

Numerical modelling of landslide-tsunami propagation in a wide range of idealised water body geometries

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Abstract

Large landslide-tsunamis are caused by mass movements such as landslides or rock falls impacting into a water body. Research of these phenomena is essentially based on the two idealised water body geometries (i) wave flume (2D, laterally confined wave propagation) and (ii) wave basin (3D, unconfined wave propagation). The wave height in 2D and 3D differs by over one order of magnitude in the far field. Further, the wave characteristics in intermediate geometries are currently not well understood. This article focuses on numerical landslide-tsunami propagation in the far field to quantify the effect of the water body geometry. The hydrodynamic numerical model SWASH, based on the non-hydrostatic non-linear shallow water equations, was used to simulate approximate linear, Stokes, cnoidal and solitary waves in 6 different idealised water body geometries. This includes 2D, 3D as well as intermediate geometries consisting of “channels” with diverging side walls. The wavefront length was found to be an excellent parameter to correlate the wave decay along the slide axis in all these geometries in agreement with Green’s law and with diffraction theory in 3D. Semi-theoretical equations to predict the wave magnitude of the idealised waves at any desired point of the water bodies are also presented. Further, simulations of experimental landslide-tsunami time series were performed in 2D to quantify the effect of frequency dispersion. This process may be negligible for solitary- and cnoidal-like waves for initial landslide-tsunami hazard assessment but becomes more important for Stokes-like waves in deeper water. The findings herein significantly improve the reliability of initial landslide-tsunami hazard assessment in water body geometries between 2D and 3D, as demonstrated with the 2014 landslide-tsunami event in Lake Askja.

Keywords: Landslide-tsunamis, SWASH, diffraction theory, frequency dispersion, nonlinear waves, wave propagation

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1. Introduction

1.1. Overview

Tsunamis generated by landslides are serious hazards in reservoirs (Fuchs et al., 2011; Panizzo et al., 2005), lakes (Fuchs and Boes, 2010; Gylfadóttir et al., 2017), fjords (Harbitz et al., 2014) and the sea (Watt et al., 2012; Watts et al., 2005). In this work the term “landslide” applies to mass movements such as unstable soil, rock falls, calving icebergs and snow avalanches and the term “tsunami” specifies (low frequency) waves in water bodies such as lakes, reservoirs, fjords and the sea hereafter (Liu et al., 2005).

One of the most destructive recorded landslide-tsunami was caused by an approximately $270 \times 10^6 \text{ m}^3$ large landslide impacting into the Vajont reservoir in Italy in 1963. The generated wave overtopped the dam crest and flooded the valley resulting in approximately 2000 casualties (Panizzo et al., 2005). Landslide-tsunamis generated by submarine mass failures include the Papua New Guinea tsunami in 1998 where a wave of 10 m height resulted in over 2100 human losses (Synolakis et al., 2002). The 2014 landslide-tsunami in Lake Askja in Iceland is a more recent example. An approximately $20 \times 10^6 \text{ m}^3$ large landslide generated a 50 m large tsunami inundating the shoreline up to 80 m (Gylfadóttir et al., 2017). On a global scale, potential landslide-tsunamis need to be assessed quite frequently considering regions such as China with over 87000 reservoirs (Liu et al., 2013), Norway with 1190 fjords (Wikipedia, 2018) and many new hydropower projects worldwide. Such past and potential future events highlight the need for reliable landslide-tsunami hazard assessment methods.

1.2. The effect of the water body geometry

Landslide-tsunamis are most reliably investigated in case specific water bodies given that the geometry and bathymetry may significantly affect the wave characteristics (Bellotti et al., 2012; Heller et al., 2012; Winckler and Liu, 2015). For generic studies, however, it is common practice to use idealised geometries. These are flume geometries (2D) and rarer basin geometries (3D) with a uniform water depth. Related geometries reflecting these idealisations can indeed be found in nature; Fig. 1a shows an example of a 2D geometry if the iceberg detaches over the entire width. The wave propagates in the direction of the main axis of the water body with the coordinate x from the landslide impact and with the water body side angles at $\theta = 0^\circ$. Fig. 1b shows the Chahalis lake representing a 3D geometry where the waves propagate with semi-circular fronts defined with the radial distance r and a propagation angle γ from the slide impact with $\theta = 90^\circ$.

The decay of the leading wave with distance from the landslide impact zone has been studied extensively in both 2D and 3D revealing a very different behaviour. For 2D geometries Kranzer and Keller (1959) found theoretically, that $H(x)/h \propto (x/h)^{-1/3}$, with H being the wave height and h the water depth, and laboratory experiments showed ranges between $H(x)/h \propto (x/h)^{-1/5}$ and $H(x)/h \propto (x/h)^{-0.3}$ (Heller and Hager, 2010; Heller and Spinneken, 2013;

45 Wiegel et al., 1970). Studies conducted in 3D found values between $H(r)/h \propto$
 46 $(r/h)^{-2/3}$ and $H(r)/h \propto (r/h)^{-1}$ (Huber and Hager, 1997; Panizzo et al., 2005;
 47 Slingerland and Voight, 1979). According to these relationships, a wave with
 48 $H/h = 0.100$ in 2D reduces to $H = 0.034$ at $x/h = 35$, using $H(x)/h \propto (x/h)^{-0.3}$
 49 and in 3D to 0.003 at $r/h = 35$ by using $H(r)/h \propto (r/h)^{-1}$. This over an order
 50 of magnitude difference has been confirmed experimentally by Heller and Spin-
 51 neken (2015). The same authors also confirmed that the landslide-tsunami wave
 52 type changes in function of the geometry; not all of the wave types observed in
 53 2D (commonly linked to the theoretical wave types Stokes, cnoidal, solitary and
 54 bores (Heller and Hager, 2011)) are observed in 3D.

55 The decay in 2D is due to two different phenomena if bottom friction is ex-
 56 cluded; frequency dispersion (Brühl and Becker, 2018) and wave breaking which
 57 is sometimes present during tsunami generation and/or propagation. In geome-
 58 tries more diverging than 2D also the contribution of the lateral energy spread
 59 is present.

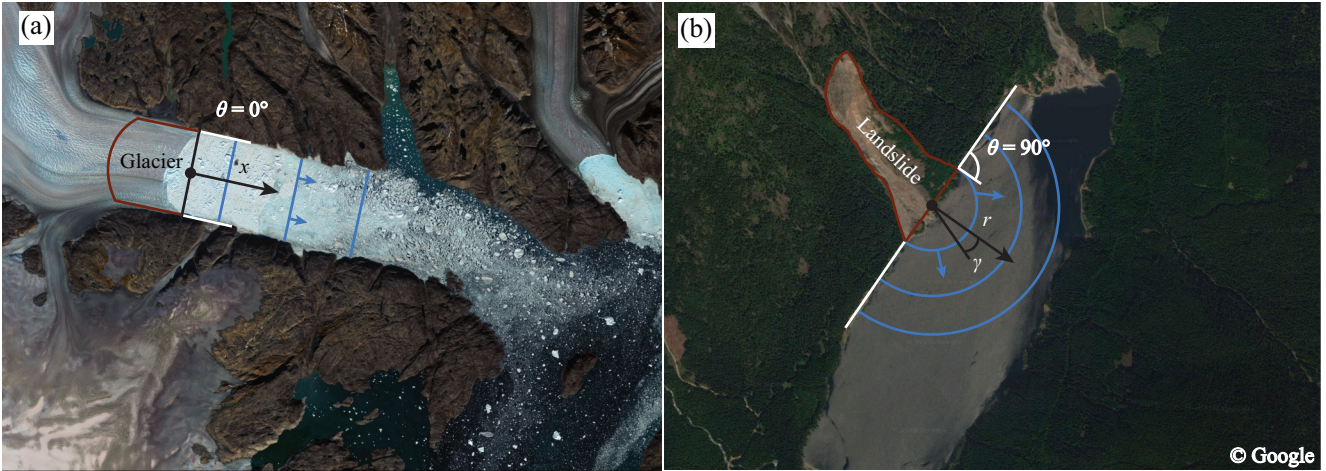


Figure 1: Landslide-tsunami settings represented by idealised geometries: (a) Heleim Glacier representing a 2D geometry (contains modified Copernicus Sentinel data, 2016, processed by Pierre Markuse) and (b) 2007 Chehalis lake case representing a 3D geometry (adapted from Google maps).

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62 Most studies involving the effect of the water body geometry were aimed at
 63 relating landslide-tsunami parameters in 3D to 2D. Submarine landslides were
 64 investigated by Jiang and LeBlond (1994) who found that the difference be-
 65 tween waves in 3D and 2D geometries is affected by the ratio b/l_s , where b is
 66 the slide width and l_s is the landslide length along its main axis, and Watts
 67 et al. (2005) who provide relations between tsunamis in 2D and 3D based on b
 68 and the maximum tsunami wavelength L_M .

69 Using subaerial landslides, Heller et al. (2009) proposed an empirical method
70 to link the wave characteristics in 3D to 2D based on the impulse product pa-
71 rameter P (Heller and Hager, 2010). The wave heights H at $x/h = r/h = 5$
72 were thereby assumed to be identical in both geometries based on observations
73 of Huber (1980) (follow-up research showed that this assumption is sometimes
74 very rough, see Heller and Spinneken, 2015). Beyond this position different de-
75 cays were defined for H based on Heller and Hager (2010) in 2D and Huber and
76 Hager (1997) in 3D.

77 Since these studies focus all on 2D and/or 3D only, the understanding of
78 landslide-tsunamis in intermediate geometries is limited. The pioneer study in-
79 vestigating an intermediate geometry was Chang et al. (1979) generating solitary
80 waves in a flume with walls at an angle of $\theta = 1.1^\circ$. These authors found that
81 Green’s law can be applied for $x/h < 40$. However, Green’s law was found to
82 have limited applicability for solitary and solitary-like waves for more extremely
83 diverging flumes (Heller et al., 2012) if the width of the diverging channel is used
84 in Green’s law.

85 Heller et al. (2012) experimentally investigated for the first time landslide-
86 tsunamis in different water body geometries with $\theta = 0$ (2D), 15, 30, 45, 60, 75
87 and 90° (3D). They found that the wave heights in the far field in intermediate
88 geometries were closer to the ones observed in 3D than in 2D. They further
89 highlighted the need to study the effect of the water body geometry in more
90 detail with different slide characteristics, wave types and larger water depths to
91 avoid scale effects (Heller, 2011; Heller et al., 2008).

92 This was later addressed (Heller and Spinneken, 2015) with a new set of
93 laboratory experiments in 2D and 3D with tsunamis measured up to a distance
94 of $x/h = r/h = 35$. The authors presented a novel method to transform wave
95 parameters (wave height, amplitude and period) from 2D to 3D for a range of
96 block slide characteristics. Intermediate geometries with $\theta = 7.5, 15, 30$ and 45°
97 were then purely numerically addressed with Smoothed Particle Hydrodynamics
98 (SPH) (Heller et al., 2016). This provided new physical insight into the effect of
99 the water body geometry for propagation distances $r/h \leq 7.5$. Larger distances
100 could not be investigated due to the large computational cost of SPH.

101 Fig. 2 shows a scheme of the division between the wave generation and wave
102 propagation zones of a landslide-tsunami. The wave generation zone (dashed
103 area), with coordinate system x and (r, γ) from the slide impact, is where the
104 momentum transfer between the landslide and water occurs (Mulligan and Take,
105 2017; Zitti et al., 2016). This zone is excluded from this study ensuring that the
106 tsunamis are reasonably stable in the simulations. Two new sets of coordinate
107 systems $x' = x + d_M$ and $(r' = r + d_M, \gamma')$ with d_M as the coupling distance
108 (Section 3.2) are also chosen to define the wave propagation zone considered in
109 the present study.

110 Herein, the landslide widths in all geometries are defined as the finite wave
111 source width in 2D in order to relate the findings from all geometries to 2D.
112 In 2D it is possible to quantify the effect of free components travelling with
113 their own celerity (this process is referred hereafter as frequency dispersion) on
114 waves generated by a landslide rather than idealised waves. Comparison with

115 laboratory experiments (Heller and Hager, 2011) will help to reveal this effect
 116 for each wave type. However, in the intermediate and 3D geometries this is not
 117 possible as lateral energy spread (i.e. diffraction) is present. Therefore, due to
 118 the non-linearity of the problem, it is not possible to separate the contribution
 119 of the lateral energy spread from that of frequency dispersion.

120 Because the wave source used is of finite width, diffraction theories (Carr
 121 and Stelzriede, 1952; Lamb, 1945; Morse and Rubenstein, 1938; Penney et al.,
 122 1952) could be used to validate the numerical simulations of this study. These
 123 theories are formulated to calculate the wave propagation of a linear wave be-
 124 hind a gap. This problem shows similarities with landslide-tsunamis with the
 125 slide, i.e. a wave source, of width corresponding to the gap width. Only the
 126 solution of Carr and Stelzriede (1952) is considered herein because the validity
 127 range of this theory is compatible with landslide-tsunamis ($b'/L \leq 0.5$) and it
 128 depends on both r' and γ' .

129 When idealised waves were considered, wave trains, rather than wave pack-
 130 ets were simulated. This was done for two reasons: first this is more similar to
 131 actual tsunami propagation and, second, it avoids spurious numerical solutions
 132 due to propagation of isolated waves or packets in still water. Finally, this study
 133 excludes shore and other depth related effects such as reflection and depth trap-
 134 ping of the tsunami (Bellotti et al., 2012) and edge waves (Couston et al., 2015;
 135 Heller and Spinneken, 2015; Romano et al., 2013) which in combination with
 136 the impact on the coast may alter the tsunami characteristics.

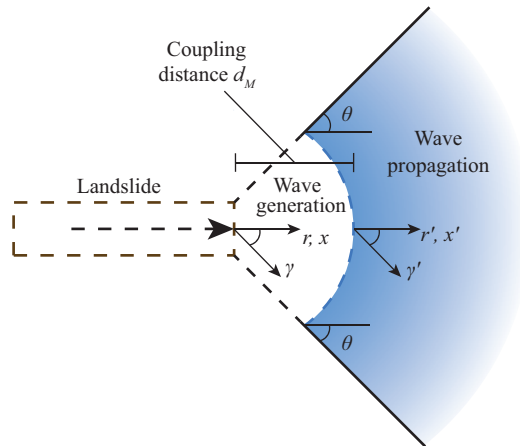


Figure 2: Scheme of the wave generation and propagation zones.

137 1.3. Numerical modelling

138 Subaerial landslide-tsunamis are challenging for numerical modelling. To
 139 overcome the difficulty in simulating wave generation and far field propagation
 140 at the same time, these two processes are usually divided using two numeri-
 141 cal methods that are subsequently coupled (Abadie et al., 2012; Tan et al.,

142 2018). Suitable options for the wave propagation are NHWAVE (Ma et al.,
 143 2012), FUNWAVE-TVD (Shi et al., 2012), XBeach (Roelvink et al., 2010) and
 144 SWASH (Zijlema et al., 2011).

145 SWASH, which is based on the non-hydrostatic Non-Linear Shallow Wa-
 146 ter Equations (NLSWEs), was chosen in the present study. SWASH is able to
 147 simulate frequency dispersion accurately with a small number of layers (e.g. 2)
 148 by using a compact difference scheme, and can be run in parallel. SWASH has
 149 also been successfully coupled with SPH for wave propagation from off- to on-
 150 shore (Altomare et al., 2015) and to study hypothetical landslide-tsunamis at
 151 Es Vedrà, offshore Ibiza (Tan et al., 2018).

152 1.4. Aims and structure

153 The present study aims to:

- 154 • Enhance the physical understanding and modelling of the effect of the wa-
 155 ter body geometry on tsunami propagation based on numerical modelling
 156 of approximate linear, Stokes, cnoidal and solitary waves in 2D, 3D and
 157 intermediate water body geometries,
- 158 • Provide insight on the effect of frequency dispersion on landslide-tsunamis,
- 159 • Provide new semi-theoretical equations accounting for the effect of the
 160 water body geometry to support landslide-tsunami hazard assessment.

161 The remainder of this article is organised as follows. In Section 2 the theoret-
 162 ical background of SWASH, the numerical setup, the boundary conditions and
 163 the calibration and validation are described. The wave propagation in idealised
 164 geometries for both idealised and real (dispersive) waves, the wave height de-
 165 cay and the lateral wave energy spread are presented in Section 3 along with
 166 semi-theoretical equations. In Section 4 the results are analysed and the 2014
 167 landslide-tsunami case in Lake Askja is used as computational example. Finally,
 168 Section 5 highlights the main conclusions and future work.

169 2. Methodology

170 2.1. SWASH

171 SWASH v4.01 (Stelling and Duinmeijer, 2003; Stelling and Zijlema, 2003;
 172 Zijlema and Stelling, 2005; Zijlema et al., 2011) was used in the present study.
 173 Only the governing equations used to solve the equations in 2D and 3D geome-
 174 tries, where a regular grid is used, are presented hereafter for simplicity. For
 175 the remaining intermediate geometries the equations are solved for a curvilinear
 176 grid.

177 SWASH solves the depth averaged non-hydrostatic NLSWEs with the conti-
 178 nuity and momentum equations written as

$$\frac{\partial \eta}{\partial t'} + \frac{\partial d\bar{u}}{\partial x'} + \frac{\partial d\bar{v}}{\partial y'} = 0 \quad (1)$$

$$\frac{\partial \bar{u}}{\partial t'} + \bar{u} \frac{\partial \bar{u}}{\partial x'} + \bar{v} \frac{\partial \bar{u}}{\partial y'} + g \frac{\partial \eta}{\partial x'} + \frac{1}{d} \int_{-h}^{\eta} \frac{\partial q}{\partial x'} dz' + c_f \frac{\bar{u} \sqrt{\bar{u}^2 + \bar{v}^2}}{d} = \frac{1}{d} \left(\frac{\partial d \tau_{x'x'}}{\partial x'} + \frac{\partial d \tau_{x'y'}}{\partial y'} \right) \quad (2)$$

$$\frac{\partial \bar{v}}{\partial t'} + \bar{u} \frac{\partial \bar{v}}{\partial x'} + \bar{v} \frac{\partial \bar{v}}{\partial y'} + g \frac{\partial \eta}{\partial y'} + \frac{1}{d} \int_{-h}^{\eta} \frac{\partial q}{\partial y'} dz' + c_f \frac{\bar{v} \sqrt{\bar{u}^2 + \bar{v}^2}}{d} = \frac{1}{d} \left(\frac{\partial d \tau_{y'x'}}{\partial x'} + \frac{\partial d \tau_{y'y'}}{\partial y'} \right) \quad (3)$$

179 where t' is the time, x' , y' and z' are the coordinates located at the mean still wa-
 180 ter level (SWL), $h(x', y')$ is the still water depth, $\eta(x', y', t')$ is the water surface
 181 elevation from the SWL and $d = h + \eta$ is the total water depth. \bar{u} and \bar{v} are the
 182 depth-averaged flow velocities in the two main directions. $\tau_{x'x'}$, $\tau_{x'y'}$, $\tau_{y'x'}$ and
 183 $\tau_{y'y'}$ are the horizontal turbulent stresses, c_f is the bottom friction coefficient
 184 defined by Manning's formula (Zijlema et al., 2011) and g is the gravity accel-
 185 eration. $q(x', y', z', t')$ is the non-hydrostatic pressure term of the total pressure
 186 p_t defined as (Zijlema and Stelling, 2005)

$$p_t = g(\eta - z') + q = p_h + q \quad (4)$$

187 where p_h is the hydrostatic pressure. Eqs. (1) to (3) were expanded in Stelling
 188 and Zijlema (2003) to the multi-layer case applied herein. The computation of
 189 the integral of the non-hydrostatic pressure gradient in Eqs. (2) and (3) is in-
 190 troduced in Zijlema et al. (2011), where the free surface boundary condition
 191 of the non-hydrostatic pressure is $q|_{\eta} = 0$ and at the bottom it is defined by
 192 applying the Keller-Box method. Then, the vertical velocities at the free surface
 193 w_s and at the bottom w_b are introduced with the momentum equation along
 194 the vertical direction. Here, the vertical acceleration is defined at every time
 195 step from the non-hydrostatic pressure. Finally, combining the vertical momen-
 196 tum equations with the non-hydrostatic pressure equation at the bottom and
 197 using the kinematic bottom boundary condition $w_b = -\bar{u} \partial h / \partial x' - \bar{v} \partial h / \partial y'$, the
 198 conservation of local mass results as

$$\frac{\partial \bar{u}}{\partial x'} + \frac{\partial \bar{v}}{\partial y'} + \frac{w_s - w_b}{d} = 0 \quad (5)$$

199 Eq. (5) closes the system of equations and allows, together with the boundary
 200 conditions, to solve Eqs. (1) to (3).

201 Time integration is carried out with the explicit method relying on the
 202 Courant-Friedrichs-Lewy (CFL) condition and the wave celerity that is avail-
 203 able in SWASH. Here only the condition for 2D simulations is illustrated as the
 204 most relevant one. The Courant number C_r is defined as

$$C_r = \Delta t' \left(\sqrt{gd} + \sqrt{u^2 + v^2} \right) \sqrt{\frac{1}{\Delta x'^2} + \frac{1}{\Delta y'^2}} \leq 1 \quad (6)$$

205 where $\Delta x'$ and $\Delta y'$ are the distances between two grid points in the x' and y'
 206 directions. To calculate the time step, a minimum and maximum C_r threshold

207 can be applied in the simulation in order to accurately control the convergence
 208 of the solution.

209 *2.2. Numerical setup*

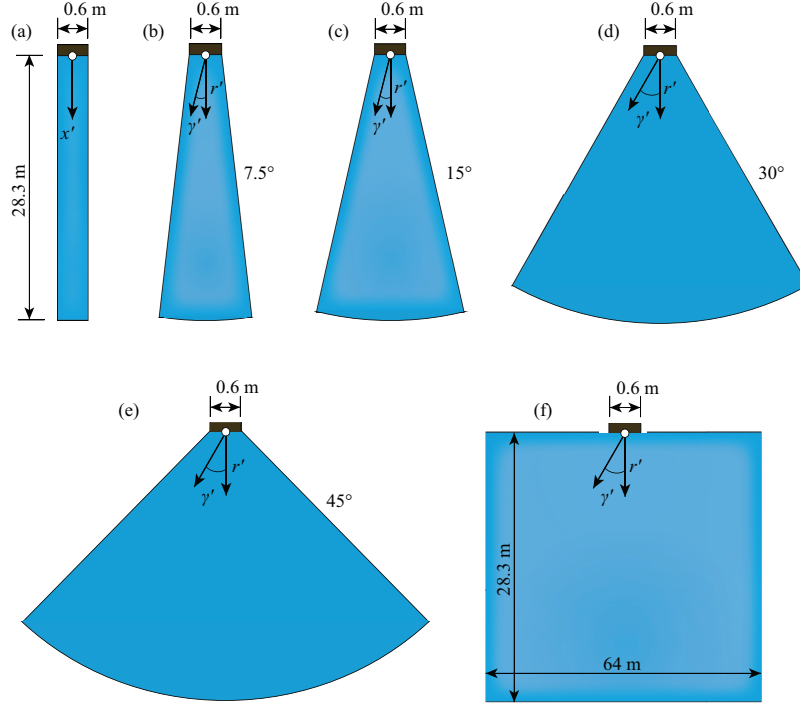


Figure 3: Investigated water body geometries in the far field modelled with SWASH: (a) 2D ($\theta = 0^\circ$), (b) $\theta = 7.5^\circ$, (c) $\theta = 15^\circ$, (d) $\theta = 30^\circ$, (e) $\theta = 45^\circ$ and (f) 3D ($\theta = 90^\circ$, the horizontal dimension is reduced in scale in this sketch due to lateral space constraint). The grey sections are the wave generation zones between the near and far fields.

210 The numerical domains used here cover the range from 2D to 3D (Fig. 3),
 211 based on the geometries used in Heller et al. (2016). The 2D geometry (Fig. 3a)
 212 consists of a 28.3 m long and 0.6 m wide flume while the 3D geometry (Fig.
 213 3b) spans a domain of 28.3 m \times 64.0 m. Intermediate geometries are defined
 214 using divergent side walls with angles of $\theta = 7.5, 15, 30$ and 45° (Fig. 3b-e).
 215 Geometries with $\theta > 45^\circ$ were excluded as previous research (Heller et al., 2012;
 216 Heller and Spinneken, 2015) showed no substantial differences of the maximum
 217 wave parameters in these geometries in relation to the 3D case. The basin width
 218 of these intermediate geometries is increasing with $0.6 + (2r'\tan\theta)$ m. Each
 219 intermediate geometry was modelled with a rounded downwave boundary with
 220 radius $r' = 28.3$ m to allow for a more even distribution of the cells in this zone.

221 The bathymetry was flat for all investigated cases and numerical wave gauges
 222 were placed at the relative distances and angles shown in Table 1.

Table 1: Locations of the numerical wave gauges.

Geometry	Relative distance x'/h or r'/h (-)	Wave propagation angle γ' ($^\circ$)
2D	3.0, 5.0, 7.5, 10.0, 15.0, 22.5, 35.0	0.0°
7.5°	3.0, 5.0, 7.5, 10.0, 15.0, 22.5, 35.0	$0.0^\circ, \pm 7.5^\circ$
15.0°	3.0, 5.0, 7.5, 10.0, 15.0, 22.5, 35.0	$0.0^\circ, \pm 7.5^\circ, \pm 15.0^\circ$
30.0°	3.0, 5.0, 7.5, 10.0, 15.0, 22.5, 35.0	$0.0^\circ, \pm 7.5^\circ, \pm 15.0^\circ, \pm 22.5^\circ, \pm 30.0^\circ$
45.0°	3.0, 5.0, 7.5, 10.0, 15.0, 22.5, 35.0	$0.0^\circ, \pm 7.5^\circ, \pm 15.0^\circ, \pm 22.5^\circ, \pm 30.0^\circ, \pm 37.5^\circ, \pm 45.0^\circ$
3D	3.0, 5.0, 7.5, 10.0, 15.0, 22.5, 35.0	$0.0^\circ, \pm 7.5^\circ, \pm 15.0^\circ, \pm 22.5^\circ, \pm 30.0^\circ, \pm 37.5^\circ, \pm 45.0^\circ, \pm 52.5^\circ, \pm 60.0^\circ, \pm 67.5^\circ, \pm 75.0^\circ, \pm 82.5^\circ$

223 The 2D and 3D geometries were defined with a regular Cartesian grid while
 224 the intermediate ones were defined with an orthogonal curvilinear grid created
 225 in the RGFRID v5.0 of the Delft3D software suite. These grids were then
 226 exported and reformatted using MATLAB to create input files readable by
 227 SWASH. The coordinate system for the grid creation was defined with $x' = 0$
 228 at the wave generation boundary with positive values in the main wave propa-
 229 gation direction. The origin in the y' -direction was defined at the centre of the
 230 wave source. The wave source in all domains was 0.6 m wide. For the results,
 231 polar coordinates (r', γ') with the origin at the centre of the wave source was
 232 used, with r' as the radial distance and γ' as the wave propagation angle with
 233 the results interpolated from the grid nodes.

234 Furthermore, the calibration was performed using a water depth of 0.6 m in
 235 all geometries based on the experiments of Heller and Hager (2011). The nu-
 236 merical code was compiled with the Intel compiler 2017 and Intel-MPI libraries
 237 for the use with multiple processors using the Message Passing Interface (MPI)
 238 protocol. The model divides the computational domain in subdomains to solve
 239 the equations with multiple cores. A stripwise decomposition method along the
 240 y' -axis was chosen. Other methods (orthogonal recursive bisection and stripwise
 241 along the x' -direction) resulted in inconsistencies in the solutions. The Univer-
 242 sity of Nottingham High Performance Computing (HPC) cluster Minerva was
 243 used to perform the simulations. A simulation time of 60 s in the 3D geometry
 244 with a grid resolution of $\Delta x' = \Delta y' = 2.5$ cm took approximately 35 hours of
 245 real time using 40 Central Processing Unit (CPU) cores and 10 GB of random
 246 access memory.

247 2.3. Boundary conditions

248 All tests for the calibration and validation of the model were performed by
 249 providing time series of linear waves as boundary conditions, allowing for a di-
 250 rect comparison with diffraction theory. A wave height of $H = 0.040$ m, a water
 251 depth of $h = 0.600$ m and a wave period of $T = 0.876$ s were used resulting in
 252 a wavelength of $L = 1.19$ m according to linear theory (Table 2). These con-
 253 ditions result in approximate linear waves. The first waves were disregarded in
 254 the analysis to include only steady wave heights.

255 Previous studies (e.g. Heller and Hager, 2011; Panizzo et al., 2005) showed
 256 that different slide scenarios lead to different wave types and decay character-
 257 istics. For this reason, after calibration and validation, the non-linear Stokes
 258 (Fenton, 1985), cnoidal (Fenton, 1999) and solitary waves (Boussinesq, 1872)
 259 were also reproduced and analysed herein. All wave parameters are summarised
 260 in Table 2 with a as the amplitude and c as the celerity. Bores were excluded
 261 because it is unlikely that they are observed in geometries other than 2D (Heller
 262 and Spinneken, 2015). Note that in the following the definition $H = a + a_t$ ap-
 263 plies, which reduces for linear waves to $H = 2a$, with a_t as the wave trough.
 264 The conditions for each wave type presented in Figs. 4 (Stokes-like waves), 6
 265 (cnoidal-like waves) and 8 (solitary-like waves) of Heller and Hager (2011) were
 266 reproduced by using the measured wave parameters in the corresponding wave
 267 theory. A time series of the water surface was calculated for each wave type
 268 and used as input for SWASH over a finite wave generation boundary $b' = 0.6$
 269 m. The wave velocity at the boundary was solved by SWASH as previous work
 270 showed the accuracy of this approach (Ruffini et al., 2019). A ramping up func-
 271 tion was added to smooth the initiation of the simulations to avoid numerical
 272 instabilities.

Table 2: Wave theories used in this study with the wave parameters measured in Heller and Hager (2011).

Wave theory	h (m)	H (m)	T (s)	L (m)	a (m)	c (m/s)
Linear	0.600	0.040	0.876	1.190	-	-
5 th order Stokes (Fenton, 1985)	0.600	0.100	1.000	1.530	-	-
5 th order cnoidal (Fenton, 1999)	0.300	0.155	1.740	2.830	0.110	1.630
1 st order solitary (Boussinesq, 1872)	0.300	0.159	-	2.823	0.159	1.969

273 The wave generation boundary was defined through a segment at $x' = 0$ m
 274 using a weakly reflective boundary condition (Blayo and Debreu, 2005). This
 275 formulation assumes a wave direction perpendicular to the boundary with an
 276 incident velocity \bar{u}_i defined by

$$\bar{u}_i = \pm \sqrt{\frac{g}{d}}(2\eta_i - \eta) \quad (7)$$

277 including the surface elevation signal of the incident wave η_i . In addition, all
 278 the lateral walls are represented by closed boundaries with zero flux velocity
 279 (Stelling and Zijlema, 2003). To avoid wave reflection from the downwave end
 280 of the domain, a sponge layer (Dingemans, 1997) with a length of at least 3
 281 times L was used in all geometries and additional lateral sponge layers were
 282 used in the 3D geometry (Fig. 4).

283 Finally, for the bottom friction a formulation based on Manning’s roughness
 284 coefficient n was chosen to compute the bottom friction coefficient c_f as

$$c_f = \frac{n^2 g}{d^{1/3}} \quad (8)$$

285 In the present study, $n = 0.009 \text{ s/m}^{1/3}$ for glass was chosen for all geometries
 286 to mimic the 2D experimental conditions in Heller and Spinneken (2015).

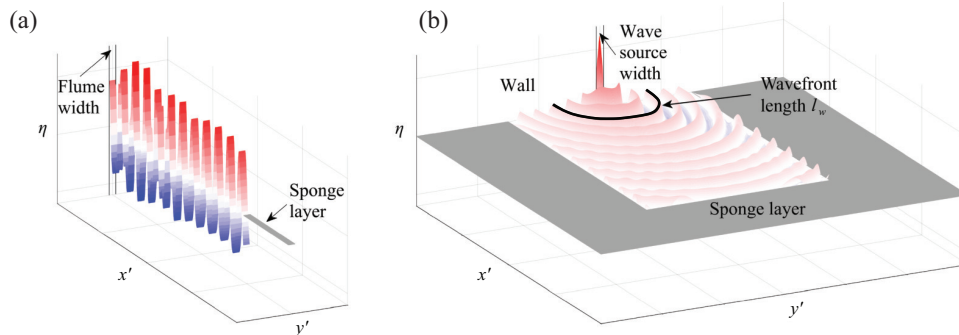


Figure 4: Three-dimensional schema of waves in (a) 2D and (b) 3D.

287 2.4. Calibration and validation

288 The calibration was performed to optimise the computational grids. The
 289 grids followed the Deltares (2018) guidelines with respect to orthogonality,
 290 smoothness, aspect ratio and minimum number of grid per wavelength. The
 291 orthogonality defines the difference of the angles between crossing grid lines
 292 from 90° where zero corresponds to orthogonal. This value was less than 0.04
 293 everywhere in the computational domains. The smoothness parameter defines
 294 the variation in size of two adjacent cells and a value of ≤ 1.1 was used. Fur-
 295 thermore, the aspect ratio takes the difference in length between the opposing
 296 sides of a cell into account. Negligible differences in the rate of convergence of
 297 the solution were noted with maximum ratio in the order of 10 at the wave
 298 generation boundary as the values rapidly decrease with distance from the wave
 299 source. The number of grid points per wavelength was at least 45. This is a finer
 300 resolution than in van Vledder and Zijlema (2014) who used 25 grid points per
 301 wavelength resulting in good agreement with theory in SWASH for diffraction
 302 at a semi-infinite breakwater.

303 The 3D geometry with approximate linear waves was used to investigate the
 304 convergence for $\Delta x' = \Delta y' = 2.5, 5.0$ and 10.0 cm and the symmetry (Appendix
 305 A) of the solution. Approximate linear waves were used as they resulted in the
 306 smallest number of grid points per L among the wave types considered in this
 307 study. Fig. 5 shows the water surface at $r'/h = 3.0$ and 35.0 for all chosen grid
 308 resolutions indicating convergence for 5.0 cm. The final resolution was set to
 309 2.5 cm to also satisfy the minimum value of grid points per L . SWASH matches
 310 higher order dispersion relations depending on the number of layers over the
 311 water depth. Higher values of kh , with k as the wave number, require a larger
 312 number of layers which shows indirectly the importance of wave dispersion for
 313 different kh values. 2 layers were chosen which results in a maximum error of 1%
 314 with $kh \leq 7.7$ (SWASH, 2016). Linear and Stokes waves were simulated using
 315 an higher order upwind discretisation scheme for the vertical advection term

316 of the \bar{u} -momentum equation, while the default 1st order upwind scheme was
 317 used for cnoidal and solitary waves. This was only necessary to reduce numerical
 318 dissipation, observed in the Stokes and linear wave propagation for the default
 319 scheme, particularly in 2D (SWASH, 2016).

320 A further validation was performed with the diffraction theory of Morse and
 321 Rubenstein (1938), by solving the application derived for water waves by Carr
 322 and Stelzriede (1952). This theory was chosen as it includes the variability of
 323 the solution with γ' and it applies to $b'/L \leq 0.5$, which is compatible with most
 324 landslide-tsunamis. The results in 3D for the approximate linear waves are compared
 325 to this theory for validation, as the diffraction theory is based on linear
 326 waves. The comparison is shown in Section 3.1.2 and the computation of the
 327 diffraction theory is explained in Appendix B.

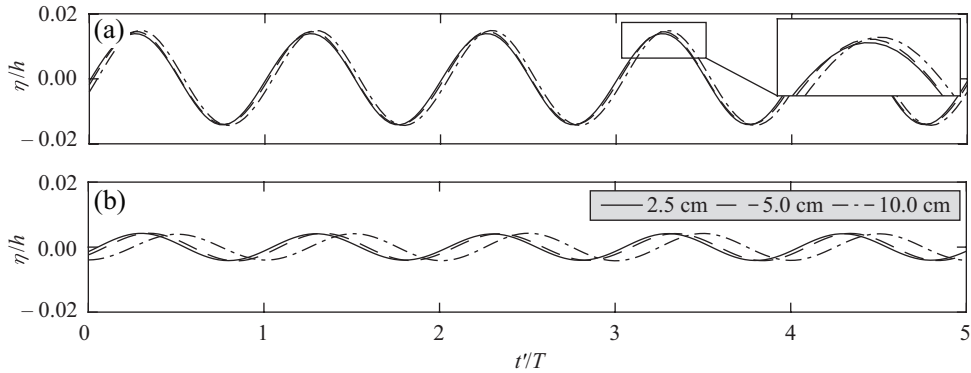


Figure 5: Wave profile convergence tests for approximate linear waves in the 3D geometry at
 (a) $r'/h = 3.0$ and (b) $r'/h = 35.0$.

328 3. Results

329 3.1. Idealised waves

330 3.1.1. Water surface time series

331 η for all idealised wave types was investigated in all geometries. Figs. 6, 7 and
 332 8 show the relative water surface elevation η/h over $5T$ at 4 different r'/h . The
 333 profiles shown in Fig. 6 are obtained for approximate linear waves in deep water
 334 with $h/L = 0.50$ and a weak non-linearity $H/h = 0.067$. Fig. 6 shows how the
 335 water body geometry affects the waves. By comparing the wave profiles in 2D
 336 to the ones in the 7.5° geometry at $r'/h = 3.0$ (Fig. 6a) only a relatively small
 337 difference is observed. This ratio progressively increases also with the angle θ
 338 resulting in the smallest waves in 3D. The ratio of the wave heights between 2D
 339 and all other geometries also progressively increases with relative distance (Fig.
 340 6b,c). At $r'/h = 35$ (Fig. 6d) the ratio between the waves in the 2D and 7.5°
 341 geometries is a factor of 3.2 and between 2D and 3D even a factor of 7.8.

342

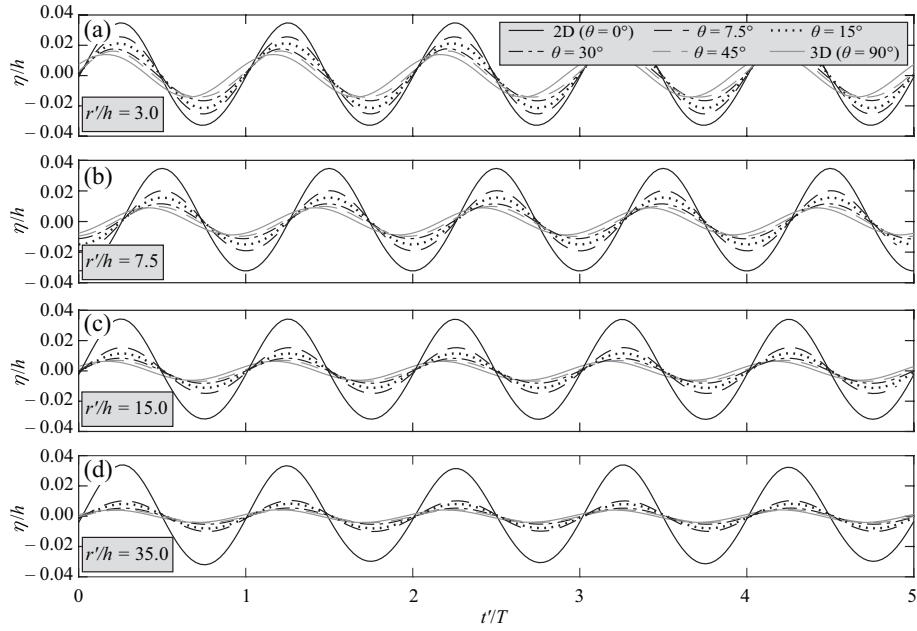


Figure 6: Relative water surface elevation η/h versus time normalised with the wave period t'/T for linear wave input in all geometries at different relative distances r'/h .

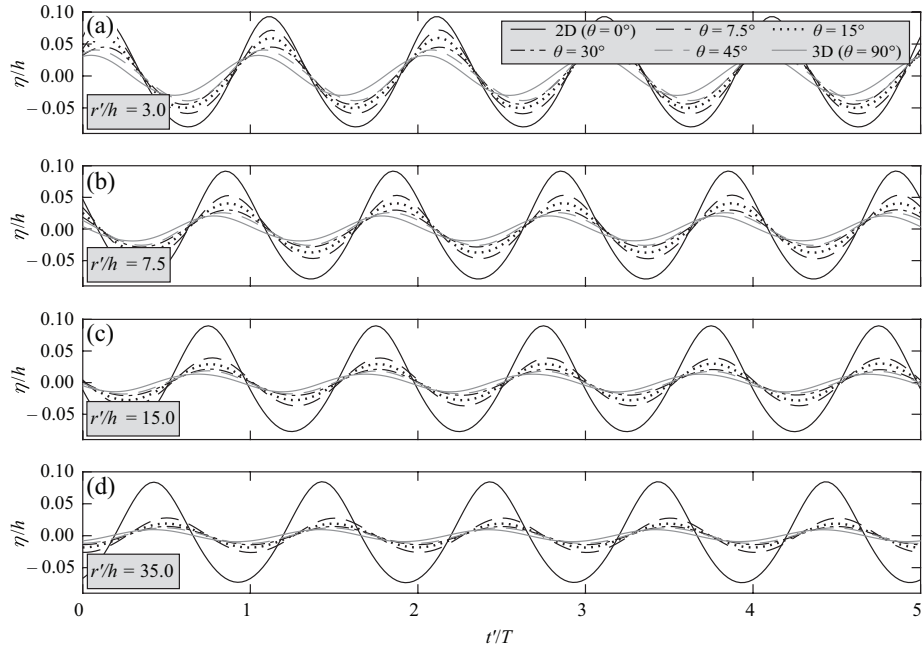


Figure 7: Relative water surface elevation η/h versus time normalised with the wave period t'/T for 5th order Stokes waves in all geometries at different relative distances r'/h .

343 Water surface time series for Stokes waves characterised by a ratio $h/L =$
344 0.39 are shown in Fig. 7 at $r'/h = 3.0, 7.5, 15.0$ and 35.0 . The Stokes wave
345 heights in Fig. 7d show differences of a factor of 2.8 between the 2D and 7.5°
346 geometry and 8.4 between 2D and 3D. The simulated cnoidal waves are shown
347 in Fig. 8 with $h/L = 0.10$, which propagate in shallower water than Stokes
348 waves. At $r'/h = 3.0$ (Fig. 8a) in the geometry $\theta = 15^\circ$ a secondary peak
349 in the wave troughs starts to develop which becomes larger with increasing θ . This
350 is associated with frequency dispersion resulting in an additional shorter wave
351 as shown in Fig. 8b-d with a different celerity relative to the primary wave.
352 At $r'/h = 35$ all the dominant waves, except the one in 2D, show a decrease
353 in celerity with decreasing wave height. In Fig. 8d the ratio between the wave
354 heights between the 2D and $\theta = 7.5^\circ$ geometry is 2.5 and between 2D and 3D
355 it is 6.5, which is smaller than for Stokes waves (Fig. 7).

356

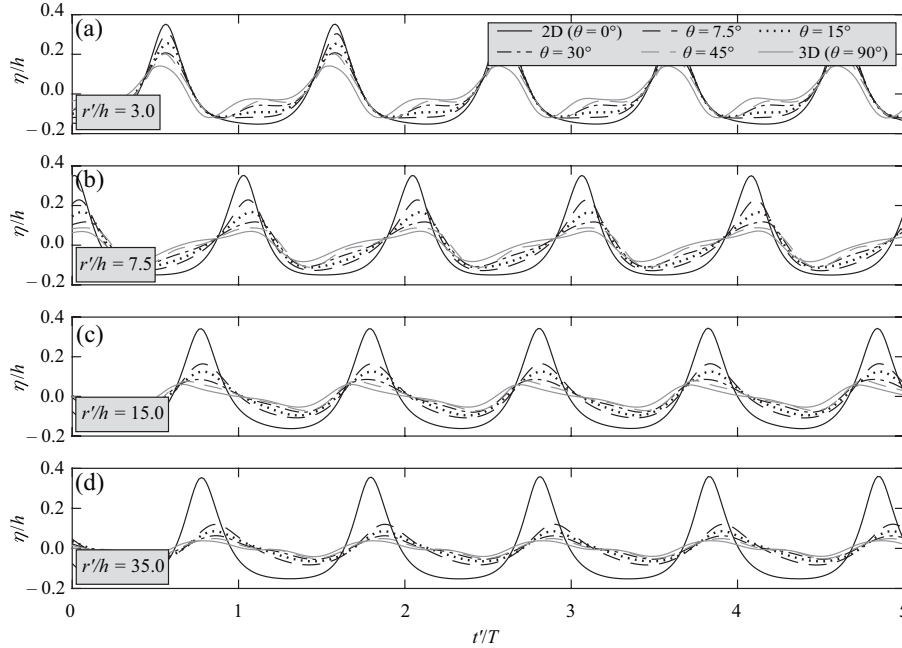


Figure 8: Relative water surface elevation η/h versus time normalised with the wave period t'/T for 5th order cnoidal waves in all geometries at different relative distances r'/h .

357 The results for the solitary waves are shown in Fig. 9. The solitary wave
358 profile is preserved at all relative distances in 2D. In all other geometries an
359 increasing tail in both amplitude and length is formed at $r'/h = 3.0$. Further,
360 the wave profile ratio between 2D and 3D at $r'/h = 35.0$ is a factor of 7.0
361 matching the results of Heller and Spinneken (2015). The ratio between a and
362 a_t is clearly changing with r'/h affecting the main wave characteristics. For the
363 wave in 3D the ratios a/a_t decrease from 2.3 at $r'/h = 3.0$ to 1.1 at $r'/h = 35.0$

364 (Fig. 9d). For the other geometries at $r'/h = 35.0$ the ratios a/a_t are 3.8 for 7.5° ,
 365 2.6 for 15° , 1.8 for 30° and 1.5 for 45° . For comparison, at $r'/h = 3.0$ the ratios
 366 are $a/a_t = 11.8, 8.2, 6.0$ and 4.5 for $\theta = 7.5^\circ, 15^\circ, 30^\circ$ and 45° respectively, with
 367 an almost constant difference of 3 times the values found at $r'/h = 35.0$. This
 368 shows that the waves approach the value $a/a_t = 1$, which is characteristic for
 369 linear waves, with both increasing θ and distance. This illustrates that the water
 370 body geometry not only affects the wave decay but also the wave non-linearity.

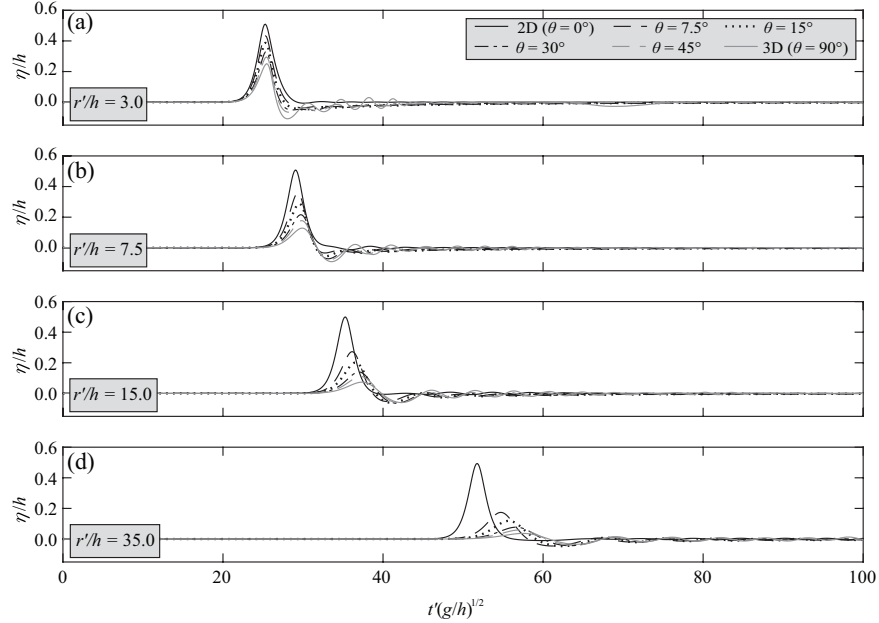


Figure 9: Relative water surface elevation for 1st order solitary waves in all geometries at different relative distances r'/h .

371 3.1.2. Wave height decay

372 The wave height H was calculated as the average over $5T$ (apart from the
 373 solitary wave). Values were calculated for all wave types and geometries at the
 374 locations shown in Table 1. Fig. 10 shows H/h for cnoidal waves over the relative
 375 distance for each geometry for $\gamma' = 0^\circ$. This clearly confirms the increasing
 376 decay of H with θ as highlighted in Section 3.1.1. The wavefront length l_w was
 377 identified as an excellent parameter to link the wave decay of the idealised waves
 378 across all water body geometries. The waves propagate with semi-circular fronts
 379 from the source. For a linear wave $Ec_g l_w = \text{constant}$, E being the mean energy
 380 density per unit area and c_g being the group velocity. Given that h is constant
 381 in all simulations the previous relationship reduces to $El_w = \text{constant}$. In addition,
 382 if the source width b' is relatively small, it can also be approximated as a line.

383 The values of l_w are then calculated for the numerical results as

$$l_w(r', \theta) = b' + 2r'\theta_{rad} \quad (9)$$

384 with the radial distance r' and the water body side angle θ_{rad} in radians. The
 385 resulting values based on Eq. (9) are shown in Table C.1 for each wave type.
 386 This parameter l_w normalised with the water depth h (i.e. l_w/h) is used to
 387 correlate H/h for all idealised wave types in Fig. 11.

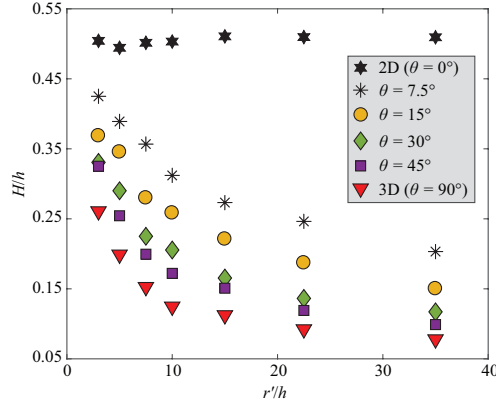


Figure 10: Relative wave height H/h decay with relative radial distance r'/h for the 5th order cnoidal waves in all geometries.

388 Fig. 11 shows H/h versus l_w/h for all wave types with the wave heights in
 389 different geometries highlighted with different markers. The diffraction theory
 390 from Carr and Stelzriede (1952) using Eq. (B.2) is plotted as a dashed black
 391 line. Furthermore, Green's law was included as

$$H(r', \theta) = H(r' = 0, \theta = 0^\circ) \left(\frac{b'}{l_w(r', \theta)} \right)^{1/2} \left(\frac{h(r' = 0)}{h(r')} \right)^{1/4}, \quad (10)$$

392 where $H(r', \theta)$ is the wave height in function of r' , $l_w(r', \theta)$ and $h(r')$ are the
 393 associated wavefront length and water depth, respectively. $H(r' = 0, \theta = 0^\circ)$ is
 394 the wave height at the source in 2D and b' is the source width. In the idealised
 395 geometries $h(r')$ is constant, such that the last term on the right-hand side
 396 of Eq. (10) reduces to 1. This equation can easily be applied by known wave
 397 characteristics at the source in 2D. The results for each wave type are then
 398 tested with the normalised Root Mean Square Error

$$nRMSE = \frac{\sqrt{\frac{1}{N} \sum_i^N (y_{pred,i} - y_{num,i})^2}}{(y_{num,max} - y_{num,min})} \quad (11)$$

399 where $y_{pred,i}$ is the i -th sample of the predicted parameter and $y_{num,i}$ is the
 400 corresponding numerical value. N is the number of considered samples, $y_{num,max}$

401 and $y_{num,min}$ are respectively the maximum and the minimum numerical values
 402 in the range considered ($nRMSE = 0$ represents perfect agreement). A similar
 403 equation to Eq. (10) can be obtained for the linear wave amplitude (Green,
 404 1838) by replacing H with the positive wave amplitude a in Eq. (10) resulting
 405 in

$$a(r', \theta) = a(r' = 0, \theta = 0^\circ) \left(\frac{b'}{l_w(r', \theta)} \right)^{1/2} \left(\frac{h(r' = 0)}{h(r')} \right)^{1/4}. \quad (12)$$

406
 407 Note that Eq. (12) will be applied to non-linear waves as a simplification
 408 hereafter. Fig. 11a shows that all H/h for approximate linear waves in all ge-
 409 ometries, apart from 3D, collapse on one curve corresponding to Green's law.
 410 Diffraction theory (Appendix B) under-predicts the wave height decay in the
 411 intermediate geometries but perfectly agrees with the wave heights observed in
 412 3D, given that this theory is based on linear waves for very similar 3D conditions
 413 (Section 1.2).

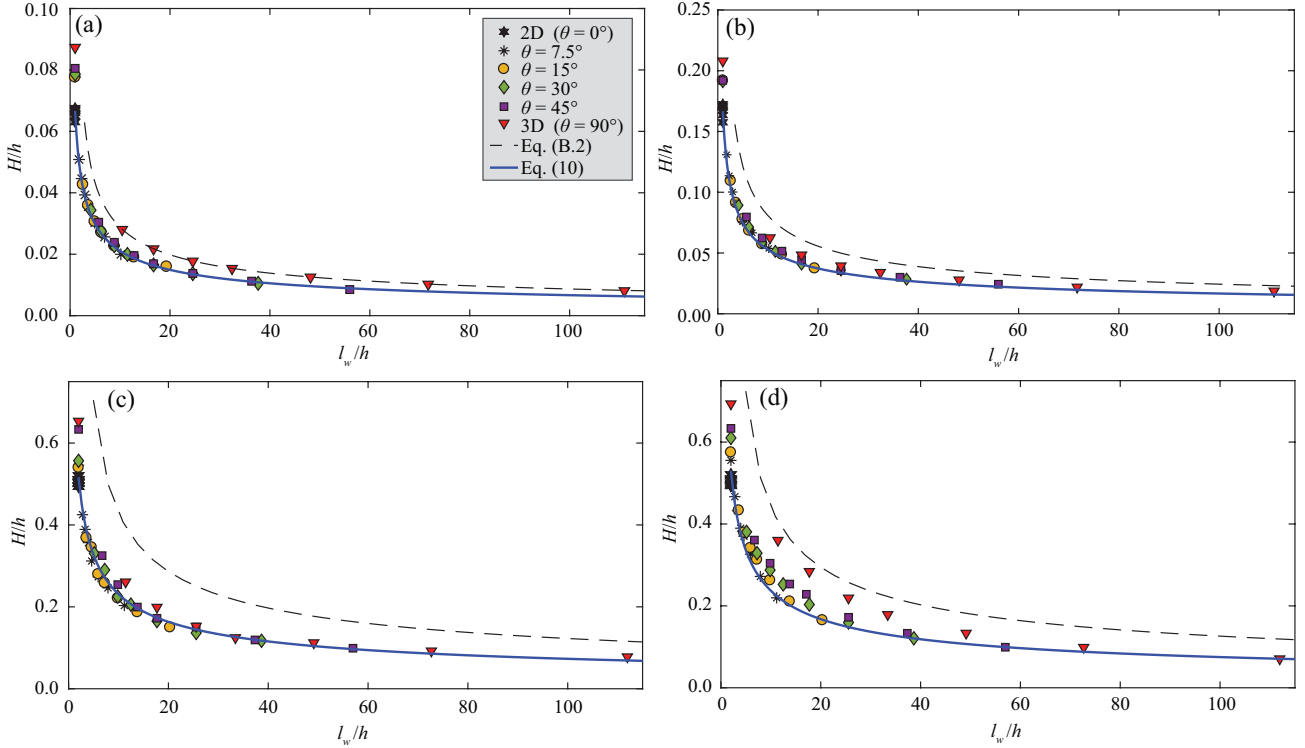


Figure 11: Relative wave height H/h decay with l_w/h for (a) approximate linear waves, (b) 5th order Stokes waves, (c) 5th order cnoidal waves and (d) 1st order solitary waves in all investigated geometries compared to Green's law (Eq. (10)) ((a) $nRMSE = 0.06$, (b) $nRMSE = 0.06$, (c) $nRMSE = 0.05$, (d) $nRMSE = 0.08$) and diffraction theory (Eq. (B.2)).

414 For Stokes waves shown in Fig. 11b, the diffraction theory under-predicts
 415 the wave height decay in all geometries, which is not surprising given that the
 416 considered theory is based on linear wave theory. Fig. 11c shows a similar decay
 417 curve for cnoidal waves. In this case the data move further away from diffraction
 418 theory. For example, at $l_w/h = 20$ the ratio between the numerical values and
 419 the values calculated by diffraction theory (Carr and Stelzriede, 1952) is 0.56
 420 (Fig. 11c). This difference appears to be very sensitive to the ratio b'/L used to
 421 calculate Eq. (B.2); larger ratios (Fig. 11a, b) result in a closer agreement with
 422 the simulated results than smaller ratios (Figs. 11c).

423 Fig. 11d shows the wave decay for solitary waves. The data scatter relative to
 424 Green's law in the range $6 < l_w/h < 40$ is larger than for the other wave types.
 425 For $l_w/h < 6$ and $l_w/h > 40$ there is still a close match between the data and Eq.
 426 (10). The largest difference from Green's law is found for the 3D geometry with
 427 up to 40% difference in wave height. Fig. C.1 shows the corresponding results
 428 for the wave amplitudes, as for the wave heights shown in Fig. 11, compared
 429 with Eq. (12) (Appendix C).

430 3.1.3. Lateral wave energy spread

431 In this section the lateral wave energy spread for each wave type is investigated.
 432 The wave height is investigated with a resolution of $\Delta\gamma' = 7.5^\circ$ at
 433 different r'/h .

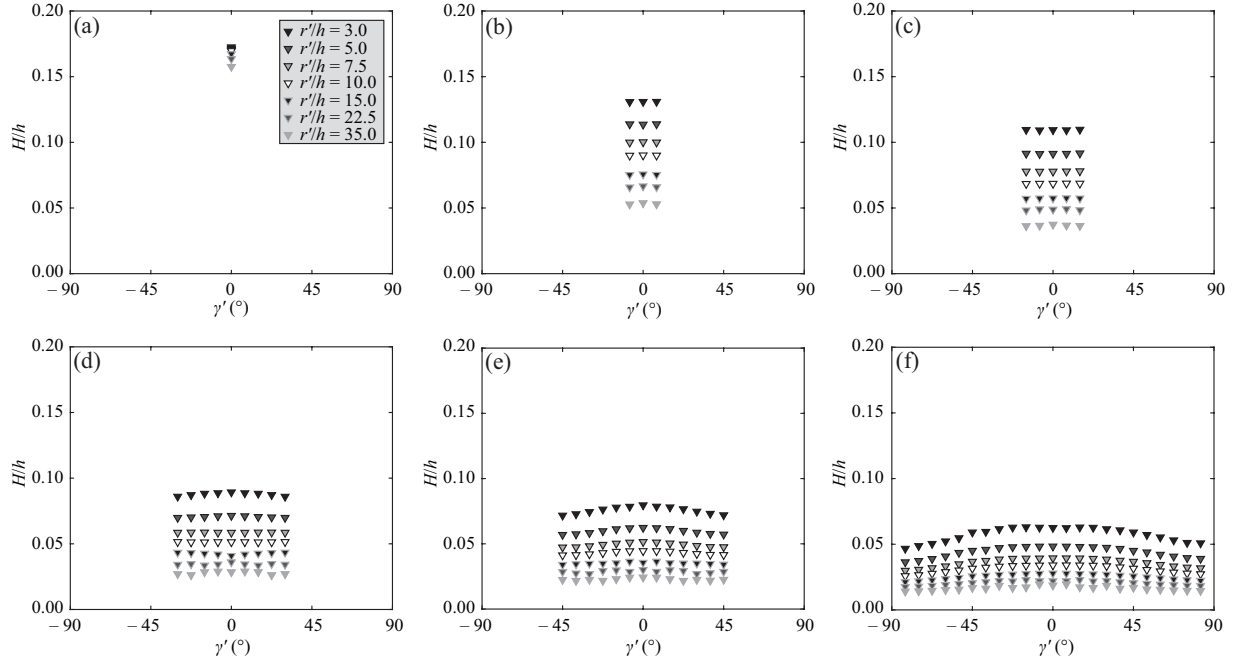


Figure 12: Relative wave heights H/h for Stokes waves as a function of the propagation angle γ' and the relative radial distance r'/h for (a) 2D ($\theta = 0^\circ$), (b) $\theta = 7.5^\circ$, (c) $\theta = 15^\circ$, (d) $\theta = 30^\circ$, (e) $\theta = 45^\circ$ and (f) 3D ($\theta = 90^\circ$).

434 Fig. 12 shows the spatial distribution of the wave heights for the 5th order
 435 Stokes waves (the other wave types are shown in Appendix D) with different
 436 r'/h values represented by different grey shades. The lateral wave decay becomes
 437 important with increasing θ . Fig. 12f shows that the maximum wave heights at
 438 $\gamma' = 0^\circ$ are 20 – 34% larger than at $\gamma' = \pm 82.5^\circ$.

439 Green's law is used to correlate the lateral decay of H with the propagation
 440 angle γ' in all investigated geometries. Fig. 13 shows H normalised by using Eq.
 441 (10), on the y -axis, over the wave propagation angle γ' for all simulated wave
 442 types. Green's law is represented by a blue circle.

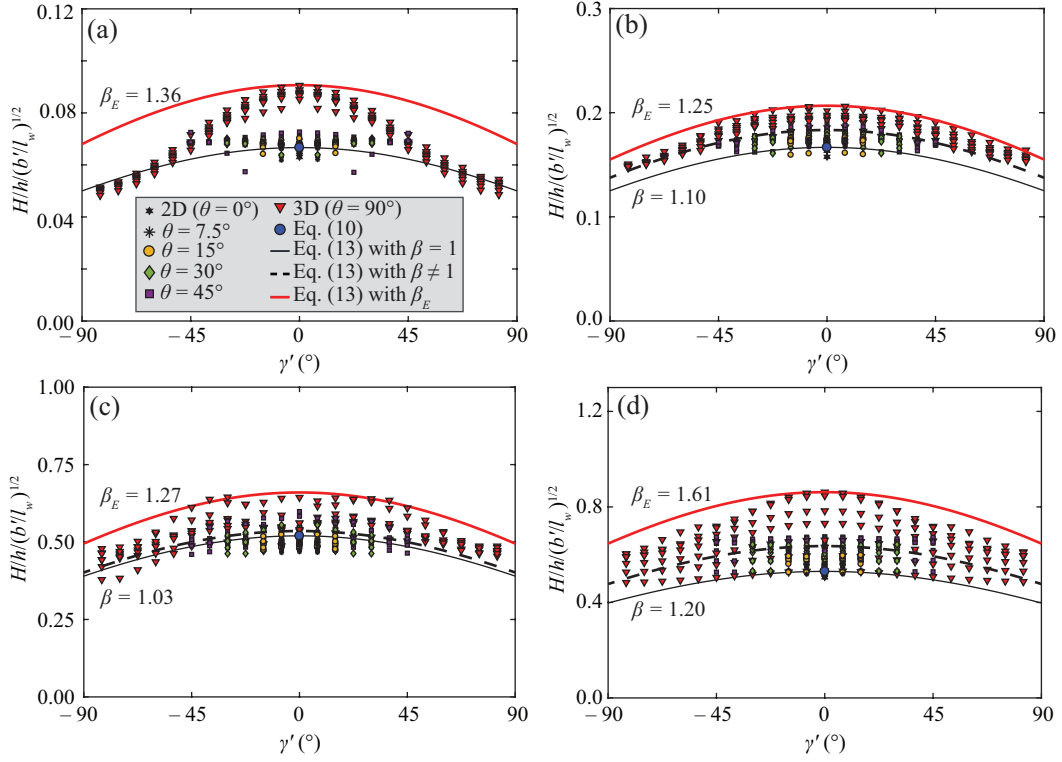


Figure 13: Lateral wave decay for (a) approximate linear waves, (b) 5th order Stokes waves, (c) 5th order cnoidal waves and (d) 1st order solitary waves for all investigated geometries, compared to Eq. (13).

443 The decay term $\cos^2(\gamma'/3)$ is inspired by Heller and Spinneken (2015) and
 444 Huber and Hager (1997) where $\cos^2\{1+\exp[-0.2(r/h)]\} (2\gamma/3)$ and $\cos^2(2\gamma/3)$, res-
 445 pectively, have been found for experimental data based on the 3D geometry.
 446 The value 2/3 is reduced to 1/3 herein to better represent the data. This smaller
 447 lateral wave decay is associated with the lack of slide momentum in the far field,
 448 where the present results apply, in contrast to Heller and Spinneken (2015) and
 449 Huber and Hager (1997) involving also the near field with a larger lateral de-
 450 cay. To reproduce the lateral decay trend in the far field, the empirical term

451 $\cos^2(\gamma'/3)$ is added to the theoretical Eqs. (10) and (12) resulting in

$$\frac{H(r', \gamma', \theta)}{h} / \left(\frac{b'}{l_w(r', \theta)} \right)^{1/2} = \beta \frac{H(r' = 0, \gamma' = 0^\circ, \theta = 0^\circ)}{h} \cos^2 \left(\frac{\gamma'}{3} \right) \quad (13)$$

$$\frac{a(r', \gamma', \theta)}{h} / \left(\frac{b'}{l_w(r', \theta)} \right)^{1/2} = \beta \frac{a(r' = 0, \gamma' = 0^\circ, \theta = 0^\circ)}{h} \cos^2 \left(\frac{\gamma'}{3} \right) \quad (14)$$

452 where $H(r', \gamma', \theta)$ and $a(r', \gamma', \theta)$ are the wave height and amplitude at the po-
 453 sition r' and γ' , $l_w(r', \theta)$ the corresponding wavefront length (Table C.1) and
 454 $H(r' = 0, \gamma' = 0^\circ, \theta = 0^\circ)$ and $a(r' = 0, \gamma' = 0^\circ, \theta = 0^\circ)$ are the 2D wave height
 455 and amplitude, respectively. The water depth $h = \text{constant}$ is maintained in Eqs.
 456 (13) and (14) to keep the equations in dimensionless form. An empirical pre-
 457 factor can be applied to $H(r' = 0, \gamma' = 0^\circ, \theta = 0^\circ)$ and $a(r' = 0, \gamma' = 0^\circ, \theta = 0^\circ)$
 458 to determine the upper envelope (β_E) and the best overall fit (β) of the numerical
 459 data. β is based on the smallest $nRMSE$, which together with the corresponding
 460 $\pm\%$ scatter are summarised in Table 3 for both H and a .

Table 3: Pre-factors for wave height H (Eq. (13)) and wave amplitude a (Eq. (14)) for each investigated wave type. The upper envelope is determined with β_E and the best overall fit to the data in Fig. 13 with β .

Wave theory	H			a		
	β_E	β ($nRMSE$)	\pm scatter	β_E	β ($nRMSE$)	\pm scatter
Approximate linear	1.36	-	-	1.36	-	-
5 th order Stokes	1.25	1.10 (0.17)	+13%, -14%	1.18	1.01 (0.14)	+17%, -14%
5 th order cnoidal	1.27	1.03 (0.16)	+23%, -12%	1.09	0.85 (0.21)	+26%, -39%
1 st order solitary	1.61	1.20 (0.21)	+36%, -21%	1.14	0.84 (0.23)	+36%, -38%

461 The black curve in Fig. 13 represents Eq. (13) with $\beta = 1$, the red line
 462 with β_E and the dashed line with β . For the approximate linear waves, only
 463 the line with β_E is presented as the main purpose to include this wave type
 464 herein is to link the numerical results to theory rather than to predict landslide-
 465 tsunamis, given that they are generally not linear. Stokes waves result in the
 466 smallest $\beta_E = 1.25$ for H requiring only 25% increase from the semi-theoretical
 467 expression to reach the upper envelope. The best fit is achieved with $\beta = 1.10$
 468 with a data scatter of +13% and -14%. For cnoidal waves (Fig. 13c) $\beta_E = 1.27$
 469 and $\beta = 1.03$ with a data scatter of +23% and -12%. Finally, the solitary waves
 470 (Fig. 13d) result in the largest difference between the black and the red curves
 471 with $\beta_E = 1.61$ and $\beta = 1.20$ with a data scatter of +36% and -21%. For the
 472 solitary wave the black curve corresponds simultaneously to a lower envelope
 473 of the values. This is already indicated in Fig. 11d where all points lay above
 474 Green's law. The corresponding values for the wave amplitude a for each wave
 475 type are also shown in Table 3. In this case the best fit is always achieved for
 476 $\beta < 1$, except for Stokes waves, while $\beta_E > 1$. Fig. C.2 shows the corresponding
 477 data.

478 Fig. 13b-d allow for a semi-theoretical prediction of idealised tsunami heights
 479 for all investigated wave types, geometries and locations. These predictions take
 480 the effect of the water body geometry into account as well as bottom friction.
 481 However, they are based on idealised wave types, which propagate as wave trains
 482 of constant H , unlike real tsunamis. This creates differences in wave propagation
 483 which are investigated in Section 3.2 based on experimental wave profiles.

484 3.2. Laboratory waves

485 Simulations of waves measured in the laboratory experiments of Heller and
 486 Hager (2011) were carried out to quantify to which extent frequency dispersion
 487 affects wave decay in 2D. The 2D geometry was chosen as it excludes the lateral
 488 energy spread and the wave decay may fully be attributed to frequency disper-
 489 sion, if bottom friction is neglected. Experimental measurements (Heller and
 490 Hager, 2011) are compared with SWASH simulations based on both idealised
 491 time series essentially excluding frequency dispersion (Section 1.2) and real time
 492 series based on the same study.

493 3.2.1. Coupling criterion

494 To perform this comparison between idealised and laboratory waves, a crite-
 495 rion for the coupling location corresponding to the boundary between the wave
 496 generation and propagation zones (Fig. 2) is required. The impact radius r_i from
 497 Evers et al. (2019) and the location of the maximum wave amplitude x_M from
 498 Heller and Hager (2010) are considered. These criteria are given as:

$$r_i(\gamma = 0^\circ) = 2.5[PB \cos(6/7\alpha)]^{1/4}h \quad (15)$$

$$x_M = (11/2)P^{1/2}h. \quad (16)$$

499 $P = FS^{1/2}M^{1/4}[\cos(6/7\alpha)]^{1/2}$ is the impulse product parameter (Heller and
 500 Hager, 2010), $B = b/h$ the relative slide width and α the slide impact angle. P
 501 includes the slide Froude number $F = V_s/(gh)^{1/2}$ with the slide centroid velocity
 502 V_s at impact, the relative slide thickness $S = s/h$ with the slide thickness s at
 503 impact and the relative slide mass $M = m_s/(\rho_w bh^2)$ with the slide mass m_s and
 504 the water density ρ_w . The coupling locations based on Eqs. (15) and (16) move
 505 further downstream for more violent slide impacts and wave generation. Both r_i
 506 and x_M depend solely on the landslide parameters, which are anyway required
 507 for landslide-tsunami hazard assessment. The slide parameters and the potential
 508 coupling locations, computed with Eqs. (15) and (16) for each investigated wave
 509 type, are summarised in Table 4.

510 To work on the safe side, the coupling location is selected at the wave gauge
 511 located downwave of both r_i/h and x_M/h . The first wave gauge position of Heller
 512 and Hager (2011) that satisfies $d_M/h = x/h \geq \max(r_i/h; x_M/h)$ is also included
 513 in Table 4. This position was chosen as coupling location and wave generation
 514 for both simulations based on the laboratory time series and idealised waves.

Table 4: Slide parameters and coupling locations based on Eqs. (15) and (16) for each wave type.

Wave type	B	S	M	F	α	P	Eq. (15)	Eq. (16)	coupling location
Stokes-like	0.50	0.23	0.11	1.36	45°	0.33	1.50	3.16	$x/h = 4.55$
Cnoidal-like	0.50	0.40	0.45	2.27	45°	1.03	1.99	5.58	$x/h = 8.10$
Solitary-like	0.50	0.81	0.90	3.77	90°	1.55	1.61	6.85	$x/h = 8.57$

3.2.2. Effects of frequency dispersion

Figure 14 shows the wave profiles at 3 different positions for a Stokes-like landslide-tsunami. The decay of the idealised waves is negligible whereas both the laboratory and the real time series show a similar decay. This shows that the primary wave decay for Stokes-like waves in 2D is mainly caused by frequency dispersion as indicated by the increase of the tail waves in Fig. 14a to c. Frequency dispersion is negligible for idealised waves where the wave profiles remain stable. To quantify frequency dispersion the ratios a_l/a_c and H_l/H_c are calculated, with a_l and H_l as the wave amplitude and height at the last wave gauge position (Figs. 14c, 15c, 16c) in Heller and Hager (2011) and a_c and H_c as the wave amplitude and height at the coupling location. These ratios are given in Table 5.

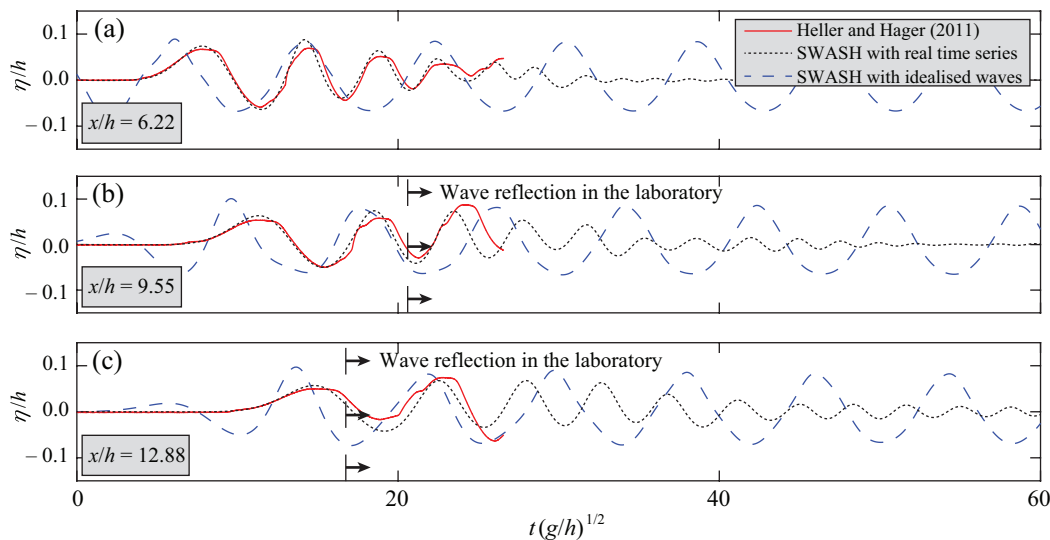


Figure 14: Comparison of 2D laboratory measurements of Stokes-like waves, real time series and 5th order idealised Stokes wave SWASH simulations: relative water surface elevation η/h at different relative distances x/h .

Similar values of $a_l/a_c = 0.66$ and 0.73 are found for the laboratory measurements and real time series simulations, respectively, confirming the capability of SWASH to simulate frequency dispersion reasonably well for Stokes-like

530 waves. However, for the idealised Stokes waves a value of $a_l/a_c = 0.96$ and even
 531 $H_l/a_c = 0.99$ is found confirming the small wave decay due to bottom friction.

532 The cnoidal-like and solitary-like waves are shown in Figs. 15 and 16. Cnoidal-
 533 like waves decay much slower than Stokes-like waves (Fig. 14) when considering
 534 that the investigated maximum relative distance for cnoidal-like waves is twice
 535 as large. Very similar a_l/a_c laboratory measurement and numerical ratios for
 536 the cnoidal-like wave profiles are found namely 0.79-0.86 (Table 5).

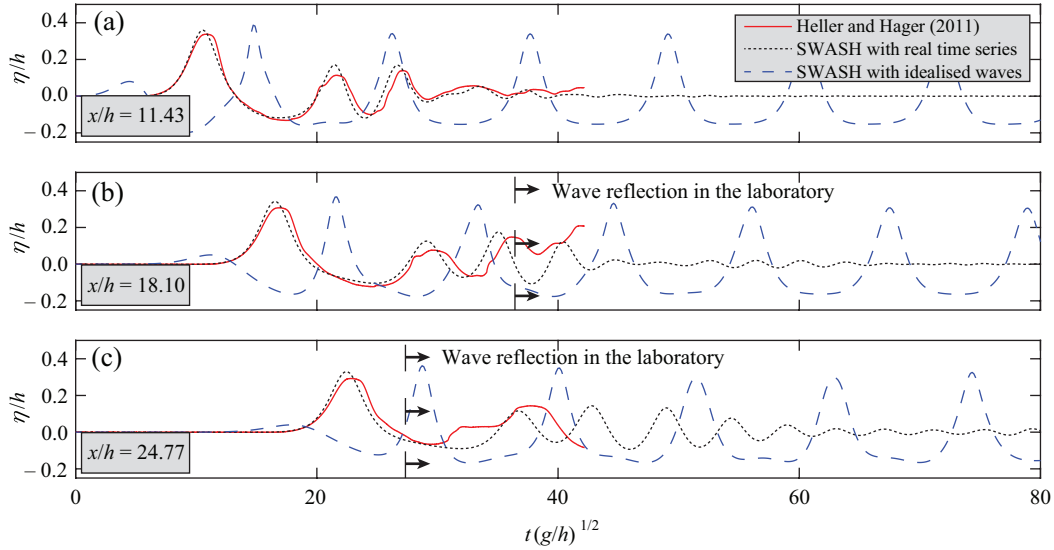


Figure 15: Comparison of 2D laboratory measurements of cnoidal-like waves, real time series and 5th order idealised cnoidal SWASH wave simulations: relative water surface elevation η/h at different relative distances x/h .

537 However, when considering H_l/H_c it becomes clear that cnoidal-like waves
 538 are also affected by frequency dispersion. In fact, there is a difference of 12%
 539 between the simulations with the experimental time series ($H_l/H_c = 0.78$) and
 540 idealised waves ($H_l/H_c = 0.90$). The results for solitary-like waves (Fig. 16)
 541 show an even closer match between laboratory measurements, real time series
 542 and idealised waves than cnoidal-like waves. Equal $a_l/a_c = H_l/H_c = 0.90$ for
 543 real and idealised wave simulations are observed and only a 8% difference to the
 544 laboratory measurements is found.

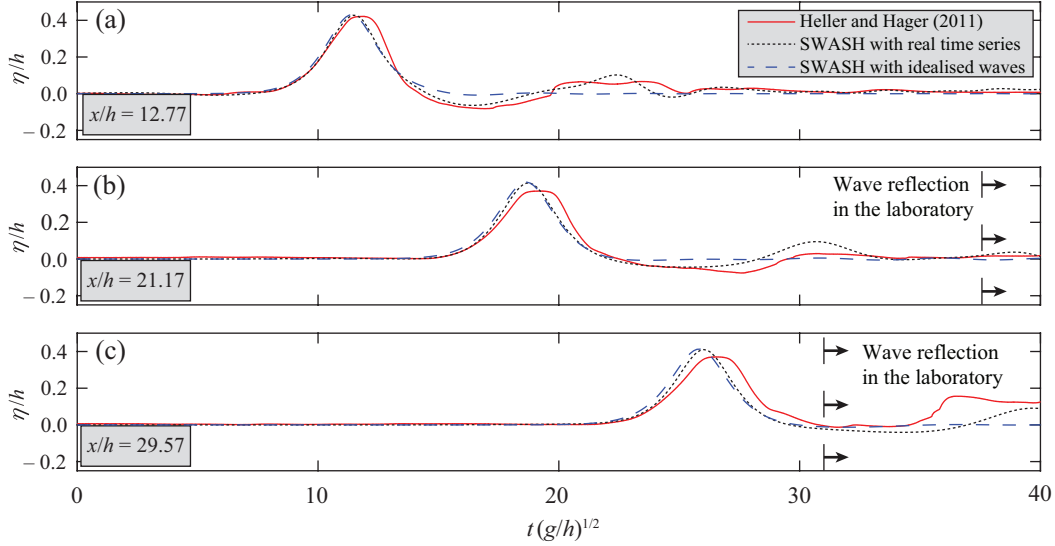


Figure 16: Comparison of 2D laboratory measurements of solitary-like waves, real time series and 1st order idealised solitary SWASH wave simulations: relative water surface elevation η/h at different relative distances x/h .

Table 5: Wave decay ratios between wave amplitude a_l and height H_l at the last wave gauge position in Heller and Hager (2011) and the wave amplitude a_c and height H_c at the coupling location for each wave type (* measurements affected by reflection).

Wave type	Gauge at coupling location	Location of last gauge	Heller and Hager (2011)	SWASH	SWASH
				real time series	idealised waves
$a_l/a_c \left(\left[\frac{a_l}{a_c} - 1 \right] \times 100 \right)$					
Stokes(-like)	$x/h = 4.55$	$x/h = 12.88$	0.66 (-34%)	0.73 (-27%)	0.96 (-4%)
Cnoidal(-like)	$x/h = 8.10$	$x/h = 24.77$	0.79 (-21%)	0.86 (-24%)	0.83 (-17%)
Solitary(-like)	$x/h = 8.57$	$x/h = 29.57$	0.83 (-17%)	0.90 (-10%)	0.90 (-10%)
$H_l/H_c \left(\left[\frac{H_l}{H_c} - 1 \right] \times 100 \right)$					
Stokes(-like)	$x/h = 4.55$	$x/h = 12.88$	0.51 (-49%)*	0.80 (-20%)	0.99 (-1%)
Cnoidal(-like)	$x/h = 8.10$	$x/h = 24.77$	0.69 (-31%)*	0.78 (-22%)	0.90 (-10%)
Solitary(-like)	$x/h = 8.57$	$x/h = 29.57$	0.83 (-17%)	0.90 (-10%)	0.90 (-10%)

545 These results show that the contribution of frequency dispersion on wave
546 decay changes with the wave type. The mismatch of H_l/H_c for the laboratory
547 Stokes-like and cnoidal-like tsunamis is due to wave reflection (Fig. 14c, Fig.
548 15c) affecting the primary wave trough (Table 5). This confirms that the effect
549 of frequency dispersion on wave decay in 2D decreases with increasing non-
550 linearity of the wave type. This further shows that the findings based on the
551 idealised waves (Section 3.1) apply well to landslide-tsunamis in proximity of the
552 shallow-water wave regime (solitary-like waves), but may overestimate landslide-
553 tsunamis closer to the deep-water regime (Stokes-like waves) where frequency
554 dispersion accounts for up to $34\% - 4\% = 30\%$ of the wave decay.

555 **4. Discussion**

556 In this section the new findings are discussed in relation to already avail-
557 able knowledge. The idealised waves essentially address the effect of the lateral
558 energy spread and neglect frequency dispersion. Laboratory measurements are
559 compared to the idealised waves propagating in the far field to quantify whether
560 the effect of the lateral energy spread or frequency dispersion is more dominant.
561 Further, Eqs. (13) and (14) are applied to the 2014 Lake Askja landslide-tsunami
562 to illustrate the application of the new semi-theoretical equations.

563 *4.1. Relevance of the water body geometry for idealised waves*

564 The ratio b'/L and the wave non-linearity H/h were found to be very im-
565 portant for the effect of the water body geometry as they significantly affect the
566 wave decay inside a water body and determine how closely the diffraction theo-
567 ry of Carr and Stelzriede (1952) matches the numerical data. This can clearly
568 be seen by comparing the results in Figs. 11b and Fig. 11c where the Stokes
569 waves result in a closer match to diffraction theory than cnoidal waves. The
570 two parameters b'/L and H/h , however, do not seem to affect the match with
571 Green's law (Eq. (10)) that follows all numerical data closely except for solitary
572 waves in Fig. 11d where the 3D geometry shows a noticeable difference, in the
573 range $6 < l_w/h < 40$.

574 The water body geometry has also an effect on the observed wave type.
575 In fact, the solitary wave transforms in a Stokes wave in 3D as indicated by
576 $a/a_t = 1.07$ in Fig. 9d. This agrees with Heller and Spinneken (2015) where
577 the more energetic solitary and bore-like waves were only observed in 2D and
578 only Stokes-like and cnoidal-like waves were observed in 3D by identical slide
579 scenarios.

580
581 The effect of the water body geometry for idealised waves was correlated
582 with l_w used in the Green's law (Eqs. (10) and (12)). This allows for a much
583 broader application of the findings of Chang et al. (1979) for solitary waves where
584 the width of the diverging channel rather than l_w was used. Further, the semi-
585 theoretical Eqs. (13) and (14) were derived to predict the lateral wave decay.
586 Using these equations, with a different pre-factor β_E for the upper envelope and
587 β for the best fit of the data for each wave type, allows for the calculation of
588 the maximum wave heights and amplitudes in all investigated geometries, for
589 all propagation angles and distances for idealised waves (excluding frequency
590 dispersion). Given that for all herein investigated scenarios the idealised waves
591 produced larger waves than the real waves (including frequency dispersion) in
592 2D (Table 5), the semi-theoretical equations in Section 3.1.3 tend to over-predict
593 real landslide-tsunamis and tend to work on the safe side.

594 *4.2. Relevance of lateral energy spread and frequency dispersion*

595 Table 6 shows the ratios a_l/a_c and H_l/H_c of the idealised waves. This helps to
596 separate the contributions of the lateral energy spread and frequency dispersion
597 on wave decay as the idealised waves essentially consider the former effect only.

598 Table 6 also includes the values of Table 5 of the idealised waves in 2D for
599 comparison. All values in Table 6 are lower than the values calculated in Table
600 5 indicating that the lateral energy spread is more important than frequency
601 dispersion, already for $\theta = 7.5^\circ$. The differences between the values in Table 5
602 and 6 further increase with θ . For example, Table 5, shows $a_l/a_c = 0.66, 0.79$
603 and 0.83 for Stokes-like, cnoidal-like and solitary-like tsunamis in 2D and the
604 corresponding values for $\theta = 7.5^\circ$ in Table 6 are $0.46, 0.43$ and 0.45 . This also
605 shows that the solitary wave is the most affected wave type by the effect of
606 the lateral energy spread with $a_l/a_c = 0.14$ for 3D (Table 6) against 0.83 for
laboratory measurements in 2D (Table 5).

Table 6: Idealised wave decay ratios between wave amplitude a_l and height H_l at the last experimental wave gauge position used in Section 3.2 (Heller and Hager, 2011) and the wave amplitude a_c and height H_c at the numerical wave source (coupling location).

Wave type	Location of last gauge (x'/h or r'/h)	2D ($\theta = 0^\circ$)	$\theta = 7.5^\circ$	$\theta = 15^\circ$	$\theta = 30^\circ$	$\theta = 45^\circ$	3D ($\theta = 90^\circ$)
a_l/a_c ($[(a_l/a_c)-1] \times 100$)							
Stokes	8.33	0.96 (-4%)	0.46 (-54%)	0.39 (-61%)	0.27 (-73%)	0.23 (-77%)	0.18 (-82%)
Cnoidal	16.70	0.83 (-17%)	0.43 (-57%)	0.31 (-69%)	0.25 (-75%)	0.23 (-77%)	0.16 (-84%)
Solitary	21.00	0.90 (-10%)	0.45 (-55%)	0.33 (-66%)	0.24 (-76%)	0.20 (-80%)	0.14 (-86%)
H_l/H_c ($[(H_l/H_c)-1] \times 100$)							
Stokes	8.33	0.99 (-1%)	0.50 (-50%)	0.36 (-64%)	0.29 (-71%)	0.25 (-75%)	0.16 (-84%)
Cnoidal	16.70	0.90 (-10%)	0.59 (-51%)	0.37 (-63%)	0.29 (-71%)	0.26 (-74%)	0.17 (-83%)
Solitary	21.00	0.90 (-10%)	0.50 (-50%)	0.38 (-62%)	0.27 (-73%)	0.21 (-79%)	0.15 (-85%)

607

608 4.3. Computation example

609 A procedure to predict landslide-tsunamis using Eqs. (13) and (14) is pre-
610 sented here. The present study only addresses wave propagation, while already
611 available relationships for the 2D case (Heller and Hager, 2010) allow to com-
612 pute the maximum wave height and its position in the wave generation zone.
613 Note that the slide width b' at the coupling location is approximated with the
614 slide width b from the impact zone plus an arc section on either side of the
615 slide (Fig. 17). This approximation is necessary as a straight line at the cou-
616 pling location (as in Fig. 3) would converge to infinity with increasing θ . This
617 approximation also satisfies the energy flux conservation between $l_w(r' = 0, \theta)$
618 and $l_w(r', \theta)$, which coincides with the assumptions made for Green's law (Dean
619 and Dalrymple, 1991).

620 The application procedure of Eq. (13) can be summarised with the following
621 steps:

- 622 1. Define the landslide width b , thickness s , mass m_s , impact velocity V_s ,
623 slope angle α , density ρ_s , water density ρ_w and water depth h
- 624 2. Evaluate the wave type in 2D using the wave type product T of Heller
625 and Hager (2011)
- 626 3. Calculate the maximum wave height H_M for 2D and its position from the
627 slide impact $r = d_M$

- 628 4. Define θ_1 and θ_2 (Fig. 17) at the slide sides to approximate the current
629 geometry to an idealised one up to $r' = 0$ and calculate the wave front
630 length $l_w(r' = 0, \theta)$
631 5. Compute $H(r' = 0, \gamma' = 0^\circ, \theta)$ by applying energy conservation

$$H(r' = 0, \gamma' = 0^\circ, \theta) = H_M(r' = 0, \gamma' = 0^\circ, \theta = 0^\circ)[b/l_w(r' = 0, \theta)]^{1/2} \quad (17)$$

- 632 6. Define θ_3 and θ_4 (Fig. 17) at the slide sides to approximate the geometry up
633 to a desired distance $r' > 0$, thereby taking any restrictions or expansions
634 of the water body into account, and calculate $l_w(r', \theta)$
635 7. Use Eq. (13) to calculate $H(r', \gamma', \theta)$ at the desired location.

636 These steps are illustrated with the 2014 landslide-tsunami event in Lake Askja
637 in Iceland.

638 The wave heights are computed at two different positions and compared
639 with the numerical results of Gylfadóttir et al. (2017). The slide parameters
640 are defined first (step 1). The slope angle is calculated by using the 500 m
641 distance between the base of the rotational failure and the mean water level
642 and the elevation difference between the same two points (92 m) resulting in
643 $\alpha = \text{atan}(92/500) = 10.4^\circ$. The effective friction coefficient is defined as $\mu =$
644 $\Delta H/\Delta L$ where $\Delta H = 230$ m is the height difference of the slide centroid's initial
645 and final positions and $\Delta L = 2450$ m is the horizontal distance between the same
646 two points. This results in $\mu = 0.09$. This small friction coefficient indicates a
647 hypermobile slide as observed in nature for large slide volumes exceeding 10^6 m³
648 (Pudasaini and Miller, 2013), which is in line with the slide volume of 10×10^6
649 m³ (considering a 30% porosity) in the Lake Askja case. The corresponding
650 impact velocity is $V_s = \sqrt{2g(\sin \alpha - \mu \cos \alpha)\Delta x} = 30.1$ m/s (Körner, 1976) with
651 $\Delta x = 500$ m as the distance from the initial position of the slide centroid to
652 the SWL. This velocity is only 2.6% smaller than 30.9 m/s used by Gylfadóttir
653 et al. (2017) as best fit for their simulations. The remaining slide parameters
654 are summarised in Table 7 with the slide mass m_s computed based on the slide
655 volume and a slide density of $\rho_s = 2000$ kg/m³.

Table 7: Dimensional landslide parameters for the 2014 Lake Askja landslide-tsunami

b (m)	s (m)	α (°)	V_s (m/s)	m_s (kg)	ρ_s (kg/m ³)	ρ_w (kg/m ³)	h (m)
550.0	35.5	10.4	30.1	2×10^{10}	2000	1000	138.0

656 The wave type product $T = S^{1/3}M \cos[(6/7)\alpha] = 0.26^{1/3}1.91 \cos[(6/7)10.4^\circ] =$
657 1.21 (Table 8) is calculated to evaluate the wave type (step 2). The wave type
658 product T for granular landslides is in the range of $4/5F^{-7/5} \leq T \leq 11F^{-5/2}$
659 ($1.06 \leq 1.21 \leq 18.06$) for which cnoidal and solitary-like waves are expected
660 in 2D (Heller and Hager, 2011). The former wave type was chosen because T
661 is closer to the lower boundary of the range where less energetic waves are ex-
662 pected hence $\beta = 1.03$ and $\beta_E = 1.27$ are selected.

663 The maximum wave height H_M is computed with $H_M = 5/9P^{4/5}h =$

Table 8: Non-dimensional landslide parameters for the Lake Askja landslide-tsunami

S	M	F	T	P	d_M (m)	H_M (m)	a_M (m)
0.26	1.91	0.82	1.21	0.49	531	43.3	34.7

664 $5/9 \cdot 0.49^{4/5} 138 = 43.3$ m (Table 8) (Heller and Hager, 2010) for 2D with $P =$
665 $FS^{1/2}M^{1/4}\{\cos[(6/7)\alpha]\}^{1/2} = 0.82 \cdot 0.26^{1/2}1.91^{1/4}\{\cos[(6/7)10.4^\circ]\}^{1/2} = 0.49$
666 introduced in Section 3.2 (step 3). Because the geometry of the Lake Askja is
667 not symmetrical, different θ result on the two slide sides. The wavefront length
668 at $r = d_M$ is thus calculated using $\theta_1 = 32.4^\circ$, $\theta_2 = 44.1^\circ$ (Fig. 17) and the
669 slide width $b = 550$ m resulting in $l_w(r' = d_M, \theta) = b + \theta_{rad,1}d_M + \theta_{rad,2}d_M =$
670 $550 + 32.4(\pi/180)531 + 44.1(\pi/180)531 = 1259$ m (step 4). Note that r' in Eq.
671 (9) is replaced here with r because the geometry already starts to diverge at
672 $r = 0$ rather than at $r' = 0$. Since H_M applies to 2D, the observed wave height at
673 the coupling location may be smaller due to lateral energy spread. This is taken
674 into account by spreading the wave energy over the wavefront length resulting
675 in $H(r' = 0, \gamma' = 0^\circ, \theta) = H_M(r' = 0, \gamma' = 0^\circ, \theta = 0^\circ)[b/l_w(r' = 0, \theta)]^{1/2} =$
676 $43.3(550/1259)^{1/2} = 28.6$ m (step 5).

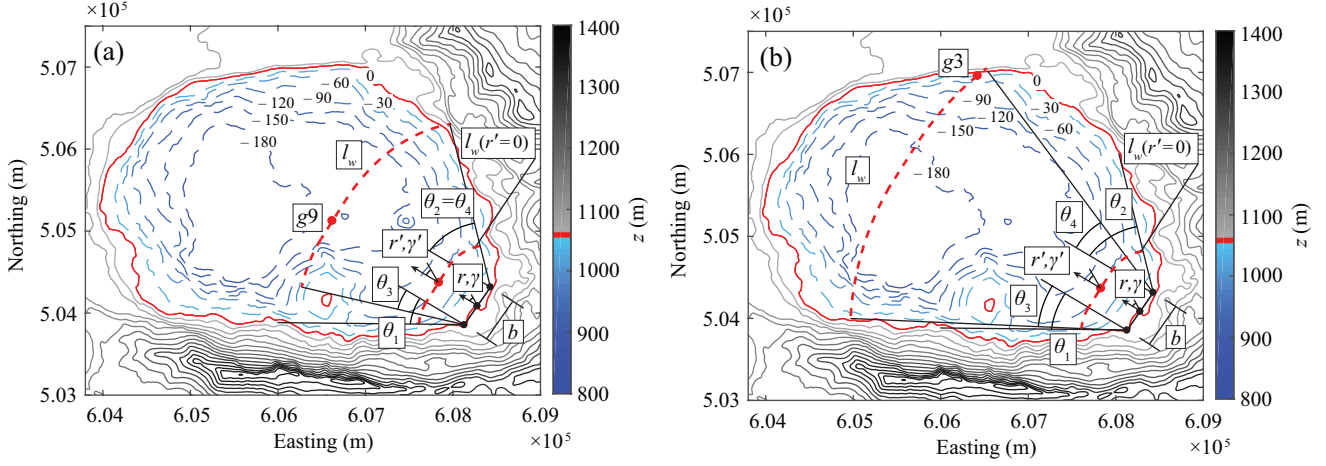


Figure 17: Computation examples for (a) wave gauge 9 and (b) wave gauge 3 of Gylfadóttir et al. (2017). The red line highlights the SWL = 1058 m above sea level. The contours represent a spacing of $\Delta z = 30$ m in global coordinates with dashed lines and solid lines representing the terrain elevation below and above the SWL, respectively.

677 The wave heights are calculated at wave gauges 9 ($r = 1970$ m, $\gamma = 0^\circ$)
678 and 3 ($r = 3440$ m, $\gamma = 23.7^\circ$) (Gylfadóttir et al., 2017). At gauge 9 the
679 wavefront length, again with r' replaced by r , is $l_w = 550 + 19.2(\pi/180)1970 +$
680 $44.1(\pi/180)1970 = 2726$ m by using $\theta_3 = 19.2^\circ$ and $\theta_4 = 44.1^\circ$ (Fig. 17a, step
681 6). θ_3 is chosen under the consideration of the water body restriction caused
682 by the small island on the left hand side of the slide, which affects the lateral

683 wave energy spread. Finally, applying Eq. (13) for $\gamma = 0^\circ$ with the pre-factors
684 $\beta = 1.03$ and $\beta_E = 1.27$ (for cnoidal waves, Table 3) results in $H = 20.0$ m and
685 $H = 24.7$ m respectively (step 7). These values are close (-10.0% and $+11.2\%$
686 difference, respectively) to the wave height $H = 22.2$ m found by Gylfadóttir
687 et al. (2017).

688 At gauge 3 the wavefront length is $l_w = 3614$ m with $\theta_3 = 30.5^\circ$ and $\theta_4 =$
689 20.5° (Fig. 17b). Eq. (13) is applied with $\gamma = 23.7^\circ$ and the pre-factors $\beta =$
690 1.03 and $\beta_E = 1.27$ (Table 3) resulting in $H = 17.1$ m and $H = 21.0$ m,
691 respectively, which in turn underestimate the wave height of $H = 26.0$ m found
692 by Gylfadóttir et al. (2017) by 34.2% and 19.2% , respectively. However, such an
693 underestimation is expected as gauge 3 is located close to the lake shore where
694 shoaling, which is not considered in Eq. (13), becomes important. Shoaling could
695 also be found in combination with other depth and geometry related effects such
696 as reflection and depth trapping of the tsunami (Bellotti et al., 2012), which in
697 combination with the impact on the coast may alter the tsunami characteristics.

698 The same procedure is applied to calculate the landslide-tsunami amplitude
699 using Eq. (14). Step 1 and step 2 remain the same as for the wave height. In 3 the
700 maximum wave amplitude $a_M = 4/9P^{4/5}h = 34.7$ m (Heller and Hager, 2010)
701 instead of H_M . Step 4 remains unchanged and step 5 is updated by calculating
702 the wave amplitude resulting in $a(r' = 0, \gamma' = 0, \theta) = a_M(r' = 0, \gamma' = 0^\circ, \theta =$
703 $0^\circ)[b/l_w(r' = 0, \theta)]^{1/2} = 22.9$ m. Step 6 remains unchanged and in step 7 Eq.
704 (14) is used, with $\beta = 0.85$ and $\beta_E = 1.09$ (Table 3). The results for the wave
705 amplitude, together with the ones for the wave heights, are summarised in Table
706 9. The values are close to $a = 13.4$ m for gauge 9 and $a = 14.2$ m for gauge 3
707 found by Gylfadóttir et al. (2017).

Table 9: Calculated wave parameters based on Eqs. (13) and (14) compared to the numerically
derived parameters by Gylfadóttir et al. (2017). In brackets the values $(y_{pred}/y_{num} -$
 $1) \times 100$ are shown (* values affected by shoaling).

Pre-factor	Predicted H (m)		H (m)	Predicted a (m)		a (m)
	β	β_E	(Gylfadóttir et al., 2017)	β	β_E	(Gylfadóttir et al., 2017)
gauge 9	20.0 (-10.0%)	24.7 ($+11.2\%$)	22.2	13.2 (-1.5%)	17.0 ($+26.8\%$)	13.4
gauge 3	17.1 (-34.2%)	21.0 (-19.2%)	26.0*	11.3 (-20.4%)	14.5 ($+2.1\%$)	14.2*

708 5. Conclusions

709 This study aimed to enhance the physical understanding of the effect of the
710 water body geometry on wave propagation with particular focus on landslide-
711 tsunamis. This aim was motivated by the very limited understanding of this
712 effect for intermediate geometries between the 2D and 3D geometries. This ef-
713 fect is associated with two components: lateral energy spread caused by the
714 increasing lateral space with the water body side angle θ and frequency disper-
715 sion. Idealised water body geometries with increasing $\theta = 0$ (2D), 7.5 , 15 , 30 , 45
716 and 90° (3D) of the flume lateral walls were used to simulate idealised and real

717 landslide-tsunamis. SWASH, a non-hydrostatic NLSWE model, was used to sim-
718 ulate propagation in the far field, where the wave is reasonable stable. Approx-
719 imate linear, Stokes, cnoidal and solitary waves were investigated up to a maxi-
720 mum distance of 35 times the water depth from the wave generation zone. These
721 idealised waves in combination with a constant water depth allowed the waves
722 in 2D to be stable and essentially excluded frequency dispersion.

723 The results in the 3D geometry were validated with diffraction theory given
724 that the wave generated by a landslide shows similarities to a wave diffracted
725 from a wave source of finite width. The wavefront length l_w (Eq. (9)) was found
726 to be an excellent parameter to link the wave heights of the idealised waves
727 in all investigated geometries along the slide axis resulting in a close match
728 with Green's law (Eq. (10)). The wave heights outside the slide axes were also
729 correlated with Green's law, modified with empirical pre-terms. These derived
730 semi-theoretical equations can be used to predict the idealised wave heights and
731 amplitudes in real water bodies based on 2D wave parameters estimated with
732 the method of Heller and Hager (2010).

733 It was further investigated how well the results derived for idealised waves
734 represent real tsunamis including frequency dispersion. Simulations in the 2D
735 geometry where therefore conducted by using the laboratory landslide-tsunami
736 time series of Heller and Hager (2011). Lateral energy spread is not present in 2D
737 such that the wave decay may essentially be attributed to frequency dispersion.
738 The 2D experiments of Heller and Hager (2011) were compared with SWASH
739 simulations based on experimental time series and idealised waves. An increas-
740 ing effect of frequency dispersion on wave decay with decreasing wave non-
741 linearity was observed. This shows that the semi-theoretical equations based on
742 the idealised waves are more appropriate for landslide-tsunamis in proximity of
743 the shallow-water wave regime (solitary-like waves), than for landslide-tsunamis
744 closer to the deep-water regime (Stokes-like waves) (Section 3.2).

745 The wave decay was also found to increase with θ , especially for solitary
746 waves. In fact, comparing wave heights and amplitudes, the effect of the lateral
747 energy spread is larger in intermediate geometries and 3D than the effect of
748 frequency dispersion in 2D. Finally, a calculation procedure to apply the new
749 semi-theoretical equations to real cases is provided showing a good agreement
750 of the wave heights (up to -10.0%) and amplitudes (up to -1.5%) for the 2014
751 Lake Askja tsunami.

752 Given that the findings in this study mainly support initial landslide-tsunami
753 hazard assessment, the effect of frequency dispersion may be neglected for
754 tsunamis in proximity of the shallow-water wave regime (solitary- and cnoidal-
755 like waves). However, in proximity of the deep-water wave regime (Stokes-like
756 waves), frequency dispersion accounts for up to 30% of the wave decay and can
757 not be neglected. The new equations can then still be applied, but will likely
758 result in an over-prediction of the real waves. This may be acceptable for initial
759 landslide-tsunami hazard assessment given that the predicted wave parameters
760 are on the safe side if depth and shore effects are excluded.

761 Future work will potentially also model the wave generation process and cou-
762 ple the wave propagation model SWASH with a wave generation model. This

763 would allow to simulate the entire landslide-tsunami process numerically. It is
 764 also planned to investigate the effect of a changing bathymetry on tsunamis.

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 769 Nottingham HPC cluster Minerva has been accessed to perform the numerical
 770 simulations.

771 Notation

A	$[-]$	= Mathieu function joining factor
a	$[L]$	= wave amplitude
a_M	$[L]$	= maximum wave amplitude
a_c	$[L]$	= wave amplitude at the coupling location
a_l	$[L]$	= wave amplitude at the last wave gauge
a_t	$[L]$	= wave trough amplitude
B	$[-]$	= relative slide width
b	$[L]$	= slide width at the slide impact location
b'	$[L]$	= source width at the coupling location
C_e	$[-]$	= even radial Mathieu function of the first kind
C_r	$[-]$	= Courant number
c	$[L/T]$	= wave celerity
ce	$[-]$	= even angular Mathieu function
c_f	$[-]$	= bottom friction coefficient
c_g	$[L/T]$	= wave group celerity
d	$[L]$	= total water depth
d_M	$[L]$	= coupling distance
E	$[M/T^2]$	= mean energy density per unit area
F	$[-]$	= slide Froude number
Fe_y	$[-]$	= even radial Mathieu function of the second kind
g	$[L/T^2]$	= gravitational acceleration
g_e	$[-]$	= Mathieu function joining factor
H	$[L]$	= wave height
H_M	$[L]$	= maximum wave height
H_c	$[L]$	= wave height at the coupling location
H_d	$[L]$	= diffracted wave height
H_i	$[L]$	= incident wave height
H_l	$[L]$	= wave height at the last wave gauge
h	$[L]$	= water depth
I	$[-]$	= wave intensity
i	$[-]$	= counter for i -th data sample
Je	$[-]$	= Mathieu even radial function of the second kind

K'	[-]	= diffraction coefficient
k	[L ⁻¹]	= wave number
L	[L]	= wavelength
L_M	[L]	= maximum wavelength
l_s	[L]	= landslide length
l_w	[L]	= wavefront length
M	[-]	= relative slide mass
m	[-]	= integer number
m_s	[M]	= slide mass
N	[-]	= Mathieu function normalising factor
N	[-]	= number of samples
Ne	[-]	= Mathieu even radial function of the first kind
n	[T/L ^{1/3}]	= Manning's coefficient
n	[-]	= integer number
P	[-]	= impulse product parameter
p_h	[M/LT ²]	= hydrostatic pressure
p_t	[M/LT ²]	= total pressure
q	[M/LT ²]	= non-hydrostatic pressure term
q_d	[-]	= Mathieu function fixed variable
r	[L]	= radial distance from the slide impact
r'	[L]	= radial distance from the coupling location
r_i	[L]	= impact radius
S	[-]	= relative slide thickness
Se	[-]	= Mathieu even angular function
s	[L]	= slide thickness
s_{mat}	[-]	= Mathieu function fixed variable
T	[-]	= wave type product
T	[T]	= wave period
t	[T]	= time from when the slide impacts
t'	[T]	= time from when the wave reaches the coupling location
u	[L/T]	= velocity in x' direction
\bar{u}	[L/T]	= depth averaged velocity in x' direction
\bar{u}_i	[L/T]	= incident velocity
V_s	[L/T]	= slide velocity
v	[L/T]	= velocity in y' direction
\bar{v}	[L/T]	= depth averaged velocity in y' direction
w_b	[L/T]	= velocity at the bottom in z' direction
w_s	[L/T]	= velocity at the surface in z' direction
x	[L]	= x -coordinate from the slide impact
x'	[L]	= x' -coordinate from the coupling location
x_M	[L]	= location of maximum wave amplitude
y'	[L]	= y' -coordinate
y_{num}	[-]	= numerical value
$y_{num,max}$	[-]	= maximum numerical value
$y_{num,min}$	[-]	= minimum numerical value

y_{pred}	[-]	= predicted value
z'	[L]	= z' -coordinate

772 **Greek symbols**

α	[°]	= slide impact angle
α_i	[°]	= incident wave angle
β	[-]	= pre-factor in Eqs. (13) and (14) and pre-factor for the best fit
β_E	[-]	= pre-factor in Eqs. (13) and (14) for the upper envelope
γ	[°]	= wave propagation angle from the slide impact
γ'	[°]	= wave propagation angle from the coupling location
γ'_{part}	[°]	= phase angle of the partial wave
ΔH	[L]	= terrain elevation difference
ΔL	[L]	= horizontal distance between two points
$\Delta t'$	[T]	= time difference
Δx	[L]	= distance travelled by the slide above SWL
$\Delta x'$	[L]	= x' -direction grid size and horizontal distance
$\Delta y'$	[L]	= y' -direction grid size
Δz	[L]	= contours spacing in z -direction
$\Delta \gamma'$	[°]	= wave propagation angle difference
$\delta \phi$	[rad]	= angular resolution for Mathieu function
η	[L]	= water surface elevation
η_i	[L]	= incident water surface elevation
θ	[°]	= water body side angle
θ_{rad}	[rad]	= water body side angle in radians
μ	[-]	= effective friction coefficient
ξ	[-]	= elliptic-cylinder coordinates of confocal ellipses
π	[-]	= mathematical constant
ρ_s	[M/L ³]	= slide density
ρ_w	[M/L ³]	= water density
τ	[ML ³ /T ²]	= turbulent stress
ϕ	[-]	= elliptic-cylinder coordinates of confocal hyperbolas

773 **Abbreviations**

2D	= Wave flume geometry
3D	= Wave basin geometry
CFL	= Courant-Friedrichs-Lewy
CPU	= Central Processing Unit
HPC	= High Performance Computing
MPI	= Message Passing Interface
NLSWE	= Non-Linear Shallow Water Equation
$nRMSE$	= normalised Root Mean Square Error
SPH	= Smoothed Particle Hydrodynamics
SWASH	= Simulating WAVes till SHore
SWL	= Still Water Level

774 **A. Symmetry of the numerical solution**

775 Fig. A.1 shows the symmetry of the numerical solution studied with H at
 776 $r'/h = 3.0, 5.0, 10.0, 15.0, 22.5$ and 35.0 for the 3D geometry. The H values are
 777 calculated using the water surface time series at propagation angles $\gamma' = 0^\circ$ and
 778 $\gamma' = \pm 45^\circ$ (Fig. 3f).

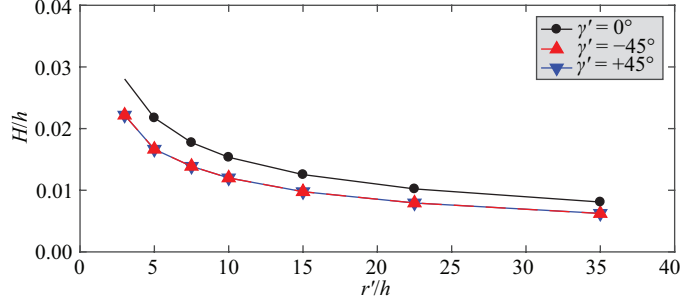


Figure A.1: Symmetry of the numerical solution in the 3D geometry. Relative wave height H/h over the relative radial distance r'/h at $\gamma' = 0^\circ$ and $\gamma' = \pm 45^\circ$.

779 **B. Diffraction theory**

780 The diffraction theory by Carr and Stelzriede (1952) was applied rather than
 781 graphical solutions (diffraction diagrams) available in the technical literature
 782 for fixed ratios b'/L between the source gap width b' and the wavelength L
 783 (e.g. Johnson, 1952; USACE, 1984). This theory was introduced by Morse and
 784 Rubenstein (1938) for diffraction of sound and electromagnetic waves at a gap
 785 into a infinite plane. This approach has an exact solution for small gaps and
 786 defines the energy distribution in function of the wave propagation angle γ' .
 787 The solution is based on elliptic-cylinder coordinates defined as

$$\begin{aligned} x' &= b'/2 \cos \xi \cos \phi \\ y' &= b'/2 \sin \xi \sin \phi \end{aligned} \quad (\text{B.1})$$

where ξ are confocal ellipses and ϕ are confocal hyperbolas (Fig. 2 in Carr and Stelzriede, 1952).

For $\phi = 0$ the hyperbolas degenerate in a straight line with a gap of width b' . The three-dimensional wave equation in elliptic-cylinder coordinates is then solved using the Mathieu function (Abramowitz and Stegun, 1964) as a method for variables separation. The solution in function of the energy intensity ratio I (Carr and Stelzriede, 1952; Morse and Rubenstein, 1938) is

$$\begin{aligned} I = \frac{H_d^2}{H_i^2} = \sum_{m,n} \frac{b'}{L} \frac{4\pi}{\sqrt{s_{mat}}} \frac{1}{N_m N_n} \sin \gamma'_{part,m} \sin \gamma'_{part,n} S e_m(s_{mat}, \alpha_i) \cdot \\ \cdot S e_n(s_{mat}, \alpha_i) S e_m(s_{mat}, \phi) S e_n(s_{mat}, \phi) \cos(\gamma'_{part,n} - \gamma'_{part,m}) \end{aligned} \quad (\text{B.2})$$

$$I_{r',\phi} = \frac{L}{r'} I \quad (\text{B.3})$$

788 where Se is the even angular Mathieu function, $s_{mat} = (\pi b'/L)^2$, α_i is the direc-
 789 tion of the wave entering the gap (Fig. B.1), ϕ is the angle from the centreline
 790 of the gap and r' the radial distance from the source. H_d is the diffracted wave
 791 height, H_i the incident wave height and the subscripts m and n are the integer
 792 number of the sum terms. Finally, γ'_{part} represents the phase angle of the partial
 793 wave and is defined as $\text{ctn}\gamma'_{part} = (Ne_n(s_{mat}, 0)/Je_n(s_{mat}, 0))$ where Ne is the
 794 even radial modified Mathieu function of the first kind and Je is the even radial
 795 modified Mathieu function of the second kind. Note that in Carr and Stelzriede
 796 (1952) the normalising factor $1/(N_m N_n)$ is missing in their representation of
 797 Eq. (B.2).

798 To solve the Mathieu function the ‘‘Mathieu functions toolbox v4.0.6’’ (Cois-
 799 son et al., 2016) for Scilab has been used allowing for a high resolution of
 800 $\delta\phi = 0.01$ rad in the final solution solving the even angular Mathieu function
 801 $ce_n(\phi, q_d)$, the even radial Mathieu function of the first kind $Ce_n(\phi, q_d)$ and the
 802 even radial Mathieu function of the second kind $Fey_n(\phi, q_d)$ where $q_d = s_{mat}/4$.
 803 Tabulated values from the National Bureau of Standards (1951) were then used
 804 to transform the three precedent solutions with the variables needed to solve
 805 the corrected theory of Carr and Stelzriede (1952) resulting in $Se_n(s_{mat}, \phi) =$
 806 $ce_n(\phi, q_d)/A_n$, $Je_n(s_{mat}, \phi) = Ce_n(\phi, q_d)/A_n g_{e,n}$ and $Ne_n(s_{mat}, \phi) = Fey_n(\phi, q_d)/A_n g_{e,n}$
 807 where A_n and $g_{e,n}$ are the joining factors.

808 Fig. B.1 shows the comparison between the calculated solution based on Eq.
 809 (B.2) and the diffraction diagram of Pos and Kilner (1987) after Johnson (1952).
 810 The x' - and y' -axes are normalised with L considering the origin of the refer-
 811 ence system at the centre of the breakwater gap. The different contours with
 812 each associated value define the wave diffraction coefficient $K' = H_d/H_i = \sqrt{I}$.
 813 Other b'/L ratios were investigated with Eq. (B.2) obtaining results with a sim-
 814 ilar match to the corresponding diffraction diagram (Johnson, 1952) as shown
 815 in Fig. B.1. This successfully validated results of the diffraction theory were
 816 applied in Fig. 11.

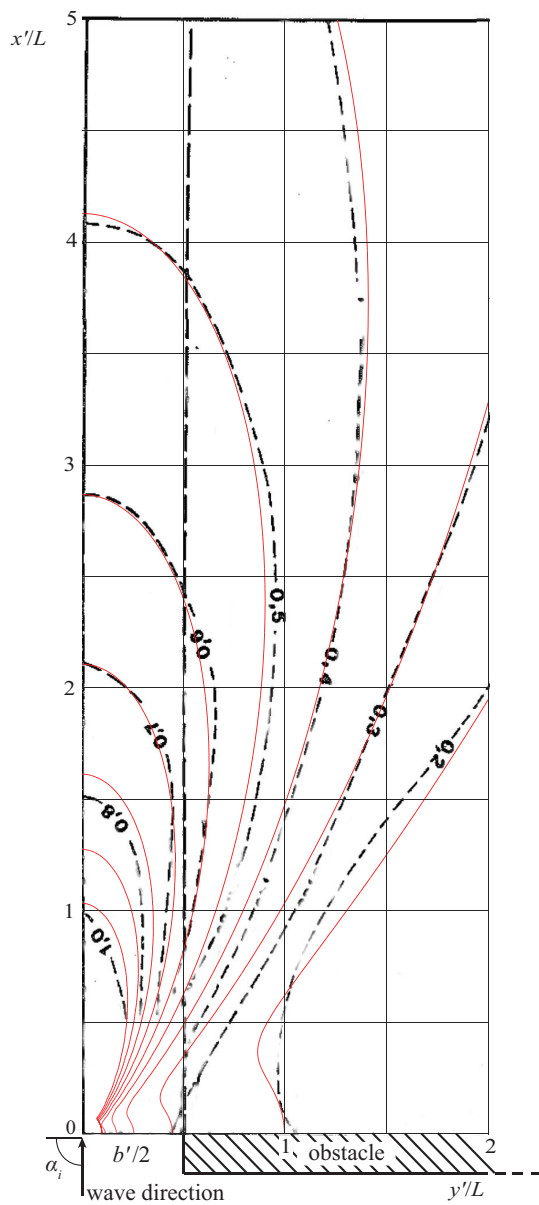


Figure B.1: Comparison of theoretically calculated diffraction solution based on Eq. (B.2) (red line) and graphical solution (diffraction diagrams) of Pos and Kilner (1987) (black dashed line) for $b'/L = 1$ and $\alpha_i = 90^\circ$.

817 **C. Amplitude decay**

818 Table C.1 shows the values of the wavefront length l_w for each wave type.
 819 Fig. C.1 shows the wave amplitude decay for each geometry and investigated
 820 wave type compared to Green's law (Eq. (12)) based on the wave amplitude a .
 821 Finally, Fig. C.2 shows the wave amplitudes for each geometry and wave type
 822 compared with Eq. (14).

Table C.1: Wavefront lengths l_w for (a) approximate linear and Stokes waves and (b) cnoidal and solitary waves based on Eq. (9).

(a) Approximate linear and Stokes waves with $h = 0.60$ m						
r'/h	2D ($\theta = 0^\circ$)	$\theta = 7.5^\circ$	$\theta = 15^\circ$	$\theta = 30^\circ$	$\theta = 45^\circ$	3D ($\theta = 90^\circ$)
3.0	0.600	1.071	1.543	2.485	3.427	6.255
5.0	0.600	1.385	2.171	3.742	5.312	10.025
7.5	0.600	1.778	2.956	5.312	7.669	14.737
10.0	0.600	2.171	3.742	6.883	10.025	19.450
15.0	0.600	2.956	5.312	10.025	14.737	28.874
22.5	0.600	4.134	7.669	14.737	21.806	43.012
35.0	0.600	6.098	11.596	22.591	35.587	66.573
(b) Cnoidal and solitary waves with $h = 0.30$ m						
r'/h	2D ($\theta = 0^\circ$)	$\theta = 7.5^\circ$	$\theta = 15^\circ$	$\theta = 30^\circ$	$\theta = 45^\circ$	3D ($\theta = 90^\circ$)
3.0	0.600	0.836	1.071	1.543	2.014	3.427
5.0	0.600	0.993	1.385	2.171	2.956	5.312
7.5	0.600	1.189	1.778	2.956	4.134	7.669
10.0	0.600	1.385	2.171	3.742	5.312	10.025
15.0	0.600	1.778	2.956	5.312	7.669	14.737
22.5	0.600	2.367	4.134	7.669	11.203	21.806
35.0	0.600	3.349	6.098	11.596	17.093	33.587

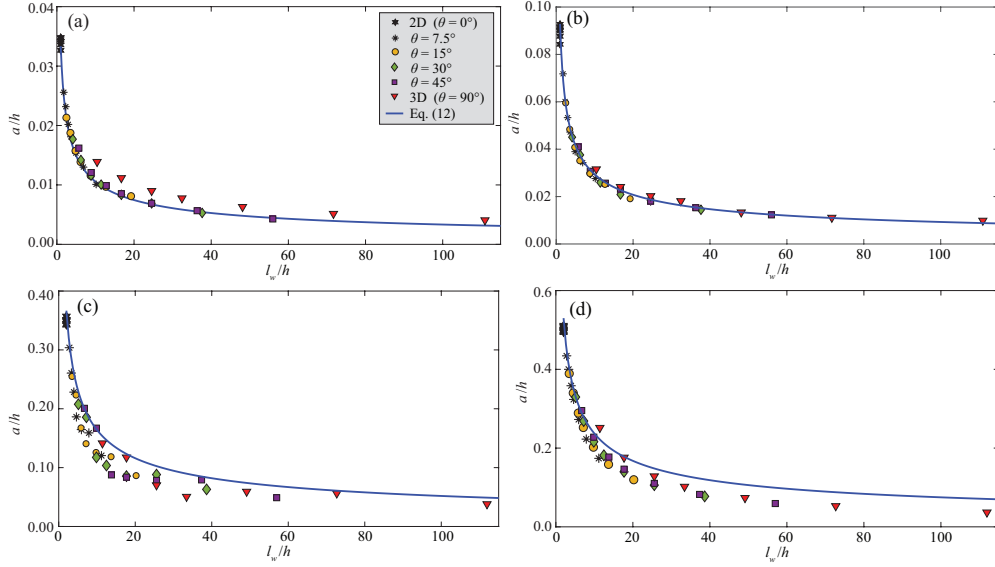


Figure C.1: Wave amplitude decay in all investigated geometries for (a) approximate linear waves, (b) 5th order Stokes waves, (c) 5th order cnoidal waves and (d) 1st order solitary waves compared to Eq. (12).

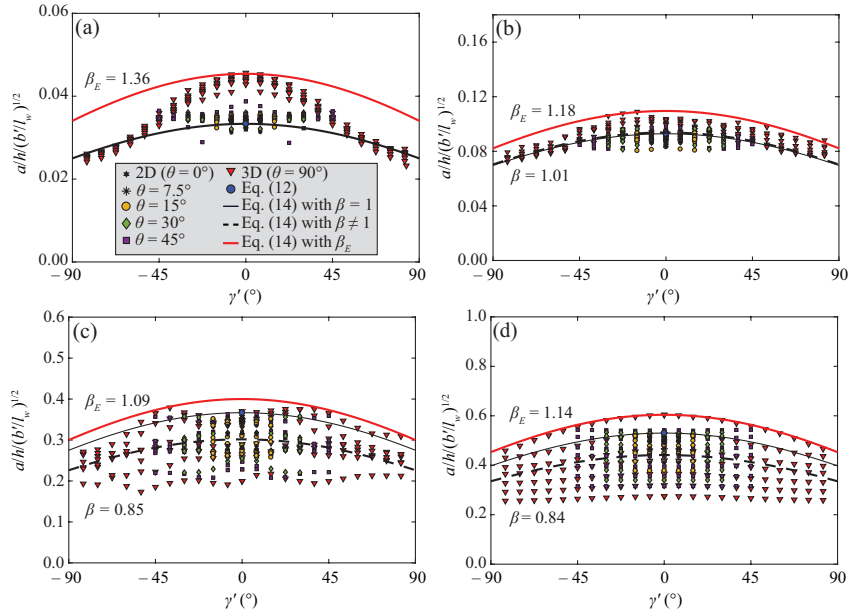


Figure C.2: Lateral wave amplitude decay for (a) approximate linear waves, (b) 5th order Stokes waves, (c) 5th order cnoidal waves and (d) 1st order solitary waves for all investigated geometries, compared to Eq. (14).

823 **D. Lateral spread for approximate linear, cnoidal and solitary waves**

824 The lateral wave decay for the approximate linear, cnoidal and solitary waves
 825 is presented here with Fig. D.1 showing the wave heights for the approximate
 826 linear waves, Fig. D.2 for cnoidal waves and Fig. D.3 for solitary waves. The
 827 cnoidal waves shown in Fig. D.2, especially for $\theta > 15^\circ$ (Fig. D.2c-f), show a
 828 convex shape with slightly higher wave heights near the side walls. Although
 829 this differs from the trend shown in Fig. 12, similar convex trends were observed
 830 in the experiments of Heller et al. (2012). The same convex shape is found for
 831 the solitary wave (Fig. D.3d,e) for $\theta = 30^\circ$ and $\theta = 45^\circ$.

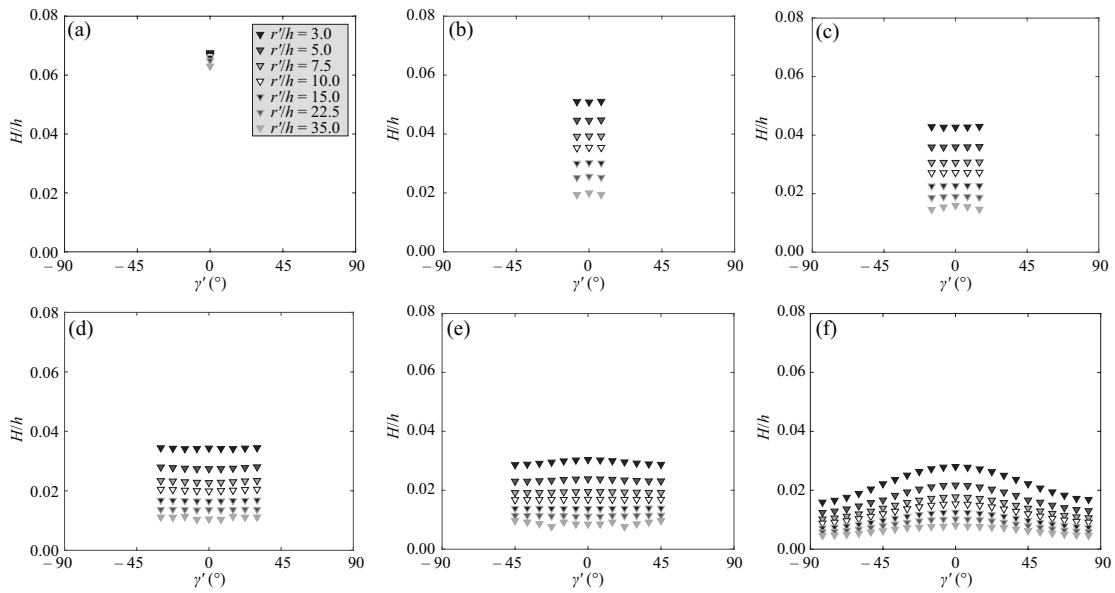


Figure D.1: Relative wave heights H/h for approximate linear waves in intermediated waters as a function of the propagation angle γ' and the relative radial distance r'/h for (a) 2D ($\theta = 0^\circ$), (b) $\theta = 7.5^\circ$, (c) $\theta = 15^\circ$, (d) $\theta = 30^\circ$, (e) $\theta = 45^\circ$ and (f) 3D ($\theta = 90^\circ$).

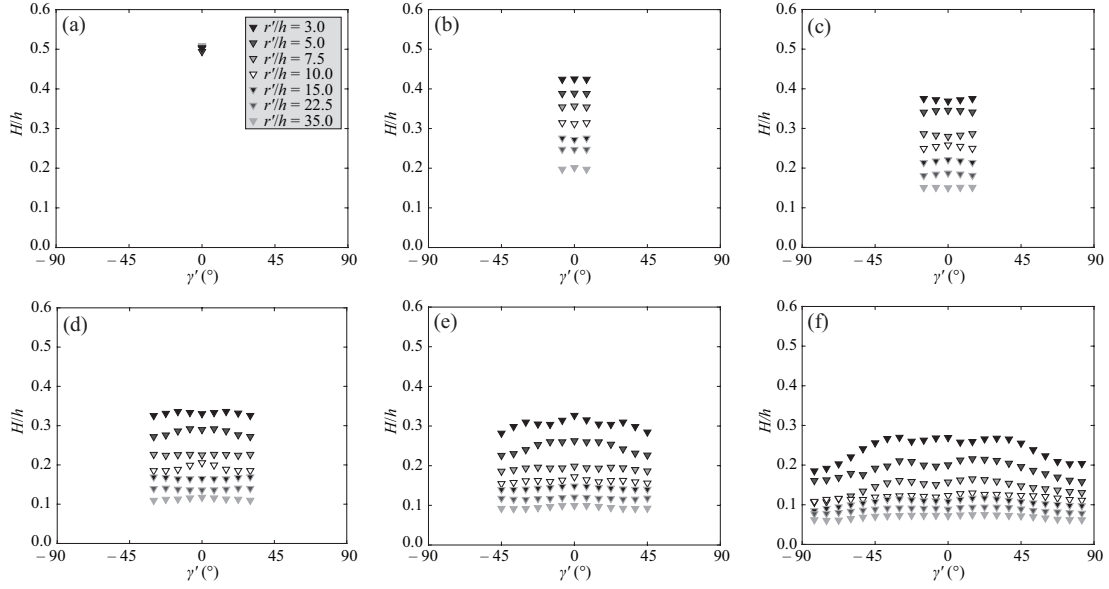


Figure D.2: Relative wave heights H/h for 5th order cnoidal waves as a function of the propagation angle γ' and the relative radial distance r'/h for (a) 2D ($\theta = 0^\circ$), (b) $\theta = 7.5^\circ$, (c) $\theta = 15^\circ$, (d) $\theta = 30^\circ$, (e) $\theta = 45^\circ$ and (f) 3D ($\theta = 90^\circ$).

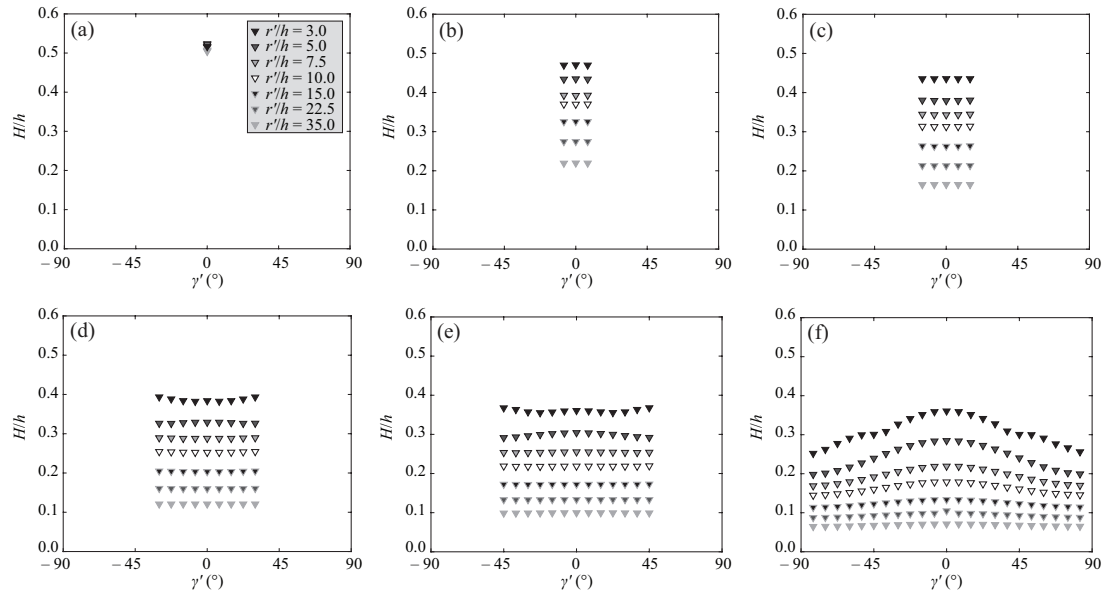


Figure D.3: Relative wave heights H/h for 1st order solitary waves as a function of the propagation angle γ' and the relative radial distance r'/h for (a) 2D ($\theta = 0^\circ$), (b) $\theta = 7.5^\circ$, (c) $\theta = 15^\circ$, (d) $\theta = 30^\circ$, (e) $\theta = 45^\circ$ and (f) 3D ($\theta = 90^\circ$).

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