56% of Fig. 2b), where type A to E identify the vertical structural element according to Table 1. Fig. 3a indicates that the most frequent vertical structural element results the type B having a 46% (14.520 buildings) of occurrence; while the types C to E are present with percentages of 13%, 16% and 22%, respectively. Finally, one may note that 3% of vertical structures are unidentified (type A, 1.090 buildings). Whereas, Fig. 3b refers to the masonry buildings MB:2H-12V representing the 28% of Fig. 2b, having a combination of two horizontal structural elements and one (types B to E) or two vertical structural elements (type A-2VS). In this case, we obtain: 53% of type B (8.451), 23% of type A-2VS, 13% of type C, 7% of type D and 4% of type E. It is worth to note that the type A-2VSincludes the residential buildings having type A or two types of masonry vertical structural elements, too.

Furthermore, residential buildings stock (Fig. 3) may be also analysed in accordance with the possible combinations among horizontal and vertical structural elements of the *AeDES* form (Table 1). Fig. 4 refers to residential masonry buildings with one type of horizontal and vertical structural element *MB:1H-1V* (Fig. 2b; Fig. 3a). It reports the horizontal structural element distribution (*type 1* to 6 of Table 1) for each type of vertical structural element (such as *types B* to *E* in Fig. 4a-d, respectively). In this analysis buildings with unidentified masonry (*type A*) are neglected. Each histogram of Fig. 4 reports the buildings numbers (wide bars) and the related percentage (narrow bars). Finally, in each histogram a dashed line is depicted as well, representing the cumulative percentage. It is clear to observe that in the buildings stock analysed



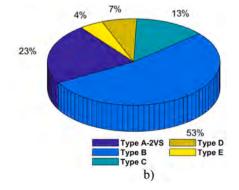


Fig. 3. Masonry buildings with (a) one type of horizontal and vertical structural element (MB:1H-1V); (b) two horizontal structural elements and one or two types of vertical structural element (MB:2H-12V).

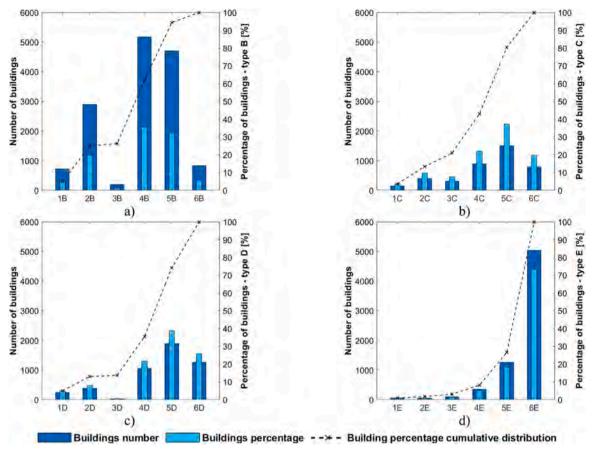


Fig. 4. MB:1H-1V. Residential buildings having a vertical structural element of: (a) type B; (b) type C; (c) type D; (d) type E, by varying the type of horizontal structural element (from 1 to 6 according to the Table 1).

masonry of poor quality (*type B* of Fig. 4a) is the dominant vertical structural element, combined with vaults (*type 2B*, 2.895 buildings, \cong 20%), beams with deformable slabs (*type 4B*, 5.172 buildings, \cong 35%), and beams with semi-rigid slabs (*type 5B*, 4.700 buildings, 30%).

Similarly, Fig. 5 shows the percentage distribution of masonry buildings with two types of horizontal and one type of vertical structural elements *MB:2H-1V*. It considers several combinations of two horizontal structural elements (*type 1* to 6 of Table 1) for each type of vertical structural element (such as *types B* to *E* in Fig. 5a-d, respectively). In this case the most frequent horizontal structural elements combinations are *types 2B–4B*, *2B–5B*, *4B–5B*, *2C-5C* with, respectively, 2.980, 2.871, 871 and 541 buildings.

As previously mentioned, the Section 4 of the *AeDES* form [4] classifies seismic damage to be assigned to each structural component in four levels, that are D_0 , D_1 , D_2 - D_3 and D_4 - D_5 , based on *EMS-98* scale and *GNTD* survey forms [25,26]. A description of these seismic damage levels referred to masonry buildings is given in Table 2. Examples of seismic damages suffered by masonry buildings during L'Aquila 2009 earthquake may be found, among the others, in Augenti & Parisi, [3], Rossetto et al. [51] and Indirli et al. [30].

The damage levels considered are assigned to each structural component, such as: vertical structures, floors, stairs, roofs, partitions and considering pre-existing damage before the occurred seismic event. For instance, Fig. 6 reports a distribution analysis of the damage level among the structural components of residential masonry buildings stock considered (56.338), referring to MB:1H-1V (Fig. 6a and previously plotted in Fig. 4) and MB:2H-1V (Fig. 6b, previously plotted in Fig. 5). In both the typological classes analysed we obtain percentages quite similar for vertical structural element, that are in this case: damage level $D_1\cong 25\%$, $D_2\cdot D_3\cong 20\%$, and $D_4\cdot D_5\cong 18\%$.

Once the damage level of each structural component is known a global building damage may be assigned. Firstly, it is necessary to convert the damage level of each structural component reported within AeDES form into EMS-98 scale, where damage is classified into six different levels, that are: D_0 (null damage), D_1 (negligible to slight damage), D_2 (moderate damage), D_3 (substantial to heavy damage), D_4 (very heavy damage) and D_5 (destruction). Table 3 reports the conversion used, developed by the Institute for Buildings Technology of the National Council of Research (CNR-ITC) where, for a given structural component, a resulting EMS-98 damage level is associated considering several combinations of damage and extension starting from the AeDES form damage level available [20].

Then, a global building damage may be estimated starting from the structural elements damage. To this scope several Authors proposed different criteria for the global damage estimation. In Di Pasquale & Goretti [17], Angeletti et al. [1] and Lagomarsino, Cattari, & Ottonelli [38] the building damage is calculated as the Weighted Sum (WS criterion) of the components damage, each of which having a specific weight. Instead, Rota, Penna, & Strobbia [54] assign the global damage by considering only the Maximum Damage (MD criterion) observed among the structure primary components, such as vertical and horizontal structural elements, and roofs. In this study the global damage is estimated according to the MD criterion because of, usually, usability assessment and reconstruction costs are mainly influenced by the most damaged structural element [54]. Furthermore, it is worth noting that with the MD criterion a more conservative approach is followed, since an overestimation of the global damage is obtained with respect to the WS criterion. Moreover, the MD criterion permits a faster seismic damage evaluation, since only few structural elements are analysed, that are vertical and horizontal structural elements, and roofs. Details about

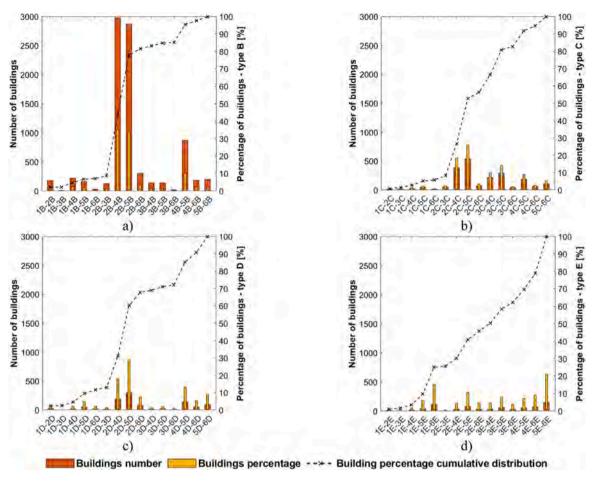


Fig. 5. *MB:2H-1V.* having a vertical structural element of: (a) *type B*; (b) *type C*; (c) *type D*; (d) *type E*, for several combinations of two horizontal structural elements (from types from 1 to 6 according to the Table 1).

Table 2Damage level description for structural components of masonry buildings according to [4].

| cording to [1]. | |
|-----------------|---|
| Damage Level | Damage description |
| $\mathbf{D_0}$ | No damage. |
| · · | This damage level may be assigned also in the case of plaster cracks |
| | due to shrinkage or small instability occurred in the past, repaired and not reactivated. |
| \mathbf{D}_1 | This damage does not significantly affect structure capacity and it does |
| | not threaten the occupants safety. |
| | It is associated to cracks having width ≤ 1 mm. No matter how they |
| | are distributed in masonry walls and in floors, without material |
| | expulsion, limited separations, or slight dislocations (≤1 mm) |
| | between parts of structures. Limited damage to the most flexible |
| | roofs with consequent falling of some tiles at the edges. Falling of |
| | small portions of degraded plaster or stucco, not connected to the masonry. |
| D_2 - D_3 | With this damage the structure capacity significantly changes, without |
| | getting close to the limit of partial collapse of the main structural |
| | components with possible falling of non-structural objects. |
| | Severe cracks, also with material expulsion, having a wide up to |
| | approximately 1 cm, symptoms of cracks due to crushing, significant |
| | separations between floors and/or stairs and walls and between |
| | orthogonal walls, some partial collapses in the secondary floors |
| | beams. Cracks of some mm in the vaults, and/or with symptoms of |
| | crushing. In roofs falling of a significant portion of the tiles covering. |
| D_4 - D_5 | With this damage the structure capacity significantly changes, bringing it |
| | close to the limit of partial or total collapse of the main structural |
| | components. |
| | |

the *MD* criterion adopted in this study may be found in D'Amato et al., [14].

3. Ground motion intensity measure

The choice of an appropriate *IM* is very important for correlating the building seismic damage to Ground Motion (GM) intensity. In general, several IMs may be used such as: macro-seismic intensity measure, a discrete measure that may be affected by the surveyor judgment, expressed for instance with the Modified Mercalli Intensity (MMI) [64] or European Macroseismic Scale (EMS) [28]; or instrumental measures, such as the PGA or Peak Ground Velocity (PGV). The use of macro-seismic intensity as IM has been largely applied in the scientific literature since a good correlation with the observed damage has been observed. To this it should be added that data referred to this IM are widespread available before instrumental devices application. Nevertheless, several disadvantages may be encountered if one refers to the macro-seismic intensity measure. Firstly, if vulnerability and fragility curves consider different intensity scales a comparison among them cannot be directly performed. Moreover, macro-seismic intensity scale consider unit intervals that may not be equal, and fractional values are not considered. Finally, in literature few Ground-Motion-to-Intensity-Conversion Equations (GMICEs) are available [46], introducing additional uncertainties within the risk assessment framework [50]. These drawbacks may be solved by selecting an appropriate instrumental measure as IM. In this way, it is also possible to decouple the uncertainties related to the seismic demand from the ones introduced by the fragility curves. Among these, PGA is traditionally the main parameter chosen, even because commonly used for defining seismic loads for structures and hazard maps [54,55].

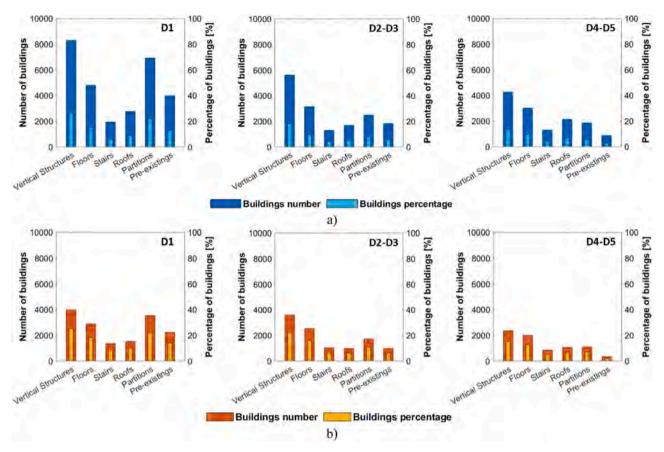


Fig. 6. Damage distributions of residential buildings components surveyed after L'Aquila 2009 earthquake: (a) MB:1H-1V buildings; (b) MB:2H-1V.

However, it may be not appropriate for correlations with the observed seismic damage, especially in the case of ductile structures or large damage states [49]. *PGV* should be more adequate in the case of deformable structures (when *PGA* becomes not adequate), but it is calculated with a direct integration of accelerograms and, therefore, it may be sensitive of record noise content and filtering process. Moreover, very few *PGV* attenuation functions are available in literature. The same limitations are to date encountered for the *Peak Ground Displacement (PGD)* [50].

Recently, there is a widespread use of Shaking map (also known as shake-map) providing an immediate visualization of the shaking level in a certain area affected by a seismic event. It is based on the interpolation algorithm of the registered GMs data and seismologic knowledge gathered from instrumental measures, taking into account local amplification effects through S-wave velocities in the upper 30 m (V_{S30}) [45]. A shake-map may display, for instance, PGA, PGV, Spectral-Acceleration of the I^{th} vibration mode $Se(T_1)$ values, or a macro-seismic intensity estimated from the data measured. Moreover, as alternative to the shake-maps, attenuation laws may be used. Among the others, recently in literature D'Amato et al. [14] and Laguardia et al. [39] proposed attenuation laws derived from L'Aquila 2009 earthquake, considering as IM the Arias Intensity (I_A), or else the $Se(T_1)$, giving the opportunity of evaluating these IMs for several periods that are not available to date within the shake-maps.

In this study, PGA is used as IM, indicated in the shake-map proposed by INGV [31] for L'Aquila 2009 earthquake. However, it should be noted that this earthquake was characterized by a seismic sequence having several epicentral sites with a similar magnitude. Fig. 7a shows their location during the earthquake swarm, related to the shocks of 6th April 2009 at 03:32 a.m. ($M_w = 6,1$), 6th April 2009 at 11:15 p.m. ($M_w = 5,0$), 7th April 2009 at 05:47 p.m. ($M_w = 5,4$), 9th April 2009 at 12:52 a. m. ($M_w = 5,2$) and 9th April 2009 at 07:38 p.m. ($M_w = 5,0$). While

Fig. 7b-d reports the *PGA* shake-maps related to the mainshock on 6^{th} April 2009 ($M_w = 6,1$), and the aftershocks on 7^{th} April 2009 ($M_w = 5,4$) and 9^{th} April 2009 ($M_w = 5,0$) [31], respectively. In the same figures masonry buildings surveyed are located with black dots, too.

As one may clearly note, in the case of L'Aquila 2009 seismic sequence, the *i-th* building may have undergone in the aftershocks a *PGA* greater than the one suffered at the mainshock (6th April 2009, $M_w = 6,1$). As proof of this, Fig. 8a depicts, by varying distance from the mainshock epicenter, the *PGA* maximum value (*PGA*_{max}) suffered by the 56.338 residential masonry buildings considered. In this figure black dots are used when the maximum value corresponds to the value occurred at the MainShock (6th April 2009, $M_w = 6,1$), i.e. *PGA*_{max}=*PGA*_{MS}. While, red dots are used when the maximum value occurred during the AfterShocks from 6th April 2009 ($M_w = 5,0$) to 9th April 2009 ($M_w = 5,0$), i.e. *PGA*_{max}=*PGA*_{AS}. As one may clearly note, for many buildings the *PGA* suffered during the aftershocks was greater than the mainshock one.

In this study, the *PGA* suffered by each building is considered as the maximum value experienced during the entire seismic sequence. This assumption is mainly due to the fact that: all shocks of the seismic sequence occurred only in three days distant (6^{th} - 9^{th} April 2009); almost the totality of the buildings stock was surveyed after the 9^{th} April because of the seismic sequence was really short (the inspection date is known on *AeDES* form). Similar approaches may be found in Rossi et al. [52], Ioannou et al. [32] and Zucconi, Romano, & Ferracuti [68]. In order to quantify the importance of this issue in the case of L'Aquila 2009 earthquake, Fig. 8b reports the percentage distribution related to 56.338 masonry residential buildings surveyed, indicating the buildings suffering a $PGA_{max} = PGA_{MS}$ (94%, 52.958 buildings), and the ones suffering a $PGA_{max} = PGA_{AS}$ (6%, 3.382 buildings). These buildings are also reported in the map of Fig. 8c, where it easy to note that the

Table 3
Conversion into EMS-98 damage levels for AeDES form damage levels.

| Damage level | Damage description | Damage levels conversion |
|-----------------|---|--|
| $\mathbf{D_0}$ | Null damage no structural damage and no non-structural damage | D_0 |
| \mathbf{D}_1 | Negligible to slight damage | D ₁ (<1/3) |
| | no structural damage and slight non- | D ₁ (1/3-2/3) |
| | structural damage | D_1 (>2/3) |
| $\mathbf{D_2}$ | Moderate damage | D_2 (<1/3) |
| | slight structural damage and moderate non- | D_1 (<1/3) - D_2 (<1/3) |
| | structural damage | D ₁ (1/3-2/3) - D ₂ (<1/3) |
| | | D ₁ (>2/3) - D ₂ (<1/3) |
| D_3 | Substantial to heavy damage | D ₁ (<1/3) - D ₂ (1/3-2/3) |
| | moderate structural damage and heavy | D ₁ (1/3-2/3) - D ₂ (1/3- |
| | non-structural damage | 2/3) |
| | | D ₂ (1/3-2/3) |
| | | D_2 (>2/3) |
| | | D ₁ (<1/3) - D ₂ (>2/3) |
| | | D ₃ (<1/3) |
| | | D ₁ (<1/3) - D ₃ (<1/3) |
| | | D ₁ (1/3-2/3) - D ₃ (<1/3) |
| | | D ₁ (>2/3) - D ₃ (<1/3) |
| | | D_2 (<1/3) - D_3 (<1/3) |
| | | $\mathbf{D_1}$ (<1/3) - $\mathbf{D_2}$ (<1/3) - |
| | | D ₃ (<1/3) |
| D_4 | Very heavy damage | D ₂ (1/3-2/3) - D ₃ (<1/3) |
| | heavy structural damage and very heavy | D ₂ (>2/3) - D ₃ (<1/3) |
| | non-structural damage | D ₃ (1/3-2/3) |
| | | D ₁ (<1/3) - D ₃ (1/3-2/3) |
| | | D ₁ (1/3-2/3) - D ₃ (1/3- |
| | | 2/3) |
| | | D_2 (<1/3) - D_3 (1/3-2/3) |
| D_5 | Destruction | D ₂ (1/3-2/3) - D ₃ (1/3- |
| | very heavy structural damage | 2/3) |
| | | D ₃ (>2/3) |
| | | D ₁ (<1/3) - D ₃ (>2/3) |
| | | D ₂ (<1/3) - D ₃ (>2/3) |

buildings with a $PGA_{\rm max}=PGA_{AS}$ are located near the aftershocks epicenters, and withitn a distance interval between 20 and 30 km from the mainshock epicenter. Moreover, for completeness Fig. 8d plots the difference percentage $\Delta_{PGA}=(PGA_{\rm max}-PGA_{MS})/PGA_{MS}(\%)$, by varying the distance from the mainshock epicentre. It is easy to note that the 6% of masonry residential buildings (Fig. 8b) during the aftershocks has registered a PGA value up to 60% higher than the mainshock one (PGA_{MS}) .

For these reasons, in this study we refer to the PGA_{max} values suffered by any residential masonry building during L'Aquila 2009 seismic sequence, obtained as the envelope among the PGA shake-maps proposed in INGV [31]. Moreover, currently no information in AeDES forms is available on the evolution of the building seismic damage during this seismic sequence.

4. Fragility curves

A fragility curve provides the conditional probability that a *Damage* (D) takes place for a given IM value, reaching or exceeding a certain value (D_i). One of the most widely adopted representation for the fragility curve is the log-normal cumulative distribution function (Eq. 1). This distribution is very commonly used for fragility curves because of it is asymmetric about the mean and skewed to the left, reflecting better the frequency distribution of a certain IM, such as the PGA. The fragility function has the following expression [50]:

$$P_{D \ge D_i} = P(D \ge D_i | IM) = \Phi \left[\frac{\ln \left(\frac{IM}{\theta} \right)}{\beta} \right] \quad i = 1, ..., 5$$
 (1)

where $P_{D>D_i}$ is the fragility curve for *i-th* damage D_i ; Φ is the standard

normal cumulative distribution, ϑ and β are, respectively, IM median value and IM logarithmic values standard deviation.

The fundamental parameters (ϑ, β) are estimated through the *Maximum Likelihood Estimation (MLE)* method, allowing us of maximizing the observed damage data occurrence probability [40,5,56]. According to this method it is possible, within a certain buildings stock and for each typological class, to partition the sample available in several intervals (i.e. sub-samples) having a constant amplitude $\Delta IM = IM_{\rm max}/n_{\rm int}$, where $IM_{\rm max}$ is the maximum IM available, and $n_{\rm int}$ the intervals number chosen. The j-th interval (bin) is given by $IM_j \pm \Delta IM/2$, centred on the mean value IM_j , including buildings stock damage from D_0 to D_5 [5]. In this study uncertainties due to the estimation on the shake-map of the IM considered were not taken into account.

Then, the likelihood function \mathcal{L}_j in the *j-th* sub-sample is defined with the binomial probability distribution function (Eq. 2) to be maximized to find the fragility curve fundamental parameters:

$$\mathscr{L}_{j} = \begin{pmatrix} k_{j} \\ z_{j} \end{pmatrix} \bullet p_{j}^{k_{j}} \bullet (1 - p_{j})^{z_{j} - k_{j}}$$

$$\tag{2}$$

where k_j is the buildings number having a damage greater or equal than a specific damage level $(D_0, D_1, ..., D_5)$; z_j is the buildings number in the j-th sub-sample; p_j is the probability of exceedance of the damage D_i expressed with the Eq. 1.

Finally, by considering the independence among the sub-samples data, the parameters θ_i and β are obtained by maximizing the product of the likelihood functions (Eq. 2), expressed logarithmic form [46] as follows:

$$(\vartheta_{1}, ..., \vartheta_{5}, \beta) = \operatorname{argmax} \sum_{i=1}^{5} \sum_{j=1}^{m} \left\{ \ln \left(\frac{k_{j}}{z_{j}} \right) + k_{j} \right.$$

$$\bullet \ln \left[\Phi \left(\frac{\ln \left(\frac{IM}{\vartheta_{i}} \right)}{\beta} \right) \right] + (z_{j} - k_{j}) \bullet \ln \left[\Phi \left(\frac{\ln \left(\frac{IM}{\vartheta_{i}} \right)}{\beta} \right) \right] \right\}$$

$$(3)$$

where $(\vartheta_1, ..., \vartheta_5, \beta)$ indicate, respectively, the median value and the logarithmic standard deviation of IM values for each D_i . In order to prevent the fragility curves intersection, a unique IM logarithm values standard deviation (β) is considered for all the curves [46].

5. Undamaged buildings estimation

The statistical elaborations presented in Sect. 2 refer to the masonry residential buildings stock available in the *Da.D.O.* database for L'Aquila 2009 earthquake that is, as already discussed, composed by buildings surveyed after the mainshock of 6th April 2009.

However, it is reasonable to expect that the buildings stock considered results incomplete, in the sense that it does not represent all the buildings that suffered the L'Aquila 2009 earthquake, but only the ones inspected to which an *AeDES* form was assigned. In other words, it could exist a certain number of not surveyed and, very likely, undamaged buildings after L'Aquila 2009 seismic sequence not included within the buildings stock considered in this study. Therefore, if one would perform a more reliable analysis of the seismic damage observed, also undamaged buildings should be taken into account requiring, hence, a database completion.

In this study, as discussed in the previous sections, the buildings stock for deriving fragility curves consists of 56.338 masonry residential buildings, falling into 95 municipalities having an *AeDES* form. This buildings stock is compared with the information collected in the 15th database census conducted by the *Italian National Statistics Institute* [33] in 2011, since it is the closest database to the 2009 when L'Aquila

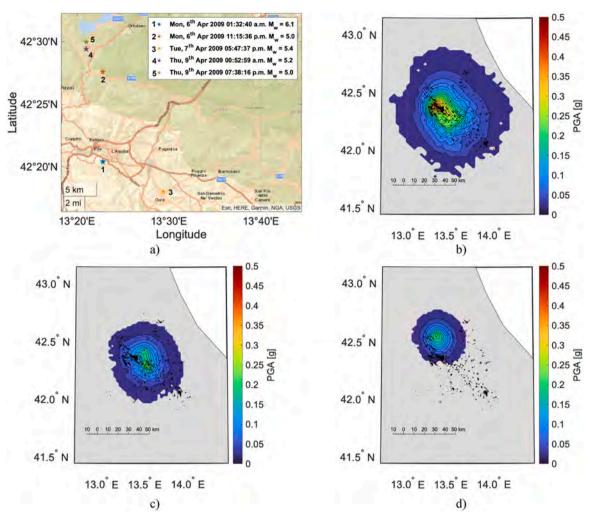


Fig. 7. (a) Epicentral sites of L'Aquila 2009 seismic sequence with $M_w \ge 5$; (b) *PGA* shake-map of the mainshock on 6th April 2009 01:32:40 a.m., $M_w = 6,1$; (c) *PGA* shake-map of the aftershock on 7th April 2009 05:47:37 p.m., $M_w = 5,4$; (d) *PGA* shake-map of the aftershock on 9th April 2009 07:38:16 p.m. $M_w = 5,0$.

earthquake occurred. The same census database was considered in other works, such as Zucconi, Ferlito, & Sorrentino [67,69], D'Amato et al. [14], Laguardia et al. [39]. The ISTAT census database, assumed in each municipality as reference, permits of knowing municipality-by-municipality only the material breakdown of buildings registered, while it does not report any other information (such as material type of horizontal and vertical structural elements, floor number, construction age) for defining typological classes similarly to the *AeDES* forms.

A municipality-by-municipality database completion including undamaged and not surveyed buildings may be conducted by comparing the buildings number having the AeDES form (i.e. surveyed after the 2009 L'Aquila earthquake) with the one reported in ISTAT [33] census database. In doing so, in each municipality the following Completeness $Ratio r_m$ may be considered [14]:

$$r_m = \frac{N_{m,AeDES}}{N_{m ISTAT}} \tag{4}$$

where m is the m-th municipality (1, ..., 95), $N_{m,AeDES}$ and $N_{m,ISTAT}$ is the buildings number surveyed with AeDES form (included within Da.D.O. database) and during the ISTAT census, respectively.

Basically, a perfect correspondence between buildings registered during the ISTAT [33] census having also an *AeDES* form would lead in each municipality to a completeness ratio r_m ideally equal to 1. To this scope Fig. 9a reports a histogram of r_m intervals found in the

municipalities analysed, while Fig. 9b illustrates the completeness ratios map. Contrary to what was expected, one may observe that in this case r_m reaches values greater than 1 in the zones around the seismic sequence epicentres, while far from the latter a r_m lower than 1 is obtained. These numerical inconsistencies are also found in other previous works, Dolce & Manfredi [19], Zucconi, Ferlito, & Sorrentino [67] and D'Amato et al., [14]. In particular, it is easy reasonable that in the municipalities where the earthquake occurred with a low intensity, almost of all undamaged buildings were hence not surveyed, so that we found $r_m < 1$ [14]. On the other hand, $r_m > 1$ may be very likely due to a different definition of "building" assumed by the two databases, and because of some building was not recorded during the ISTAT [33] census but surveyed with the AeDES form after L'Aquila 2009 earthquake [14]. This probably is due to the fact that some building was not accurately reported into the cadastral maps and, therefore, was not recorder into ISTAT census, contributing to the buildings number underestimation with respect to the AeDES database [67]. Lastly, it should be remembered that in this study the ISTAT [33] database is considered, since it is the closest database to the L'Aquila 2009 earthquake. Therefore, it could be possible that discrepancies between ISTAT [33] and AeDES database are given to the fact that some building after the L'Aquila 2009 seismic swarm was demolished and, consequently, not considered in the ISTAT census. However, this is still an open issue, needing to be investigated more in depth in the future.

In this study it is assumed that buildings not surveyed (i.e. without *AeDES* form) did not have any damage due to L'Aquila seismic sequence.

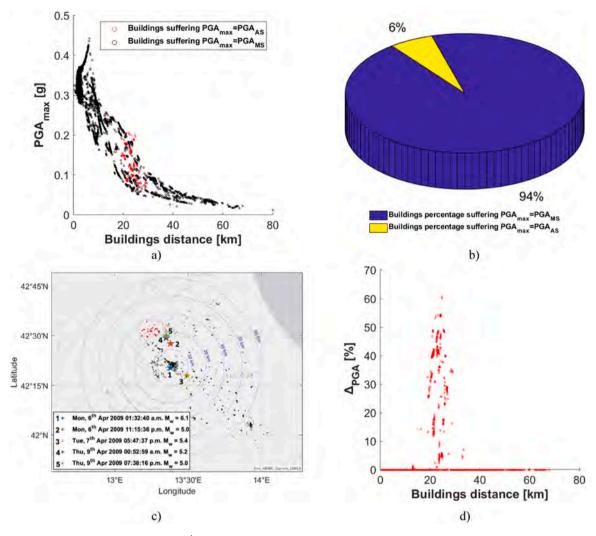


Fig. 8. (a) PGA values from the mainshock epicenter (6th April 2009, $M_w = 6.1$) recorded during the mainshock and the aftershocks; (b) Percent distribution of the maximum PGA occurred during the mainshock or aftershocks; (c) Residential buildings maps and distance from the mainshock epicenter; d) PGA percentage increment respect to the value recorded in the mainshock.

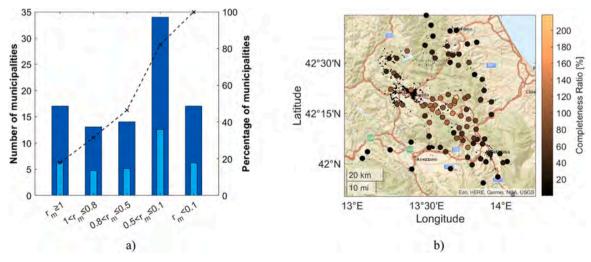


Fig. 9. (a) r_m intervals found in the 95 municipalities analyzed; (b) completeness ratios map.

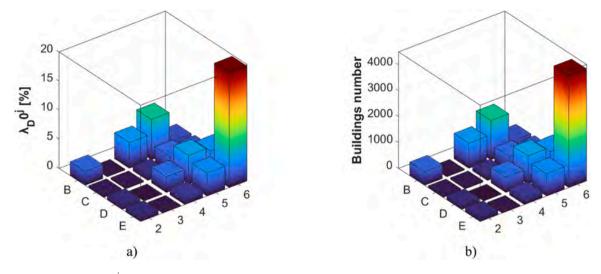


Fig. 10. MB:1H-1V. (a) λ_{D0}^{j} (in percentage) and (b) number of undamaged buildings added for all the structures typologies considered.

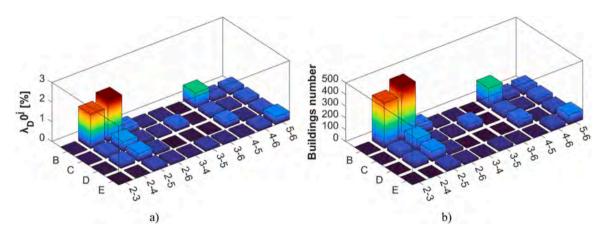


Fig. 11. MB:2H-1V. (a) λ_{D0}^{j} (in percentage) and (b) number of undamaged buildings added for all the structures typologies considered.

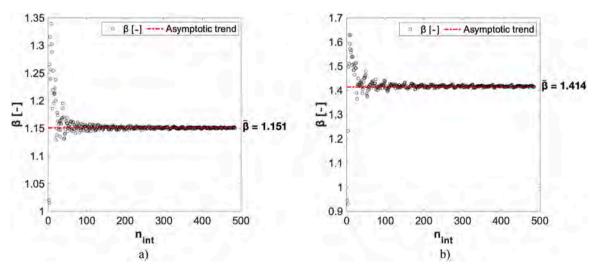


Fig. 12. Standard deviation of the *PGA* logarithmic values β . Masonry type a) 2C and b) 2D–4D.

Therefore, a D_0 level is assigned to these buildings. According to this assumption, in the municipalities where $r_m < 1$, the masonry residential buildings stock is completed as follows [59,60]:

$$N_{m,added}^{DO} = N_{m,ISTAT} - N_{m,AeDES}^{DO-DS}(m = 1, ..., 95)$$
(5)

where $N_{m.added}^{D0}$ is the undamaged buildings number added for completing

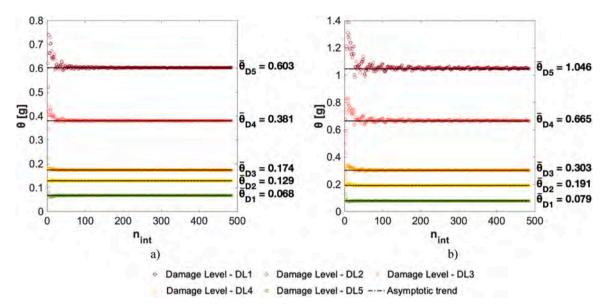


Fig. 13. Median of PGA values ϑ for different damages level. Masonry type (a) 2C and (b) 2D–4D.

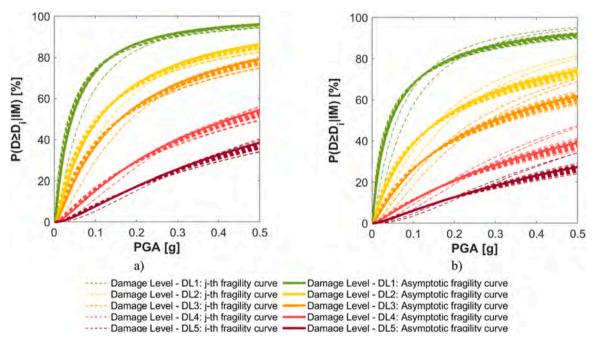


Fig. 14. Fragility curves obtained by varying $(\theta_{D1}, ..., \theta_{D5}, \beta)$ for several n_{int} . Masonry type (a) 2C and (b) 2D–4D.

the buildings stock in the m-th municipality, and $N_{m,AeDES}^{DO-DS}$ is the buildings number reported in the Da.D.O. database having an AeDES form. Hence, the total buildings number $N_{m.tot}$ is given by:

$$N_{m,tot} = N_{m,ISTAT} = N_{m,AeDES}^{D0-D5} + N_{m,added}^{D0}$$
 (6)

by assuming that in each municipality the buildings distribution by construction material, and in particular for masonry buildings considered in this study, is derived from ISTAT [33] census buildings stocks.

In accordance with the assumptions made, starting from the stock of $N_{AeDES}^{D0-D5} = \sum N_{m,AeDES}^{D0-D5} = 56.338$ masonry residential buildings surveyed with *AeDES* form, the completion procedure adopted provides $N_{added} = \sum N_{m,added}^{D0} = 21.955$, yielding to a completed buildings stock of $N_{m,tot} = \sum N_{m,tot} = 78.293$ buildings.

Unfortunately, the ISTAT [33] census database does not provide any

information on masonry structures typologies as appear in the *AeDES* form and reported in the Table 1, as possible combination between horizontal (indicated with a number from 1 to 6) and vertical structural elements (indicated with a letter from A to E). Hence, in order to obtain a hypothetical undamaged buildings breakdown according to *AeDES* form typologies, it is assumed that this unknown breakdown follows the known undamaged buildings breakdown observed from the *AeDES* forms. Therefore, in the *m-th* municipality the following expression is applied for calculating the added number of undamaged buildings (i.e. with D_0) $N_{madded}^{D0,j}$ for the j-th masonry structures typology (Table 1):

$$N_{m,added}^{D0,j} = \frac{\sum_{m=1}^{95} N_{m,AeDES}^{D0,j}}{\sum_{m=1}^{95} N_{m,AeDES}^{D0}} N_{m,added}^{D0} = \lambda_{D0}^{j} \bullet N_{m,added}^{D0}$$
 (7)

where $N_{m,added}^{DO}$ is the undamaged buildings number added by means of

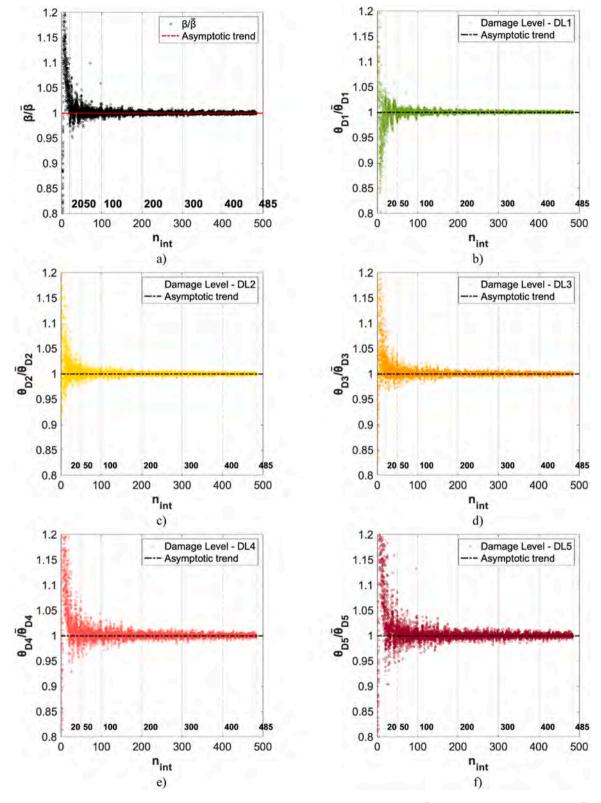


Fig. 15. Masonry residential buildings stock of L'Aquila 2009 (completed database). (a) Ratio $\beta/\overline{\beta}$; (b), (c), (d), (e) and (f) ratios $\vartheta_{Di}/\overline{\vartheta}_{Di}$.

Eq. 5; while $N_{m,AeDES}^{D0,j}$ and $N_{m,AeDES}^{D0}$ refer to the m-th municipality and correspond, respectively, to the undamaged buildings number belonging to the j-th masonry structure typology (Table 1), and to the undamaged buildings total number both with the AeDES form (in the case of the masonry residential buildings stock considered we found that $\sum_{m=1}^{95} N_{m,AeDES}^{D0} = 16.714$). λ_{D0}^{j} expresses, for the j-th masonry structure

typology, the ratio between the sums of $N_{m,AeDES}^{D0,j}$ and $N_{m,AeDES}^{D0}$ referred to all the municipalities, so that $\sum_j \lambda_{D0}^j = 1$. In the Eq. 7 the sums are extended to all the undamaged buildings of all the 95 municipalities considered because of it is assumed that in this way a better masonry structures typologies breakdown of undamaged buildings may be estimated. However, this aspect deserves to be investigated more in detail in

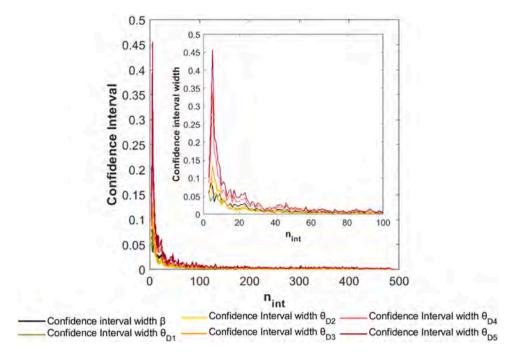


Fig. 16. Confidence Intervals of ratios $\theta_{Di}/\overline{\theta}_{Di}$ and $\beta/\overline{\beta}$ plotted in Fig. 15 at a 95% confidence level.

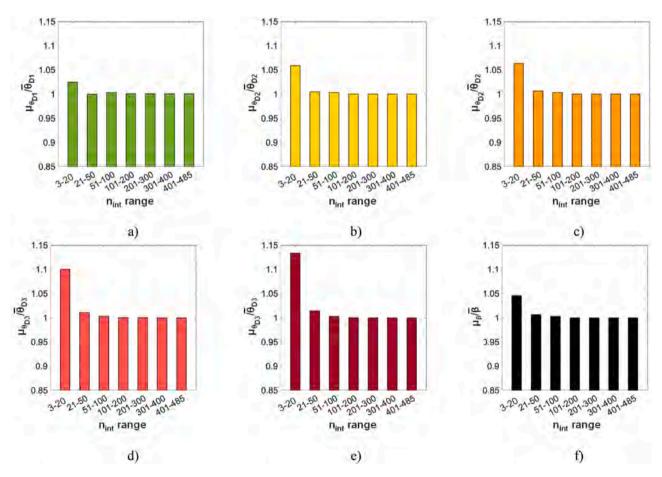


Fig. 17. Ratios (a) $\mu_{\theta_{D1}}/\overline{\theta}_{D1}$, (b) $\mu_{\theta_{D2}}/\overline{\theta}_{D2}$, (c) $\mu_{\theta_{D3}}/\overline{\theta}_{D3}$, (d) $\mu_{\theta_{D4}}/\overline{\theta}_{D4}$, (e) $\mu_{\theta_{D5}}/\overline{\theta}_{D5}$ and (f) $\mu_{\beta}/\overline{\beta}$ for several $n_{\rm int}$ ranges.

the future due to the uncertainties that this kind of estimation may imply. For completeness Fig. 10 and Fig. 11 report, according to the Eq. 7, for all masonry structures typologies of the Table 1 the ratio λ_{D0}^{j} (in

percentage) and the number of undamaged buildings added. In particular, Fig. 10 refers to case of MB:1H-1V (masonry residential buildings have one horizontal and one vertical structural element); whereas

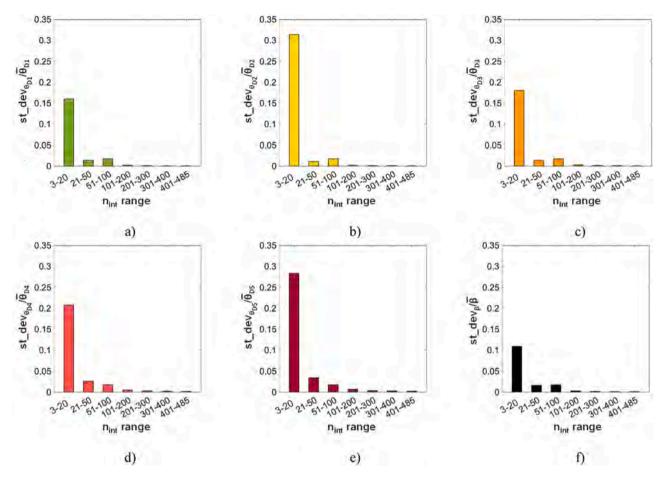


Fig. 18. Standard deviations (a) $st_dev_{\vartheta_D}/\bar{\vartheta}_{D1}$, (b) $st_dev_{\vartheta_D}/\bar{\vartheta}_{D2}$, (c) $st_dev_{\vartheta_D}/\bar{\vartheta}_{D3}$, (d) $st_dev_{\vartheta_D}/\bar{\vartheta}_{D4}$, (e) $st_dev_{\vartheta_D}/\bar{\vartheta}_{D5}$ and (f) $st_dev_{\vartheta}/\bar{\vartheta}$ for several n_{int} ranges.

Fig. 11 plots the results obtained with respect to the MB:2H-1V buildings.

The procedure proposed for database completion is easy to be implemented since it requires information available from the buildings already surveyed, and from Italian national census periodically performed on the buildings stock considered. Of course, it represents a first tentative of taking into account the undamaged and not surveyed residential buildings for deriving fragility curves that may be significative from a statistic point of view. In this way, the completion proposed permits of obtaining a breakdown of the masonry undamaged buildings (added) for all the structural typologies considered by the *AeDES* form (Table 1).

6. Sample partitioning for fragility curves fitting the observed seismic damage

As previously introduced, for fitting fragility curves to the observed seismic damage of a certain buildings stock, a sample partition in IM intervals is necessary having in general a constant amplitude. The j-th interval (bin) with limits $IM_j \pm \Delta IM/2$, includes the buildings seismic damage from D_0 to D_5 [5].

Once the buildings stock seismic damage is partitioned, the *MLE* method is applied in order to estimate the fundamental parameters $(\vartheta_1,\ldots,\vartheta_5,\beta)$ describing the fragility curves for any damage level (Eq. 3) [40,5,56]. Without any doubt, the partitioning is a crucial point since how to choose the intervals number $(n_{\rm int})$ and, consequently, their amplitude ΔIM influences the fundamental parameters estimation $(\vartheta_1,\ldots,\vartheta_5,\beta)$. For demonstrating this, a sensitivity analysis is performed in this study calculating the fundamental parameters by varying the IM intervals amplitude, by assuming in this case that IM corresponds to the

PGA. Numerical investigations are referred to several typologies of masonry residential buildings belonging to the L'Aquila 2009 buildings stock available within *Da.D.O.*, and completed as proposed in this study.

As example, Fig. 12 and Fig. 13 report the fundamental parameters obtained by referring to two different masonry typologies according to AeDES classification (Table 1), that are: type 2C, i.e. buildings with masonry of irregular texture and poor quality, with tie-rods and tiebeams; type 2D-4D, i.e. buildings with masonry of regular texture and good quality, with two horizontal structural elements: vaults and beam with deformable slabs, both without tie-rods and tie-beams. As for the two typologies here discussed, it results a sample of 548 buildings for type 2C, and of 285 buildings for type 2D-4D. These values are greater than an indicative lower bound of 200 buildings indicated in Rossetto et al. [48] for obtaining a theoretical acceptable sample size in fragility curves analysis. Numerical investigations are conducted by increasing the intervals number $n_{\rm int}$ down to about 0001 g obtaining $n_{\rm int} = 485$, since the maximum PGA for both the masonry typologies investigated is equal to 0485 g. More in detail, Fig. 12 reports as the standard deviation of the PGA logarithmic values β (Eq. 1) varies as n_{int} increases (i.e. the interval PGA amplitude reduces), by referring to the type 2C (Fig. 12a) and to type 2D-4D (Fig. 12b). Analogously, Fig. 13 plots the variability of PGA median values as n_{int} increases for type 2C (Fig. 13a) and for type 2D-4D (Fig. 13b). As one may easily note, in the masonry typologies considered the fundamental parameters $(\vartheta_1, ..., \vartheta_5, \beta)$ tend to stabilize as the interval number increases, reaching substantially an asymptotic value. In both the cases analysed β rapidly reduces its dispersion as n_{int} increases (Fig. 12), and tends to converge on the asymptotic values $(\overline{\beta})$ when $n_{\rm int}$ is higher than 100. Whereas, as for the fundamental parameter $(\vartheta_1, \dots, \vartheta_5)$ it is observed that they soon converge on the asymptotic value for a very small value of n_{int} only for damage level D_1 , D_2 and D_3

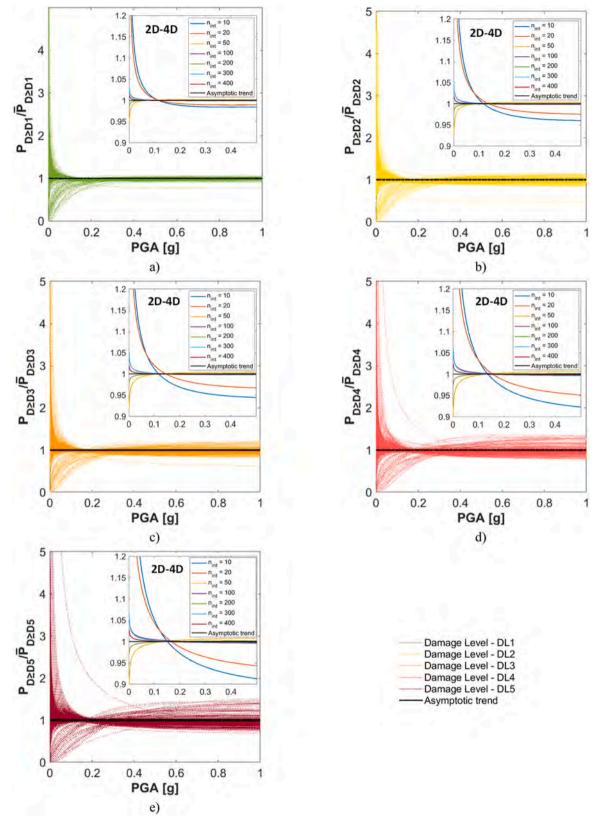


Fig. 19. Fragility curves ordinates ratios $P_{D \geq Di}/\overline{P}_{D \geq Di}$ for all the damage levels considered.

 $(\overline{\vartheta}_{D1}, \overline{\vartheta}_{D2}, \overline{\vartheta}_{D3})$. While, a more marked dispersion around the asymptotic values is observed in the case of D_4 and D_5 $(\overline{\vartheta}_{D4}, \overline{\vartheta}_{D5})$, stabilizing when $n_{\rm int}$ is higher than 100.

Finally, it is useful to understand how the fundamental parameters

variability reported in Fig. 12 and Fig. 13 reflect on the corresponding fragility curves. To this aim, Fig. 14 illustrates a set of fragility curves (D_1-D_5) for $type\ 2C$ (Fig. 14a) and $type\ 2D-4D$ (Fig. 14b), calculated for different values of $(\vartheta_{D1},\ldots,\vartheta_{D5},\beta|n_{int})$ each of which related to a specific

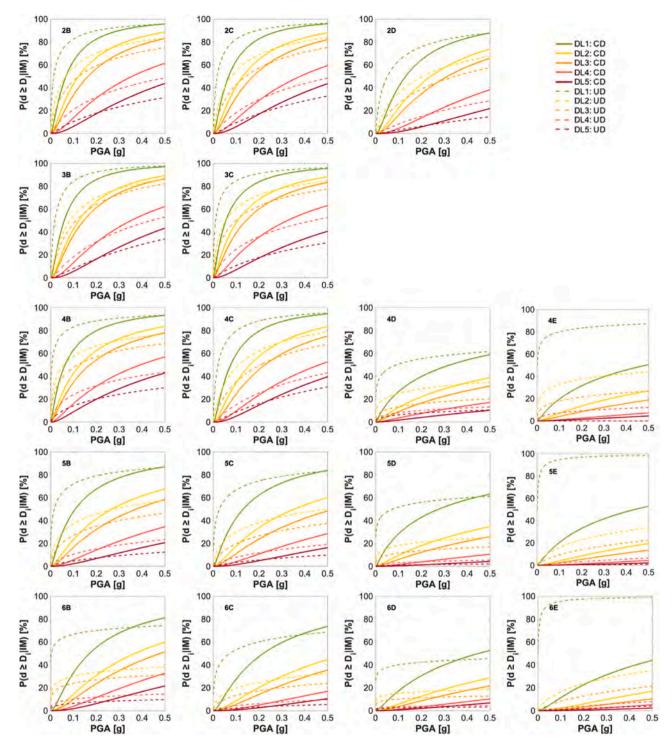


Fig. 20. MB:1H-1V. Typological fragility curves from type 2B to type 6E (Table 1).

 $n_{\rm int}$. In these graphs the thicker fragility curves indicate the ones calculated by referring to the asymptotic values highlighted in Fig. 12 and Fig. 13. As one may note the variability of $(\vartheta_{D1},\ldots,\vartheta_{D5},\beta|n_{\rm int})$ reflects, of course, on the fragility curves of Fig. 14, that is less relevant in the case of masonry *type 2C* (Fig. 14a) and, on the contrary, more pronounced in the case of masonry *type 2D–4D* (Fig. 14b). Therefore, it may be concluded that reliable fragility curves are obtained if a non-arbitrary *PGA* intervals number $(n_{\rm int})$ is chosen. In the cases analysed $n_{\rm int}$ results equal to about 100.

The fundamental parameters convergence discussed in detail for the masonry *types 2C* and *2D–4D* may be generalized for all other residential

masonry types considered in this study. This is proved in Fig. 15 plotting the dimensionless ratios $\vartheta_{Di}/\overline{\vartheta}_{Di}$ (i = 1, ..., 5) and $\beta/\overline{\beta}$ referred to all the Table 1 typologies where it has been possible to derive ϑ_{Di} and β for all the damage levels. The asymptotic values $\overline{\vartheta}_{Di}$ and $\overline{\beta}$ are generally found when 485 intervals are considered. As it is easy to note, although a certain dispersion is observed when the $n_{\rm int}$ is low, dimensionless ratios tend to the unity when $n_{\rm int}$ is 100 or higher, even if a monotonic convergence is not observed. Fig. 16 depicts an estimation of the interval width computed at 95% confidence level for each of the dimensionless ratios $\vartheta_{Di}/\overline{\vartheta}_{Di}$ (i = 1, ..., 5) and $\beta/\overline{\beta}$. The interval width is obtained as upper bound – lower bound, and plotted by varying $n_{\rm int}$. In this way it is

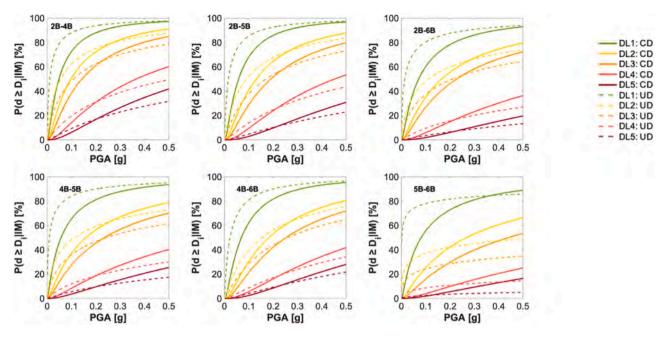


Fig. 21. MB:2H-1V. Typological fragility curves of type B (Table 1).

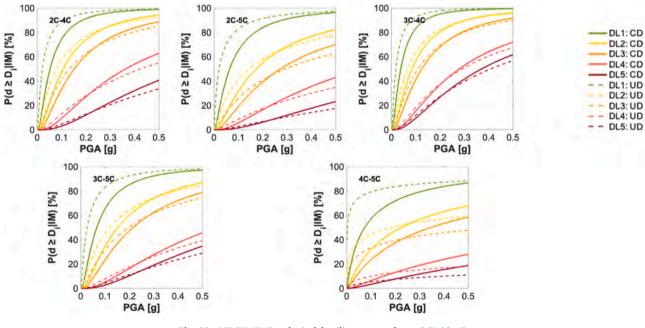


Fig. 22. MB:2H-1V. Typological fragility curves of $type\ C$ (Table 1).

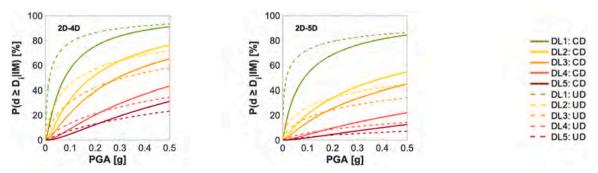


Fig. 23. MB:2H-1V. Typological fragility curves of type D (Table 1).

Table 4 *MB:1H-1V.* Fundamental parameters of fragility curves from *type 2B* to *type 6E* (Table 1).

| type | n, | $\overline{\vartheta}_{DI}$ [g] | $\overline{\vartheta}_{D2}$ [g] | $\overline{\vartheta}_{D3}$ [g] | $\overline{\vartheta}_{D4}$ [g] | $\overline{\vartheta}_{D5}$ [g] | β [-] |
|------|--------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|-------|
| 2B | 3.890 | 0,068 | 0,123 | 0,164 | 0,357 | 0,600 | 1,164 |
| 2C | 548 | 0,068 | 0,123 | 0,174 | 0,381 | 0,603 | 1,151 |
| 2D | 712 | 0,132 | 0,241 | 0,315 | 0,704 | 1,222 | 1,147 |
| 3B | 260 | 0,060 | 0,124 | 0,145 | 0,352 | 0,604 | 1,125 |
| 3C | 404 | 0,056 | 0,108 | 0,143 | 0,324 | 0,681 | 1,296 |
| 4B | 6.982 | 0,064 | 0,130 | 0,173 | 0393 | 0,640 | 1,378 |
| 4C | 1.254 | 0,077 | 0,161 | 0,226 | 0,463 | 0,682 | 1,172 |
| 4D | 2.228 | 0,326 | 0,854 | 1,240 | 2980 | 5,388 | 1,884 |
| 4E | 831 | 0,488 | 1,559 | 2,584 | 7,473 | 11,687 | 1,856 |
| 5B | 7.663 | 0,108 | 0,269 | 0,375 | 0,856 | 1,513 | 1,356 |
| 5C | 2.645 | 0,131 | 0,354 | 0,527 | 1,078 | 1,890 | 1,358 |
| 5D | 4.014 | 0,276 | 1,008 | 1,573 | 4,587 | 10,496 | 1,772 |
| 5E | 2.969 | 0,437 | 2,313 | 3,583 | 10,632 | 18,811 | 1,783 |
| 6B | 1.609 | 0,171 | 0,368 | 0,480 | 0,865 | 1,299 | 1,216 |
| 6C | 1.624 | 0,219 | 0,596 | 0,813 | 1,751 | 2,576 | 1,308 |
| 6D | 3.084 | 0,450 | 1,229 | 1,741 | 3,759 | 5,334 | 1,587 |
| 6E | 13.645 | 0,631 | 2,155 | 3,433 | 5,961 | 10,495 | 1,524 |

Table 5

MB:2H-1V. Fundamental parameters of fragility curves of type B (Table 1).

| type | n. | $\overline{\vartheta}_{DI}$ [g] | $\overline{\theta}_{D2}$ [g] | $\overline{\vartheta}_{D3}$ [g] | $\overline{\theta}_{D4}$ [g] | $\overline{\theta}_{D5}$ [g] | β [-] |
|-------|-------|---------------------------------|------------------------------|---------------------------------|------------------------------|------------------------------|-------|
| 2B-4B | 3.705 | 0,048 | 0,097 | 0,142 | 0,365 | 0,641 | 1,213 |
| 2B-5B | 3.782 | 0,058 | 0,130 | 0,190 | 0,452 | 0,890 | 1,156 |
| 2B-6B | 425 | 0,071 | 0,165 | 0,226 | 0,794 | 1,554 | 1,331 |
| 4B-5B | 1.207 | 0,057 | 0,159 | 0,234 | 0,710 | 1,280 | 1,426 |
| 4B-6B | 271 | 0,069 | 0,182 | 0,253 | 0,637 | 0,988 | 1,172 |
| 5B-6B | 308 | 0,081 | 0,267 | 0,439 | 1,354 | 2,124 | 1,487 |

Table 6

MB:2H-1V. Fundamental parameters of fragility curves of type C (Table 1).

| type | n. | $\overline{\vartheta}_{DI}$ [g] | $\overline{\vartheta}_{D2}$ [g] | $\overline{\vartheta}_{D3}$ [g] | $\overline{\vartheta}_{D4}$ [g] | $\overline{\vartheta}_{D5}$ [g] | β [-] |
|-------|-----|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|-------|
| 2C-4C | 481 | 0,052 | 0,106 | 0,152 | 0,363 | 0,630 | 0,983 |
| 2C-5C | 742 | 0,064 | 0,173 | 0,273 | 0,611 | 1,156 | 1,146 |
| 3C-4C | 246 | 0,038 | 0,084 | 0,124 | 0,279 | 0,371 | 1,003 |
| 3C-5C | 402 | 0,066 | 0,152 | 0,214 | 0,561 | 0,756 | 1,059 |
| 4C-5C | 283 | 0,074 | 0,224 | 0,344 | 1,354 | 2,278 | 1,719 |

Table 7

MB:2H-1V. Fundamental parameters of fragility curves of type D (Table 1).

| ty | pe | n. | $\overline{\vartheta}_{DI}$ [g] | $\overline{\vartheta}_{D2}$ [g] | $\overline{\vartheta}_{D3}$ [g] | $\overline{\vartheta}_{D4}$ [g] | $\overline{\vartheta}_{D5}$ [g] | β [-] |
|----|-----|-----|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|-------|
| 20 | -4D | 285 | 0,078 | 0,186 | 0,292 | 0,631 | 0,984 | 1,377 |
| 2D | –5D | 479 | 0,087 | 0,407 | 0,627 | 1,897 | 3,649 | 1,733 |

possible to note that the confidence interval width rapidly reduces to zero as n_{int} increases, despite the high confidence level (95%).

Fig. 17 and Fig. 18 illustrate, in a different way, what depicted in Fig. 15. In particular, Fig. 17a reports the ratio $\mu_{\theta_{D1}}/\bar{\vartheta}_{D1}$, where $\mu_{\theta_{D1}}$ is the mean of the fundamental parameters ϑ_{D1} (median value) calculated in each $n_{\rm int}$ range (bin) considered (such as 3–20, 21–50, 51–100, 101–200, 201–300, 301–400 and 401–485), and $\bar{\vartheta}_{D1}$ is the corresponding asymptotic value. Similarly, the ratios $\mu_{\vartheta_{D2}}/\bar{\vartheta}_{D2}$ - $\mu_{\vartheta_{D5}}/\bar{\vartheta}_{D5}$ of other damage levels are plotted in Fig. 17b-e. Finally, Fig. 17f reports the ratio $\mu_{\beta}/\bar{\beta}$, where μ_{β} is the mean of the fundamental parameters β (logarithmic standard deviation) calculated in each $n_{\rm int}$ range considered, and $\bar{\beta}$ is the asymptotic value found. Fig. 18a reports the ratio $st_dev_{\vartheta_{D1}}/\bar{\vartheta}_{D1}$, where $st_dev_{\vartheta_{D1}}$ is the standard deviation of the fundamental parameters ϑ_{D1} (median value) resulting in each $n_{\rm int}$ range (bin) considered. Analogously, Fig. 18b-e illustrate the ratios $st_dev_{\vartheta_{D2}}/\bar{\vartheta}_{D2}$ - $st_dev_{\vartheta_{D5}}/\bar{\vartheta}_{D5}$

respectively. Whereas, Fig. 18f shows the ratio $st_dev_{\beta}/\overline{\beta}$, where st_dev_{β} is the standard deviation of the fundamental parameters β (logarithmic standard deviation) calculated in each $n_{\rm int}$ range considered. It is easy to observe that, for all the masonry typologies considered, as the n_{int} increases the mean value of the ratios $\vartheta_{Di}/\overline{\vartheta}_{Di}$ and $\beta/\overline{\beta}$ converge to 1, whereas their standard deviations reduce to zero. This permits to generalize the results previously obtained for the two specific masonry residential typologies considered (masonry type 2C and 2D-4D, Fig. 12 through Fig. 14). Therefore, a rapid converge on the asymptotic values of the fundamental parameters ϑ_{Di} and β may be expected by increasing the PGA intervals number. Finally, Fig. 19 illustrates, for all typologies of Table 1, the ratios $P_{D>Di}/\overline{P}_{D>Di}$, where $P_{D>Di}$ is the fragility curve ordinate by referring to $(\vartheta_{D1},...,\vartheta_{D5},\beta|n_{\rm int})$, and $\overline{P}_{D\geq Di}$ the corresponding fragility curve ordinate referred to the asymptotic values $(\overline{\vartheta}_{D1}, \dots, \overline{\vartheta}_{D5},$ $\overline{\beta}$). For clarity also curves referred to only some n_{int} are reported in a different scale (such as 10, 20, 50, 100, 200, 300 and 400), too. For brevity, these graphs are illustrated by considering only the masonry residential typology 2D-4D. It is easy to note that, even if a monotonic convergence is not observed again, the ratios tend clearly to the unity, with a greater dispersion for low PGA values for all the damage levels.

7. Typological fragility curves proposed

In order to derive typological fragility curves for several residential masonry buildings typologies (according to the Table 1 classification), a municipality-by-municipality database completion of the buildings stock is applied, by means of the approach indicated in Sect. 5. The resulting fragility curves are plotted in Figs. 20–23, considering the fundamental parameters equal to the obtained asymptotic values $(\bar{\vartheta}_{D1}, \ldots, \bar{\vartheta}_{D5}, \bar{\beta})$ summarized in Tables 4–7.

It should be noted that in order to assign to a generic building one of the typologies considered in this study a building knowledge is necessarily required. This can be done through a building visual inspection, preceded by an interview with the owner, in order to find out information such as construction age, materials, structural type and the presence (or not) of interventions occurred over the years. Furthermore, if necessary, in situ investigations may be carried out, addressed to the acquisition of information necessary to be able to identify the typology consistent with one of those defined in Baggio et al. [4]. By the contrast, if some information is insufficient or missing to identify vertical and horizontal structural elements, a correct typology may not be assigned and, consequently, the building should be classified as "unidentified" (type A) within AeDES form.

More in detail, Fig. 20 and the Table 1 illustrates the fragility curves e fundamental parameters related to the MB:1H-1V (Table 1), respectively. Whereas, as for MB:2H-1V, three typologies of vertical structures are considered that are: $type\ B$ of Table 1 (masonry with irregular texture and poor quality without tie-rods and tie-beams), $type\ C$ (masonry with irregular texture and poor quality with tie-rods and tie-beams), and $type\ D$ (masonry with regular texture and good quality without tie-rods and tie-beams). They are illustrated, respectively, in Figs. 21–23 and Tables 5–7.

Lilliefors test is used to quantify the goodness of fit of the fragility curves for all the structural typologies considered [41]. This test is carried out to assess the acceptability of the lognormal distribution for a 95% confidence level as required by ATC-58 [42,43]. The D statistic is the Kolmogorov-Smirnov test parameter corresponding to the maximum of the absolute value of the differences between the empirical and theoretical function. The null hypothesis, H_0 , for the test is the decision on whether to accept or reject the hypothesis. The null hypothesis is accepted if D is less than or equal to Lilliefors test parameter D_{crit} at 5% significance level. The obtained results are presented in Table 8, and it is depicting that all the proposed fragility curves pass the Lilliefors test for all damage levels considered. The D statistic is performed by considering the asymptotic values of the fundamental parameters.

Table 8
Lilliefors test results based on asymptotic values.

| type | Damage D | 1 | Damage D | 2 | Damage D | 3 | Damage D | 4 | Damage D |) ₅ | H_0 |
|-------|----------|-------------------|----------|-------|----------|-------------------|----------|-------------------|----------|----------------|----------|
| | D | D _{crit} | D | Dcrit | D | D _{crit} | D | D _{crit} | D | D_{crit} | |
| 2B | 0,124 | 0,140 | 0,116 | 0,131 | 0,168 | 0,131 | 0,153 | 0,134 | 0,131 | 0,135 | Accepted |
| 2C | 0,125 | 0,138 | 0,111 | 0,122 | 0,122 | 0,123 | 0,126 | 0,144 | 0,130 | 0,164 | Accepted |
| 2D | 0,118 | 0,120 | 0,117 | 0,135 | 0,135 | 0,146 | 0,164 | 0,188 | 0,205 | 0,262 | Accepted |
| 3B | 0,185 | 0,188 | 0,161 | 0,176 | 0,150 | 0,176 | 0,201 | 0,207 | 0,189 | 0,251 | Accepted |
| 3C | 0,132 | 0,145 | 0,114 | 0,137 | 0,124 | 0,135 | 0,141 | 0,152 | 0,138 | 0,192 | Accepted |
| 4B | 0,137 | 0,164 | 0,164 | 0,164 | 0,140 | 0,164 | 0,153 | 0,167 | 0,166 | 0,167 | Accepted |
| 4C | 0,131 | 0,132 | 0,109 | 0,131 | 0,132 | 0,134 | 0,138 | 0,142 | 0,152 | 0,156 | Accepted |
| 4D | 0,070 | 0,146 | 0,109 | 0,150 | 0,107 | 0,156 | 0,171 | 0,173 | 0,168 | 0,196 | Accepted |
| 4E | 0,128 | 0,146 | 0,137 | 0,159 | 0,167 | 0,192 | 0,233 | 0,288 | 0,209 | 0,343 | Accepted |
| 5B | 0,121 | 0,144 | 0,129 | 0,140 | 0,132 | 0,144 | 0,132 | 0,146 | 0,143 | 0,152 | Accepted |
| 5C | 0,134 | 0,192 | 0,127 | 0,192 | 0,122 | 0,192 | 0,200 | 0,207 | 0,175 | 0,242 | Accepted |
| 5D | 0,132 | 0,207 | 0,181 | 0,213 | 0,179 | 0,213 | 0,221 | 0,233 | 0,234 | 0,262 | Accepted |
| 5E | 0,095 | 0,170 | 0,158 | 0,180 | 0,128 | 0,192 | 0,159 | 0,251 | 0,228 | 0,343 | Accepted |
| 6B | 0,102 | 0,113 | 0,103 | 0,121 | 0,123 | 0,127 | 0,109 | 0,170 | 0,130 | 0,188 | Accepted |
| 6C | 0,083 | 0,133 | 0,135 | 0,142 | 0,160 | 0,148 | 0,198 | 0,188 | 0,214 | 0,226 | Accepted |
| 6D | 0,122 | 0,161 | 0,153 | 0,170 | 0,137 | 0,173 | 0,200 | 0,207 | 0,235 | 0,242 | Accepted |
| 6E | 0,096 | 0,159 | 0,160 | 0,167 | 0,173 | 0,176 | 0,154 | 0,207 | 0,155 | 0,251 | Accepted |
| 2B-4B | 0,162 | 0,184 | 0,179 | 0,184 | 0,146 | 0,184 | 0,165 | 0,180 | 0,146 | 0,176 | Accepted |
| 2B-5B | 0,241 | 0,242 | 0,174 | 0,242 | 0,154 | 0,233 | 0,150 | 0,233 | 0,192 | 0,233 | Accepted |
| 2B-6B | 0,145 | 0,164 | 0,163 | 0,164 | 0,175 | 0,176 | 0,148 | 0,233 | 0,227 | 0,304 | Accepted |
| 4B-5B | 0,119 | 0,173 | 0,150 | 0,161 | 0,141 | 0,161 | 0,159 | 0,176 | 0,205 | 0,213 | Accepted |
| 4B-6B | 0,154 | 0,170 | 0,167 | 0,180 | 0,178 | 0,192 | 0,212 | 0,324 | 0,184 | 0,324 | Accepted |
| 5B-6B | 0,147 | 0,167 | 0,168 | 0,176 | 0,166 | 0,184 | 0,244 | 0,251 | 0,281 | 0,304 | Accepted |
| 2C-4C | 0,146 | 0,161 | 0,122 | 0,142 | 0,100 | 0,146 | 0,141 | 0,161 | 0,182 | 0,213 | Accepted |
| 2C-5C | 0,123 | 0,127 | 0,109 | 0,124 | 0,113 | 0,124 | 0,148 | 0,173 | 0,174 | 0,242 | Accepted |
| 3C-4C | 0,185 | 0,207 | 0,173 | 0,176 | 0,185 | 0,196 | 0,180 | 0,219 | 0,207 | 0,233 | Accepted |
| 3C-5C | 0,170 | 0,170 | 0,146 | 0,159 | 0,148 | 0,167 | 0,247 | 0,252 | 0,287 | 0,304 | Accepted |
| 4C-5C | 0,164 | 0,176 | 0,155 | 0,180 | 0,165 | 0,192 | 0,246 | 0,304 | 0,219 | 0,343 | Accepted |
| 2D-4D | 0,172 | 0,188 | 0,177 | 0,192 | 0,178 | 0,219 | 0,168 | 0,242 | 0,310 | 0,324 | Accepted |
| 2D-5D | 0,124 | 0,152 | 0,124 | 0,167 | 0,146 | 0,188 | 0,219 | 0,288 | 0,287 | 0,343 | Accepted |

For sake of completeness the fragility curves plotted in Figs. 20-23 refer to both the Completed Database (CD) according to the procedure proposed in this study (continuous lines in the graphs), and the Uncompleted Database (UD, dashed lines). One may note that the database completion leads to different fragility curves for all the typological classes considered. A significant scatter is obtained demonstrating the statistical importance of the undamaged (i.e., buildings with D_0) and not surveyed buildings when fragility curves are derived. The completion with undamaged buildings influences the fragility curves with respect to both the damage level and IM (in this case PGA). For all the structural typologies considered, it is noted that the fragility curves related to the damage level D_1 lead always to overestimate the exceedance probability if the *UD* is considered. This is due to the fact that when completion is applied to the stock considered, the undamaged buildings number increases (CD) and, therefore, the exceedance probability of the damage level D_1 tends to reduce with respect to the case when only surveyed buildings are considered (UD). For the others damage levels, this overestimation arises mainly for low PGA values. As the PGA increases the scatter between the UD and CD fragility curves tend to reduce, demonstrating that the completion for high damage level and high PGA values is not significant, since in these cases seismic damages surveyed are dominant and, therefore, the completion becomes less relevant.

8. Conclusions

In this paper, typological fragility curves have been proposed for existing residential masonry buildings, through the macro-seismic approach by examining damage observed on a stock of 56.338 buildings affected by L'Aquila 2009 seismic sequence. They refer to the possible combinations of vertical and horizontal structural elements as contemplated within the *AeDES* form (Table 1). All the curves the fragility curves proposed, according to the *ATC-58* criterion, pass the *Lilliefors test* for all damage levels considered with a 95% confidence level.

The issues investigated may be useful in order to reduce uncertainties

in deriving fragility curves. A criterion has been proposed for completing the buildings stock considered with undamaged and not surveyed buildings, that can be easily extended to any type of buildings stock. This aspect becomes particularly important in the municipalities far from the epicentre, where usually post-earthquake surveys are not uniformly conducted. Therefore, there is a lack of information on a large number of undamaged buildings, due to the fact the *AeDES* form for these buildings is not available. Comparisons among the completed and uncompleted database highlight the statistical importance of undamaged buildings added. In particular, it has been noted that for all typologies considered, the completion is particularly important for low values of damage levels and of *PGA*. While, it tends to decrease as the *PGA* increases, showing that for high damage levels and high *PGA*, database completion becomes less relevant.

Moreover, investigations have been carried out in order to evaluate the influence of the buildings stock damage partitioning on the typological fragility curves. The results obtained have demonstrated that the fundamental parameters derived by means of MLE method strictly depends on the PGA internals amplitude. Even if a non-monotonic converge is observed, they tend to stabilize as the intervals number $(n_{\rm int})$ increases, converging on the asymptotic values. In the cases analysed, fundamental parameters values close to the asymptotic ones have been obtained when $n_{\rm int}$ is greater than 100.

Finally, in future in continuity with this work, uncertainties on the *PGA* estimation derived from shake-maps will be taken into account, in order to improve the fragility curves proposed. Moreover, other *IMs* will be also considered (*PGV*).

CRediT authorship contribution statement

All authors contributed equally to this manuscript.

Declaration of Competing Interest

The authors declare that they received no funds, grants or other

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Data availability

Data will be made available on request.

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