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Proceedings of the 13th ERME Topic Conference  
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Slovakia**

Hans-Georg Weigand, Ana Donevska-Todorova, Eleonora Faggiano, Paola Iannone, Janka Medová, Michal Tabach, Melih Turgut

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CONSTANTINE  
THE PHILOSOPHER  
UNIVERSITY  
IN NITRA



ERME Topic Conference  
Mathematics Education in the Digital Age

**MEDA3**

## Mathematics Education in Digital Age 3

Proceedings of the **13th ERME Topic Conference (ETC13)**  
held on 7 – 9 September 2022 in Nitra, Slovakia



Edited by:

Hans-Georg Weigand

Ana Donevska-Todorova; Eleonora Faggiano; Paola Iannone

Janka Medová; Michal Tabach; Melih Turgut

Nitra 2022

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### **Mathematics Education in Digital Age 3 (MEDA3)**

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Editors: Hans-Georg Weigand, Ana Donevska-Todorova, Eleonora Faggiano,  
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Faculty of Natural Sciences and Informatics  
Constantine the Philosopher University in Nitra

**MEDA3**

# Mathematics Education in Digital Age 3

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Nitra, 2022

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