A simple method to measure the temperature and levitation height of devices rotating at cryogenic temperatures

Cite as: Rev. Sci. Instrum. **91**, 045118 (2020); https://doi.org/10.1063/5.0005498 Submitted: 21 February 2020 . Accepted: 06 April 2020 . Published Online: 27 April 2020

Paolo de Bernardis (10), Fabio Columbro (10), Silvia Masi (10), Alessandro Paiella (10), and Giovanni Romeo (10)







ARTICLES YOU MAY BE INTERESTED IN

A levitated magnetic dipole configuration as a compact charged particle trap Review of Scientific Instruments 91, 043507 (2020); https://doi.org/10.1063/1.5142863

Fast switching coil system for sample premagnetization in an unshielded ultra-low-field nuclear magnetic resonance experiment

Review of Scientific Instruments 91, 045119 (2020); https://doi.org/10.1063/5.0003882

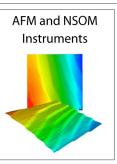
An innovative experimental device for borehole ballooning

Review of Scientific Instruments 91, 046103 (2020); https://doi.org/10.1063/1.5139950













A simple method to measure the temperature and levitation height of devices rotating at cryogenic temperatures

Cite as: Rev. Sci. Instrum. 91, 045118 (2020); doi: 10.1063/5.0005498 Submitted: 21 February 2020 • Accepted: 6 April 2020 •







Published Online: 27 April 2020

and Giovanni Romeo³

Paolo de Bernardis, 1.2 D Fabio Columbro, 1.2 D Silvia Masi, 1.2.a) Alessandro Paiella, 1.2 D







AFFILIATIONS

- Dipartimento di Fisica, Sapienza Universitá di Roma, P.le A. Moro 2, 00185 Roma, Italy
- ²INFN, Sezione di Roma, P.le A. Moro 2, 00185 Roma, Italy
- ³Istituto Nazionale di Geofisica e Vulcanologia, Via di Vigna Murata 605, 00143 Roma, Italy

a) Author to whom correspondence should be addressed: silvia.masi@roma1.infn.it

ABSTRACT

We describe a simple system to measure the temperature and levitation height of levitating cryogenic devices in rotation. Devices of this kind are the half-wave-plates rotating on superconducting magnetic bearings used in several cryogenic polarimeters for the cosmic microwave background. The temperature measurement is important to monitor the radiative background and potential systematic effects in the polarimeter. In our implementation, the temperature sensor is a thermistor, physically mounted on the rotating device. The sensor is biased with an AC current, which is transferred from the stationary electronics to the rotating device via capacitive coupling. The levitation height sensor is a network of capacitors, similar to the one used for the capacitive coupling of the thermistor. We describe the optimization of the readout system and its performance, which has been tested on a room-temperature prototype. We show that this system reaches an accuracy better than 3% for the measurement of the thermistor resistance and an accuracy of ~10 µm for the measurement of its levitation height.

Published under license by AIP Publishing. https://doi.org/10.1063/5.0005498

I. INTRODUCTION

Modern measurements of Cosmic Microwave Background (CMB) polarization use large-throughput arrays of transition edge sensors (TESs)²⁻⁵ or kinetic inductance detectors (KIDs)⁶⁻⁹ operating in a cryogenic environment. The detectors are cooled to sub-K temperature to maximize their sensitivity, and the optical components of the polarimeter are also cooled to reduce the radiative loading on the detectors and minimize systematic effects. A Stokes polarimeter uses a rotating half-wave-plate (HWP) and a polarizer to modulate the linearly polarized component. The HWP temperature should also be minimized. This is very important, in particular, for space-based experiments (such as LiteBIRD¹⁰), where the thermal emission of the HWP can load the detectors, increase their photon-noise budget (basically limited by the CMB brightness), and produce modulation-synchronous effects (see Refs. 11 and 12 for a

discussion). For these reasons, the temperature of the HWP should be kept lower than 10-20 K, depending on the frequency of operation of the detectors. Similar arguments with relaxed requirements are applicable to balloon-borne (such as LSPE-SWIPE¹³) and ground-based (such as QUBIC¹⁴) experiments. Superconducting magnetic bearings provide a nearly frictionless, fast rotation of the HWP, perfectly compatible with the cryogenic implementation of the Stokes polarimeter. 15–18 The HWP assembly levitates and rotates in the magnetic field produced by the interaction of a permanent magnet in the rotor and a set of static superconducting bulks, reaching a mechanical rotation speed $f_o \sim$ a few Hz and modulating the polarized signal at $\sim 4f_o$.

In this configuration, however, there is no mechanical contact between the HWP and the rest of the system. Any power dissipation (for example, due to eddy currents) or absorbed power (for example, due to the radiative load from the external environment) raises the

temperature of the rotating assembly and the HWP, which can cool down only radiatively. At low temperatures, radiative cooling of the HWP is not effective, so the power dissipation on the rotor should be carefully minimized. In Fig. 1, we show the results of a simulation, performed with Comsol Multiphysics, ¹⁹ of the temperature of a rotating metal-mesh HWP mounted on an aluminum rotor and surrounded by a 5 K environment. The simulation allows for thermal gradients in the plastic HWP (the conductivity of the very thin metal meshes is neglected). The temperature is monitored in the center of the HWP, while the gradient within the HWP itself is negligible (\lesssim 10 mK). We assume 0.02 HWP emissivity, flat in the relevant frequency band, while we assume to have blackened (emissivity ~0.5) the cryostat-side of the aluminum ring to favor cooling. The heating power comes from the radiation of the surrounding environment (2.7 K sky and 5 K cryogenic system) and from the eddy currents produced by the driving coil currents. With these assumptions, the total expected heat load is ~0.1 mW, evenly distributed over the edge of the aluminum ring. We also considered more pessimistic cases (0.2 mW and 0.5 mW, see Ref. 20 for details). From Fig. 1, it is evident that such small power inputs can produce a HWP temperature rise of a few K to tens of K, resulting in an increased radiative load on the detectors, photon noise, and spurious synchronous signals.

For this reason, it is very important to monitor the temperature of the HWP using precise measurements. In the case of a contact-less rotor, one way to measure the temperature of the HWP is by monitoring its thermal emission. There are two basic ways of implementing such a measurement. The first one is to measure directly the emission of the optical device, provided it is sufficiently emissive at the measurement wavelength and in the temperature range of interest. Since the temperature of the HWP is expected to be <20 K, its thermal emission will be very weak for wavelengths much shorter than 150 μ m. Monitoring the emission at wavelengths longer than 150 μ m is also difficult, since the materials currently used in HWPs for CMB measurements (sapphire or polyethylene embedding thin

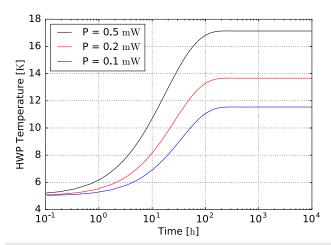


FIG. 1. Simulation of the temperature of a levitating rotating metal-mesh HWP (300 mm diameter, which is the range of interest for the HWP of the LiteBIRD experiment ^{10,21}), radiatively heated with three different levels of input power, starting from a base temperature of 5 K. See the text for details.

metal meshes) have low emissivity at wavelengths longer than 150 μ m. In this case, it is difficult to modulate the thermal emission to be measured. The second approach is to blacken, e.g., two quarter sectors of the ring supporting the HWP optical device and make the other two quarter sectors reflective. The detector can look at the rotating ring, measuring the modulated signal produced alternating the emissive and reflective quarters of the ring. If the reflective sectors reflect a stable background, the amplitude of this signal will depend on the temperature of the support ring, which might be considered a good proxy of the temperature of the HWP. The blackened sectors of the ring will also help to cool down the rotating HWP assembly. The signal detected with a reasonable throughput (0.2 cm² sr) and optical bandwidth (20%) at a sensing wavelength of, e.g., 1.4 mm is in the 1-100 pW range for temperatures between 3 K and 20 K. For a precision measurement, sensitive detectors are required, especially at the lowest edge (~3 K) of the temperature range.

Here, we describe a simpler, cost effective, reliable method to measure the temperature of the rotating assembly, avoiding the use of such a complex detection system. This is based on a regular thermistor, mounted on the rotating assembly. The thermistor is capacitively coupled to the steady readout system and biased with an AC current.

A simple extension of the method also allows for monitoring the distance of the rotor with respect to the stator along the rotation axis, i.e., its levitation height. This is also a very important parameter of the system, and since the coupling capacitor capacitance is a strong function of the distance between the plates, the proposed measurement system will also serve efficiently to this purpose.

In the following, we describe the measurement system, its optimization, and its performance. In Sec. II, we describe the capacitively coupled readout of the thermistor and of the rotor levitation height, including the general design and the optimization of the electronics. In Sec. III, we describe the results of a validation of the method, carried out using a room-temperature 600 mm diameter rotating disk as a stand-in for the cryogenic half-wave plate rotor. In Sec. IV, we summarize and discuss the results.

II. THE CAPACITIVELY COUPLED THERMISTOR

A. Practical implementation

The block diagram of the proposed system is shown in Fig. 2. A regular thermistor for cryogenic temperature measurements $[RuO_2$ resistor, CERNOX TM (Ref. 22), or similar, with resistance values ranging between $500~\Omega$ and $50~k\Omega]$ is mounted on the rotary assembly. Each contact of the thermistor is connected to one pole of a plane capacitor, i.e., a simple rectangular copper pad (10 mm wide \times 50 mm long, see below) mounted on the rotating assembly. The other pole of the same capacitor is similar and is mounted on the stator. At a certain angle of the rotation of the HWP, the two poles of both capacitors will align one on top of the other, with a gap of $\sim\!\!1$ mm between the poles, thus creating two capacitors. Each capacitance can be computed as

$$2C = \epsilon_0 \frac{A}{d} \sim 4.4 \text{ pF}. \tag{1}$$

The steady pole of the first capacitor is connected to an AC voltage generator, while the steady pole of the second capacitor

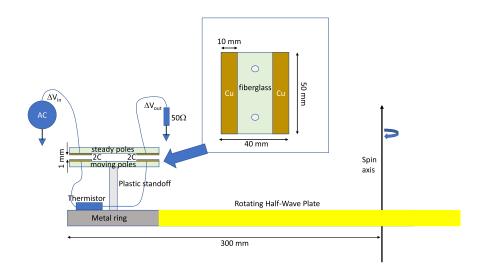


FIG. 2. Schematic diagram of the temperature and distance measurement concept. The dimensions refer to the room-temperature demonstration mock-up (600 mm diameter) where the HWP was replaced by an inertially equivalent aluminum disk rotating on a low-friction ball-bearing.

is connected to a low-value load resistor ($R_L \sim 50~\Omega$) closing the circuit to ground. When the poles are aligned, an AC current flows through the thermistor with an amplitude depending on its resistance R, which, in turn, depends on its temperature [R = R(T)].

The sizing of the capacitor poles and their separation is a tradeoff between different needs. The distance between the moving and steady poles (nominally 1-2 mm) is a tradeoff between the need of maximizing the capacitance and the need to operate in a relatively wide range of levitation heights and to cope with the small height drop expected when the rotor is released from its clamping device. We have to limit the global size of the sensor to accommodate it above the rotor ring and within the shields protecting the optical beam crossing the HWP. On the other hand, a large area of the poles would produce a large capacitance and thus a large transmitted signal. It would also produce a wider signal peak when the steady and moving poles align: this would make it easier to properly sample it and evaluate its maximum amplitude. For simplicity of implementation, we accommodated the steady poles of the input and output capacitors on the same printed circuit board (PCB); the same layout has been used for the moving poles. A large distance between the two poles on the same PCB would reduce the parasitic capacitance (see below). In our prototype, the best tradeoff was found for rectangular poles, 10 mm wide × 50 mm long, separated by a 20 mm gap.

Parasitic capacitances are present in the setup sketched in Fig. 2. Since two poles of different capacitors are present on the same PCB, there is a parasitic capacitance between these poles, C_{pB} for the steady poles and C_{pT} for the moving poles. Its effect is to transfer part of the bias signal directly from the input to the output without biasing the thermistor. The 20 mm distance between the poles reduces this parasitic capacitance to ~1 pF, assuming $\epsilon_r = 4.4$ for the PCB material. This applies to both the input and output poles of the steady capacitors and to the input and output poles of the moving capacitors, where C_{pT} is in parallel to the thermistor. In an optimized implementation, we can reduce C_{pT} and C_{pB} by a factor of ~4 using separate standoffs for the input and output poles. In any case, in the

analysis of the capacitively coupled thermistor, C_{pB} and C_{pT} are not negligible with respect to 2C.

From Eq. (1), it is immediately evident that the capacitance is a strong function of the distance between the poles. Hence, the amplitude and phase of the signal transferred to the rotating assembly via the capacitors will be a function of the levitation height. This means that we have to disentangle the two effects (changes in thermistor resistance and changes in levitation height). This can be done by doubling the moving sets of capacitor poles. We will use one set of capacitor poles to bias the thermistor connected between them (thermistor network) and the other one to bias a metal wire, with negligible resistance, connected between the two moving poles (reference network). The amplitude of the signal of the reference network depends only on the levitation height, allowing a measurement of it and a correction of measurements of the thermistor network. We discuss these issues in Sec. III.

B. Basic circuit analysis and optimization

The equivalent circuit of the capacitively coupled thermistor is reported in Fig. 3.

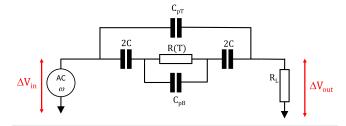


FIG. 3. Equivalent circuit of the temperature measurement. The excitation ΔV_{in} is produced by a voltage generator at frequency $f=\omega/(2\pi)$. The rotating capacitors have capacitance 2C; R(T) is the thermistor resistance; C_{pT} is the parasitic capacitance between the steady poles of the two capacitors; C_{pB} is the parasitic capacitance between the rotating poles of the two capacitors; and R_L is the load resistor.

The transfer function for the circuit in Fig. 3 can be written as

$$\frac{\Delta V_{out}}{\Delta V_{in}} = \frac{1}{1 + \frac{Z}{R_I}},\tag{2}$$

where ΔV_{out} and ΔV_{in} are the measurement and drive voltage, respectively, $R_L \sim 50~\Omega$ is the load resistor, and Z is the combined impedance of the network of horizontal components in Fig. 3. We obtain

$$Re(Z) = \frac{R(T)}{(1 + C_{pT}/C)^2 + \omega^2 R^2(T) C_p^2},$$
 (3)

$$\operatorname{Im}(Z) = -\frac{1}{\omega C} \frac{\left(1 + C_{pT}/C\right) + \omega^2 R^2(T)(C + C_{pB})C_p}{\left(1 + C_{pT}/C\right)^2 + \omega^2 R^2(T)C_p^2},$$
 (4)

$$C_p = C_{pB}(1 + C_{pT}/C) + C_{pT},$$
 (5)

where $\omega = 2\pi f$ is the angular frequency of the drive signal.

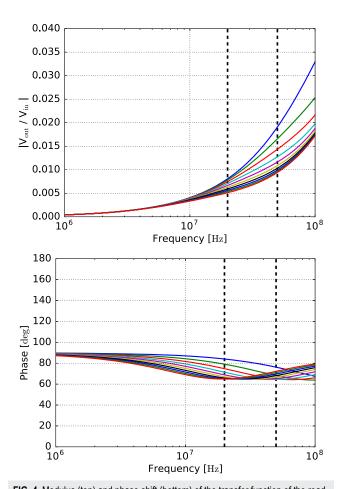


FIG. 4. Modulus (top) and phase shift (bottom) of the transfer function of the readout circuit for thermistor values between 1 k Ω (top line) and 10 k Ω (bottom line) in 1 k Ω steps. The optimal frequency range of operation (significant and roughly equalized response to thermistor resistance variations) is approximately bracketed by the two dashed lines.

The modulus and phase shift of the transfer function are plotted in Fig. 4 for a thermistor resistance R(T) ranging from 1 k Ω to 10 k Ω , a coupling capacitance 2C=1 pF (a value expected for a distance of ~4 mm between the steady and moving poles in our prototype), a parasitic capacitance between the steady poles of the two capacitors $C_{pT}=0.3$ pF, and a parasitic capacitance between the rotating poles of the two capacitors $C_{pB}=0.3$ pF (as expected using separate standoffs for the two poles).

From Fig. 4, it is evident that for the typical values of the components considered here, the optimal excitation frequency is in the 20–50 MHz range, where the output signal excursion is significant and roughly equalized. This frequency range also has the advantage of being significantly higher than the typical bias frequency of frequency-domain multiplexed TES (~1 MHz) and significantly lower than the typical bias frequency of KID (~1 GHz) so that the crosstalk between this signal and CMB detector signals is minimized.

The expected non-linear relation between the resistance of the thermistor and the output signal is shown in Fig. 5.

With an excitation amplitude of 1 V_{rms} , the output signal is in the range of 10 mV $_{rms}$. However, in the range of temperatures of interest here, the rms voltage across the thermistor must be limited below 0.01 V_{rms} to avoid self-heating of the thermistor. This requires an excitation amplitude of the capacitor–thermistor network smaller than 1 V_{rms} , as shown in Fig. 6. For example, at 25 MHz, for an excitation amplitude of 50 mV $_{rms}$, we have a signal across the thermistor of $\sim\!10$ mV $_{rms}$ and a power dissipation in the thermistor of $\sim\!100$ nW. This adds negligible heating in the thermistor and in the rotor. Note also that the biasing is intermittent, further reducing the heat load. The small excitation, however, results in very small (order of 0.3 mV $_{rms}$) output signals across the load resistor of Fig. 3. For this reason, a custom readout scheme has been developed, as described below.

C. Excitation and readout circuit

In the simplest implementation, the excitation signal is obtained from a 25 MHz digital clock, which is filtered by a resonant circuit to obtain a sine-wave. We prefer to remove the higher

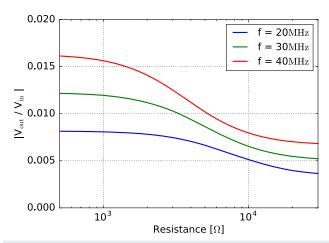


FIG. 5. Expected output voltage as a function of the thermistor resistance for excitation frequencies f = 20 MHz. 30 MHz. and 40 MHz (bottom to top lines).

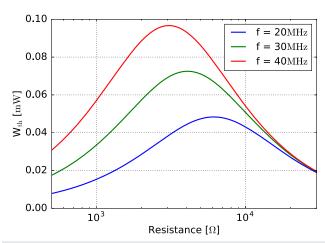


FIG. 6. Expected power dissipated in the thermistor, as a function of the thermistor resistance, for excitation frequencies f = 20 MHz, 30 MHz, and 40 MHz (bottom to top lines) for a 1 V_{rms} excitation amplitude. The power scales as the square of the excitation voltage and must be reduced to avoid self-heating of the thermistor.

harmonics present in the original square-wave, since they produce large spikes through the capacitor-thermistor network of Fig. 3, which are difficult to model due to the presence of stray capacitance and uncertainties in the high frequency gain of the active components in the following signal recovery chain. Having a pure tone would also minimize the crosstalk between this signal and the signals from the CMB detectors. The sine-wave signal is equally split between two lines using a simple SMA (SubMiniature version A) tee adapter. One line is used to bias the capacitively coupled thermistor, and the other is read by an amplitude monitor. The tone supplying the capacitively coupled thermistor is reduced in amplitude by means of a -20 dB, $50~\Omega$ SMA coaxial attenuator to obtain the excitation signal ΔV_{in} and connected via a 50 Ω , 2 m long stainless steel coaxial cable to the capacitor-thermistor network. This results in an excitation across the thermistor $\Delta V_{\it th} \sim 10$ mV $_{\it rms}$. The signal across the load resistor is connected via a 50 Ω , 2 m long coaxial cable to the input of a low-noise amplifier, based on a Mini-Circuits MAR-8 MMIC²³ module, with gain ~30 dB. The output is low-pass filtered and sent to an RF-to-rms converter based on an Analog Devices AD8361²⁴ chip. The DC output of the AD8361 is amplified by a factor of 10 and digitized. In the amplitude monitor, a -10 dB, 50 Ω SMA coaxial attenuator adapts the signal level to the input of a second RF-to-rms converter, used to monitor any change in the excitation amplitude. The block-diagram of the readout electronics is shown in Fig. 7.

The output of this readout circuit has a significant offset due to the parasitic capacitance and the rms value of the noise of the thermistor and amplifier but is usable anyway if the noise level is stable (i.e., if external noise and radio-frequency interference (RFI) sources do not couple significantly to the capacitor-thermistor network).

In Fig. 8, we plot the measured response of the readout circuit to different values of the thermistor resistance. The measurement has been carried out by replacing the thermistor with different fixed-value precision resistors.

In the previous analysis, we have neglected the effect of resistive losses in the coaxial cables. Low heat conductivity stainless steel coaxial cables, few meters long, have a high resistance of the order of a few 100 Ω . This is of the same order of the impedance of the coupling capacitors at our readout frequency and of the order of the resistance of the thermistor at the lowest temperatures. Moreover, its value changes with temperature from room-temperature to cryogenic temperatures, so it cannot be easily calibrated out using room-temperature measurements alone. If not properly taken into account, the change in resistive losses can produce a systematic error in the measurement of the temperature of 10%-20% in the low-edge of the temperature range. On the other hand, at variance with ~DC measurements, 4-wire measurements are difficult to carry out at these frequencies due to the need of terminating all the coaxial lines with 50 Ω matched loads, implying that the readout lines cannot be of high impedance. For all these reasons, our approach is to use an additional reference network, measuring a stable capacitor, with the same capacitance as the moving capacitors. The stable capacitor is read by means of a couple of coaxial lines identical to the ones used for the temperature and levitation height measurements and using the same generator and RF level meter used for the other measurements. The output signal from this channel will depend only on the losses in the coaxial cables and can be used to normalize out the effect of their temperature-driven changes.

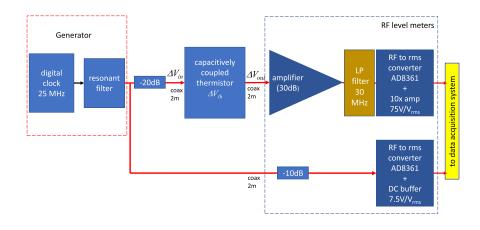


FIG. 7. Block-diagram of the simplest excitation and readout scheme. All components other than the capacitively coupled thermistor are shielded and operated at room-temperature. The thermistor and its coupling capacitors operate at cryogenic temperatures (few K).

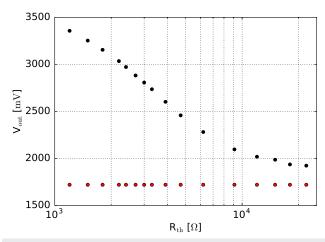


FIG. 8. Measured response of the readout circuit shown in Fig. 7 to different values of the thermistor resistance (black dots). For these measurements, we replaced the thermistor with a set of fixed-value precision resistors. The measurement frequency is 25 MHz. The red dots represent the measured values of the excitation amplitude monitor output. If the thermistor is a CERNOXTM model CX-1050, resistance values between 1 kΩ and 10 kΩ correspond to temperatures between ~10 K and ~2 K, which is the range of interest for the HWP of the LSPE¹³ and QUBIC²⁵ experiments.

The output noise of the readout circuit depends on the Johnson noise of the thermistor, on the noise of the amplifier, and on the electromagnetic interference (EMI) on the capacitive sensor. For a 50 Ω load resistor, the Johnson voltage noise is $\sqrt{4k_BTR} \sim 1 \text{ nV}/\sqrt{\text{Hz}}$. Given the small value of the source resistance, the current noise of the amplifier is negligible, while the voltage noise of the amplifier is $\sim 1 \text{ nV}/\sqrt{\text{Hz}}$. Over a bandwidth $\Delta f \sim 30 \text{ MHz}$, with a gain $G \sim 30$, the standard deviation of the output of the amplifier is rms $\sim 0.2 \text{ mV}_{\text{rms}}$. The RF-to-rms converter operates with a time constant $\tau \sim 20 \ \mu\text{s}$ and with a gain $G_c \sim 7.5 \text{ V/V}_{\text{rms}}$, and an additional gain $G_a = 10 \text{ is provided}$ by the output amplifier. The minimum fluctuation of the output of the readout circuit is thus $\sigma_{out} = G_c G_a \times rms/\sqrt{2\tau\Delta f} \sim 0.5 \text{ mV}_{\text{rms}}$.

The average value of the output due to the bias signal is of the order of several hundreds of mV_{rms} to $\sim\!2~V_{rms},$ resulting in an expected signal-to-noise ratio much larger than 100, if the interference is negligible.

We have tested the previous forecast acquiring the output of the readout with a 24-bit analog-to-digital (A/D) converter. The measured rms fluctuation is consistent with the expected value when the capacitor network is well shielded in a grounded metal box. Such a configuration is representative of the operation of the sensor inside the metal cryostat of a CMB polarimeter.

When operated in the laboratory, outside the metal shielding, the system is sensitive to the position with respect to the rotator and the environment and also to cell-phones and computer-generated electromagnetic interference (EMI). These effects limit the performance of the system in the measurements reported below, which, nonetheless, reach an acceptable performance level.

The improved performance of the readout and reduced sensitivity to EMI might be obtained by reducing the bandwidth at the

amplifier output, e.g., replacing the low-pass filter in Fig. 7 with a resonant filter. In order to avoid thermally driven mismatches between the filter response and the generator frequency, a lockin demodulation might be used. We leave this to future developments, since even for the simple readout circuit described above, the readout noise is not the limiting factor, as we show below.

III. MEASURED PERFORMANCE

We tested the performance of the measurement method using a room-temperature mock-up, where the levitating rotor is replaced by a 600 mm diameter aluminum disk rotating on a low-friction ball-bearing, and the thermistor has been simulated using resistors with values spanning the expected range $R_{th} \sim 1~{\rm k}\Omega - 10~{\rm k}\Omega$. The rotor driver, based on steady coils pushing or pulling on permanent magnets on the disk, and the strong levitation magnet of the superconducting magnetic bearing are the same as for the cryogenic device. As explained at the end of Sec. II A, we have a reference network for levitation height measurements and a thermistor network for temperature measurements. In the following, we describe the measurements we carried out with the room-temperature mock-up for both networks.

A. Distance measurements

The capacitance 2C of the coupling capacitors depends on the distance between the steady and moving capacitor poles [Eq. (1)], which depends directly on the levitation height of the rotor. In the reference network, the two coupling capacitors are simply connected in series by a short conductor replacing the thermistor and connecting the two rotating poles. As a result, the amplitude and phase of the transmitted signal depend only on the levitation height. During the rotation of the rotor, the steady capacitor poles will sequentially face the moving poles of the thermistor network capacitors and the moving poles of the reference network capacitors. Hence, the output of the readout chain will monitor in close sequence the thermistor resistance and the distance between the poles.

In Fig. 9, we report sample records of the raw readout output for a system with four networks. Here, two thermistors with resistances of 10 k Ω and 4.7 k Ω , spaced by 180° in azimuth, are mounted on the rotor. Each thermistor network is followed by its reference network. The measurement has been repeated for different values of the distance h between the moving capacitor poles and the steady capacitor poles while the rotor is spinning at ~40 rpm. Note that at this spin rate, the signal peak is ~75 ms wide. This is much longer than the integration time of the RF-to-rms converter (~ 20 μs), thus allowing for much faster spin rates without any significant degradation of the peak height.

The data demonstrate that the reference network allows for a good measurement of the distance between the poles. If we assume a distance between the capacitor poles of 1 mm, the system has a resolution $dV/dh \sim 1.6 \text{ V mm}^{-1}$, while for a distance of 2 mm, the resolution is $dV/dh \sim 0.75 \text{ V mm}^{-1}$.

Note that the measured rms fluctuation of the readout output σ_M is several mV rms larger than the one expected from the Johnson and amplifier noise alone. This means that significant perturbations arise from the unshielded operation and the stray capacitance variations with respect to the surrounding environment.

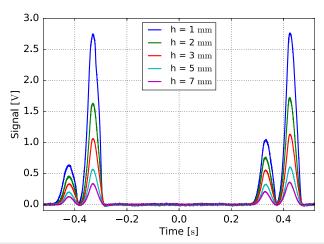


FIG. 9. Sample records of the readout output while the rotor was spinning at 40 rpm. The four peaks (left to right) correspond to the first thermistor network (R_{th} = 10 k Ω), its reference capacitor, a second thermistor network (R_{th} = 4.7 k Ω), and its reference capacitor. The reference capacitors provide an effective way to estimate the distance between the capacitor poles, which depends on the vertical position of the levitating rotor.

Using anyway the measured noise, we can also compute the error in the measurement of the levitation height,

$$\sigma_h = \frac{dV}{dh}\sigma_M. \tag{6}$$

We find that variations of the height as small as $\sigma_h \sim 6 \ \mu m$ and $\sigma_h \sim 13 \ \mu m$ for distances h of 1 mm and 2 mm, respectively, can be detected reading the reference capacitive networks.

Note that, in principle, any tilt of the rotor (which might introduce systematic effects in high precision applications; see, e.g., Ref. 26) could be dynamically sampled by replicating the readout chain and the assembly of static poles in three replicas separated by 120° in azimuth.

B. Temperature measurements

The *thermistor network* is sensitive to both temperature changes and levitation height changes. The distance measurements from the reference network described in Sec. III A can thus be used to correct the effect of distance fluctuations in the measurements of the *thermistor network*.

In order to check the effectiveness of the method, we normalize the peak signal of each thermistor network to the peak signal of its *reference network* and plot in Fig. 10 their ratios. Regardless of the distance between the capacitor poles, the ratio remains approximately constant, confirming the effectiveness of the correction method.

The measured output signal noise σ_M is readily converted into an error in the temperature measurement, once the $R_{th}(T)$ characteristic of the thermistor is defined,

$$\Delta T = \frac{dT}{dR} \sigma_R = \frac{dT}{dR} \frac{dR}{dV} \sigma_M, \tag{7}$$

where the first derivative is estimated from the calibration curve of the thermistor $R_{th}(T)$, while the second derivative is estimated

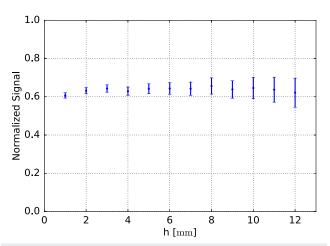


FIG. 10. Ratio between the peak signals of two thermistor networks ($R_{th} = 4.7 \text{ k}\Omega$ and $R_{th} = 10 \text{ k}\Omega$), each normalized to the peak signal of its reference network, plotted for a wide range of distances between steady and moving capacitor poles.

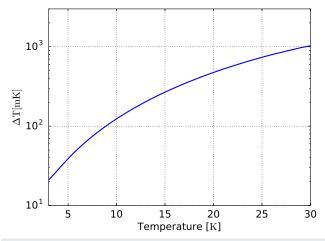


FIG. 11. Error on the measured temperature, estimated for a CX-1050 sensor read through the readout circuit described in the text.

from the calibration data $V(R_{th})$ of Fig. 8. In Fig. 11, we plot ΔT for a CERNOXTM CX-1050 temperature sensor. Since the measured σ_M does not depend on the value of the thermistor resistance, the behavior of ΔT vs rotor temperature is due to the combination of the thermistor resistance $R_{th}(T)$ becoming steeper for lower temperatures and the $V(R_{th})$ of the readout circuit mildly decreasing for the correspondingly larger resistances. The relative error remains smaller than 3% in the entire temperature range of interest.

IV. CONCLUSIONS

We have designed, built, and tested a device able to sense the temperature and position of a levitating rotor during its fast rotation at cryogenic temperatures. The measurement is based on regular thermistors, mounted on the rotor, periodically and briefly biased by a high-frequency AC current through a capacitive network.

We have demonstrated the correct operation of the capacitive readout in a room-temperature real-world environment. We included the electromagnetic interference of the rotor driver coils and of the levitation magnet and even variable capacitive coupling to the surrounding environment. The latter will arguably be absent in the cryogenic operation inside a grounded cryostat shell. The presence of varying capacitive coupling toward the surrounding environment results in increased output fluctuations with respect to the ones due to resistors and amplifier noise, but the resulting noise is sufficiently small to permit measurements of the temperature at precisions required for upcoming experiments.

An alternative inductive coupling between the rotating thermistor and the static readout system, while, in principle, possible and effective, would be severely affected by the magnetic interference from the driving coils.

We do not expect any change in the performance of the measurement setup when cooled to cryogenic temperatures. The coaxial cables we used have the same dimensions and length as those that will be used in the cryogenic setup, and we do not use any electronic component near the capacitive networks that are intrinsically temperature-independent.

Using a CX-1050 CERNOXTM thermistor, the error in the measured resistance converts into an error in the temperature smaller than 3% for the 2-30 K temperature range of interest for the levitating HWPs of cryogenic CMB polarimeters.

Reference capacitive networks read through the same circuit allow for precision measurements of the levitation height of the rotor with a resolution of $\sim 10 \ \mu m$. This provides an important diagnostic of the dynamics of the rotor and allows for corrections of the thermistor resistance measurement fluctuations due to any variation in levitation height.

The proposed monitoring system can be implemented in cryogenic CMB polarimeters with modest impact on the cryogenic system and good scalability: it needs only two coaxial cables for the each static set of capacitor poles plus two coaxial cables for monitoring the resistive losses; it produces negligible dissipation on the HWP rotating assembly ($<0.1 \mu W$ per thermistor). The size of the coupling capacitor poles can be tailored to fit any HWP support ring, if this is wider than ~1 cm. The system operates correctly for any reasonable HWP rotation speed. We plan to install it in the forthcoming SWIPE instrument of LSPE¹³ and possibly in the MHFT (Medium High Frequency Telescope) instrument of LiteBIRD.

ACKNOWLEDGMENTS

This research was supported by the Italian Space Agency (ASI: LSPE and LiteBIRD contracts) and by the Italian National Institute for Nuclear Physics (INFN-LSPE activity).

The data that support the findings of this study are available from the corresponding author upon reasonable request.

REFERENCES

3C. M. Posada, P. A. R. Ade, A. J. Anderson, J. Avva, Z. Ahmed, K. S. Arnold, J. Austermann, A. N. Bender, B. A. Benson, L. Bleem, K. Byrum, J. E. Carlstrom, F. W. Carter, C. Chang, H.-M. Cho, A. Cukierman, D. A. Czaplewski, J. Ding, R. N. S. Divan, T. de Haan, M. Dobbs, D. Dutcher, W. Everett, R. N. Gannon, R. J. Guyser, N. W. Halverson, N. L. Harrington, K. Hattori, J. W. Henning, G. C. Hilton, W. L. Holzapfel, N. Huang, K. D. Irwin, O. Jeong, T. Khaire, M. Korman, D. L. Kubik, C.-L. Kuo, A. T. Lee, E. M. Leitch, S. L. Escudero, S. S. Meyer, C. S. Miller, J. Montgomery, A. Nadolski, T. J. Natoli, H. Nguyen, V. Novosad, S. Padin, Z. Pan, J. E. Pearson, A. Rahlin, C. L. Reichardt, J. E. Ruhl, B. Saliwanchik, I. Shirley, J. T. Sayre, J. A. Shariff, E. D. Shirokoff, L. Stan, A. A. Stark, J. Sobrin, K. Story, A. Suzuki, Q. Y. Tang, R. B. Thakur, K. L. Thompson, C. E. Tucker, K. Vanderlinde, J. D. Vieira, G. Wang, N. Whitehorn, V. Yefremenko, and K. W. Yoon, Proc. SPIE 9914, 290-300 (2016).

⁴R. O'Brient, P. Ade, K. Arnold, J. Edwards, G. Engargiola, W. Holzapfel, A. T. Lee, X.-f. Meng, M. Myers, G. Rebeiz, P. Richards, H. Spieler, A. Suzuki, and H. T. Tran, AIP Conf. Proc. 1185, 502-505 (2009).

⁵F. Columbro, P. G. Madonia, L. Lamagna, E. S. Battistelli, A. Coppolecchia, P. de Bernardis, R. Gualtieri, S. Masi, A. Paiella, F. Piacentini, G. Presta, M. Biasotti, G. D'Alessandro, F. Gatti, L. Mele, and B. Siri, J. Low Temp. Phys. 199, 312-319 (2020)

⁶P. A. R. Ade, R. W. Aikin, M. Amiri, D. Barkats, S. J. Benton, C. A. Bischoff, J. J. Bock, J. A. Bonetti, J. A. Brevik, I. Buder, E. Bullock, G. Chattopadhyay, G. Davis, P. K. Day, C. D. Dowell, L. Duband, J. P. Filippini, S. Fliescher, S. R. Golwala, M. Halpern, M. Hasselfield, S. R. Hildebrandt, G. C. Hilton, V. Hristov, H. Hui, K. D. Irwin, W. C. Jones, K. S. Karkare, J. P. Kaufman, B. G. Keating, S. Kefeli, S. A. Kernasovskiy, J. M. Kovac, C. L. Kuo, H. G. LeDuc, E. M. Leitch, N. Llombart, M. Lueker, P. Mason, K. Megerian, L. Moncelsi, C. B. Netterfield, H. T. Nguyen, R. O'Brient, R. W. O. IV, A. Orlando, C. Pryke, A. S. Rahlin, C. D. Reintsema, S. Richter, M. C. Runyan, R. Schwarz, C. D. Sheehy, Z. K. Staniszewski, R. V. Sudiwala, G. P. Teply, J. E. Tolan, A. Trangsrud, R. S. Tucker, A. D. Turner, A. G. Vieregg, A. Weber, D. V. Wiebe, P. Wilson, C. L. Wong, K. W. Yoon, and J. Zmuidzinas, Astrophys. J. 812, 176 (2015).

⁷H. McCarrick, G. Jones, B. R. Johnson, M. H. Abitbol, P. A. R. Ade, S. Bryan, P. Day, T. Essinger-Hileman, D. Flanigan, H. G. Leduc, M. Limon, P. Mauskopf, A. Miller, and C. Tucker, Astron. Astrophys. 610, A45 (2018).

⁸S. Masi, P. de Bernardis, A. Paiella, F. Piacentini, L. Lamagna, A. Coppolecchia, P. A. R. Ade, E. S. Battistelli, M. G. Castellano, I. Colantoni, F. Columbro, G. D'Alessandro, M. D. Petris, S. Gordon, C. Magneville, P. Mauskopf, G. Pettinari, G. Pisano, G. Polenta, G. Presta, E. Tommasi, C. Tucker, V. Vdovin, A. Volpe, and D. Yvon, J. Cosmol. Astropart. Phys. 2019, 003.

⁹A. Paiella, A. Coppolecchia, L. Lamagna, P. A. R. Ade, E. S. Battistelli, M. G. Castellano, I. Colantoni, F. Columbro, G. D'Alessandro, P. de Bernardis, S. Gordon, S. Masi, P. Mauskopf, G. Pettinari, F. Piacentini, G. Pisano, G. Presta, and C. Tucker, J. Cosmol. Astropart. Phys. 2019(1), 039, arXiv:1810.00598 [astroph.IM].

¹⁰H. Sugai, P. A. R. Ade, Y. Akiba, D. Alonso, K. Arnold, J. Aumont, J. Austermann, C. Baccigalupi, A. J. Banday, R. Banerji, R. B. Barreiro, S. Basak, J. Beall, S. Beckman, M. Bersanelli, J. Borrill, F. Boulanger, M. L. Brown, M. Bucher, A. Buzzelli, E. Calabrese, F. J. Casas, A. Challinor, V. Chan, Y. Chinone, J.-F. Cliche, F. Columbro, A. Cukierman, D. Curtis, P. Danto, P. de Bernardis, T. de Haan, M. D. Petris, C. Dickinson, M. Dobbs, T. Dotani, L. Duband, A. Ducout, S. Duff, A. Duivenvoorden, J.-M. Duval, K. Ebisawa, T. Elleflot, H. Enokida, H. K. Eriksen, J. Errard, T. Essinger-Hileman, F. Finelli, R. Flauger, C. Franceschet, U. Fuskeland, K. Ganga, J.-R. Gao, R. Génova-Santos, T. Ghigna, A. Gomez, M. L. Gradziel, J. Grain, F. Grupp, A. Gruppuso, J. E. Gudmundsson, N. W. Halverson, P. Hargrave, T. Hasebe, M. Hasegawa, M. Hattori, M. Hazumi, S. Henrot-Versille, D. Herranz, C. Hill, G. Hilton, Y. Hirota, E. Hivon, R. Hlozek, D.-T. Hoang, J. Hubmayr, K. Ichiki, T. Iida, H. Imada, K. Ishimura, H. Ishino, G. C. Jaehnig, M. Jones, T. Kaga, S. Kashima, Y. Kataoka, N. Katayama, T. Kawasaki, R. Keskitalo, A. Kibayashi, T. Kikuchi, K. Kimura, T. Kisner, Y. Kobayashi, N. Kogiso, A. Kogut, K. Kohri, E. Komatsu, K. Komatsu, K. Konishi, N. Krachmalnicoff, C. L. Kuo, N. Kurinsky, A. Kushino, M. Kuwata-Gonokami, L. Lamagna, M. Lattanzi, A. T. Lee, E. Linder, B. Maffei, D. Maino, M. Maki, A. Mangilli, E. Martínez-González, S. Masi, R. Mathon, T. Matsumura, A. Mennella, M. Migliaccio, Y. Minami, K. Mistuda, D. Molinari, L. Montier, G. Morgante, B. Mot, Y. Murata, J. A. Murphy, M. Nagai, R. Nagata, S. Nakamura, T. Namikawa, P. Natoli, S. Nerval, T. Nishibori, H. Nishino,

¹D. Baumann and H. V. Peiris, Adv. Sci. Lett. 2, 105 (2009).

²K. D. Irwin and G. C. Hilton, "Transition-edge sensors," in Cryogenic Particle Detection, edited by C. Enss (Springer Berlin Heidelberg, Berlin, Heidelberg, 2005), pp. 63-150.

Y. Nomura, F. Noviello, C. O'Sullivan, H. Ochi, H. Ogawa, H. Ogawa, H. Ohsaki, I. Ohta, N. Okada, N. Okada, L. Pagano, A. Paiella, D. Paoletti, G. Patanchon, F. Piacentini, G. Pisano, G. Polenta, D. Poletti, T. Prouvé, G. Puglisi, D. Rambaud, C. Raum, S. Realini, M. Remazeilles, G. Roudil, J. A. Rubiño-Martín, M. Russell, H. Sakurai, Y. Sakurai, M. Sandri, G. Savini, D. Scott, Y. Sekimoto, B. D. Sherwin, K. Shinozaki, M. Shiraishi, P. Shirron, G. Signorelli, G. Smecher, P. Spizzi, S. L. Stever, R. Stompor, S. Sugiyama, A. Suzuki, J. Suzuki, E. Switzer, R. Takaku, H. Takakura, S. Takakura, Y. Takeda, A. Taylor, E. Taylor, Y. Terao, K. L. Thompson, B. Thorne, M. Tomasi, H. Tomida, N. Trappe, M. Tristram, M. Tsuji, M. Tsujimoto, C. Tucker, J. Ullom, S. Uozumi, S. Utsunomiya, J. V. Lanen, G. Vermeulen, P. Vielva, F. Villa, M. Vissers, N. Vittorio, F. Voisin, I. Walker, N. Watanabe, I. Wehus, J. Weller, B. Westbrook, B. Winter, E. Wollack, R. Yamamoto, N. Y. Yamasaki, M. Yanagisawa, T. Yoshida, J. Yumoto, M. Zannoni, and A. Zonca, "Updated design of the CMB polarization experiment satellite LiteBIRD," J. Low Temp. Phys. (published online 2020), arXiv:2001.01724 [astro-ph.IM].

¹¹M. Salatino, P. de Bernardis, and S. Masi, Astron. Astrophys. **528**, A138 (2011). ¹²F. Columbro, E. S. Battistelli, A. Coppolecchia, G. D'Alessandro, P. de Bernardis, L. Lamagna, S. Masi, L. Pagano, A. Paiella, F. Piacentini, and G. Presta, Astron. Nachr. 340, 83 (2019).

¹³L. Lamagna, G. Addamo, P. A. R. Ade, C. Baccigalupi, A. M. Baldini, P. M. Battaglia, E. Battistelli, A. Bau', M. Bersanelli, M. Biasotti, C. Boragno, A. Boscaleri, B. Caccianiga, S. Caprioli, F. Cavaliere, F. Cei, K. A. Cleary, F. Columbro, G. Coppi, A. Coppolecchia, D. Corsini, F. Cuttaia, G. D'Alessandro, P. de Bernardis, G. D. Gasperis, M. D. Petris, F. D. Torto, V. Fafone, Z. Farooqui, F. Farsian, F. Fontanelli, C. Franceschet, T. Gaier, F. Gatti, R. Genova-Santos, M. Gervasi, T. Ghigna, M. Grassi, D. Grosso, F. Incardona, M. Jones, P. Kangaslahti, N. Krachmalnicoff, R. Mainini, D. Maino, S. Mandelli, M. Maris, S. Masi, S. Matarrese, A. May, P. Mena, A. Mennella, R. Molina, D. Molinari, G. Morgante, F. Nati, P. Natoli, L. Pagano, A. Paiella, F. Paoness, A. Passerini, M. P. de Taoro, O. A. Peverini, F. Pezzotta, F. Piacentini, L. Piccirillo, G. Pisano, L. Polastri, G. Polenta, D. Poletti, G. Presta, S. Realini, N. Reyes, A. Rocchi, J. A. Rubino-Martin, M. Sandri, S. Sartor, A. Schillaci, G. Signorelli, M. Soria, F. Spinella, V. Tapia, A. Tartari, A. Taylor, L. Terenzi, M. Tomasi, E. Tommasi, C. Tucker, D. Vaccaro, D. M. Vigano', F. Villa, G. Virone, N. Vittorio, A. Volpe, B. Watkins, A. Zacchei, and M. Zannoni, "Progress report on the large scale polarization explore," J. Low Temp. Phys. (published online 2020).
¹⁴A. Mennella, P. Ade, G. Amico, D. Auguste, J. Aumont, S. Banfi, G. Barbaràn,

P. Battaglia, E. Battistelli, A. Baù, B. Bélier, D. Bennett, L. Bergé, J. Bernard, M. Bersanelli, M. Sazy, N. Bleurvacq, J. Bonaparte, J. Bonis, E. Bunn, D. Burke, D. Buzi, A. Buzzelli, F. Cavaliere, P. Chanial, C. Chapron, R. Charlassier, F. Columbro, G. Coppi, A. Coppolecchia, R. D'Agostino, G. D'Alessandro, P. Bernardis, G. Gasperis, M. Leo, M. Petris, A. Donato, L. Dumoulin, A. Etchegoyen, A. Fasciszewski, C. Franceschet, M. Lerena, B. Garcia, X. Garrido, M. Gaspard, A. Gault, D. Gayer, M. Gervasi, M. Giard, Y. Héraud, M. Berisso, M. González, M. Gradziel, L. Grandsire, E. Guerard, J. Hamilton, D. Harari, V. Haynes, S. Versillé, D. Hoang, N. Holtzer, F. Incardona, E. Jules, J. Kaplan, A. Korotkov, C. Kristukat, L. Lamagna, S. Loucatos, T. Louis, A. Lowitz, V. Lukovic, R. Luterstein, B. Maffei, S. Marnieros, S. Masi, A. Mattei, A. May, M. McCulloch, M. Medina, L. Mele, S. Melhuish, L. Montier, L. Mousset, L. Mundo, J. Murphy, J. Murphy, C. O'Sullivan, E. Olivieri, A. Paiella, F. Pajot, A. Passerini, H. Pastoriza, A. Pelosi, C. Perbost, M. Perciballi, F. Pezzotta, F. Piacentini, M. Piat, L. Piccirillo, G. Pisano, G. Polenta, D. Prêle, R. Puddu, D. Rambaud, P. Ringegni, G. Romero, M. Salatino, A. Schillaci, C. Scóccola, S. Scully, S. Spinelli, G. Stankowiak, M. Stolpovskiy, F. Suarez, A. Tartari, J. Thermeau, P. Timbie, M. Tomasi, S. Torchinsky, M. Tristram, C. Tucker, G. Tucker, S. Vanneste, D. Viganò, N. Vittorio, F. Voisin, R. Watson, F. Wicek, M. Zannoni, and A. Zullo, Universe 5, 42 (2019).

¹⁵T. Essinger-Hileman, A. Kusaka, J. W. Appel, S. K. Choi, K. Crowley, S. P. Ho, N. Jarosik, L. A. Page, L. P. Parker, S. Raghunathan, S. M. Simon, S. T. Staggs, and K. Visnjic, Rev. Sci. Instrum. 87, 094503 (2016).

¹⁶B. R. Johnson, F. Columbro, D. Araujo, M. Limon, B. Smiley, G. Jones, B. Reichborn-Kjennerud, A. Miller, and S. Gupta, Rev. Sci. Instrum. 88, 105102 (2017).

¹⁷F. Columbro, P. de Bernardis, and S. Masi, Rev. Sci. Instrum. 89, 125004

¹⁸Y. Sakurai, T. Matsumura, T. Iida, H. Kanai, N. Katayama, H. Imada, H. Ohsaki, Y. Terao, T. Shimomura, H. Sugai, H. Kataza, R. Yamamoto, and S. Utsunomiya, IEEE Trans. Appl. Supercond. 28, 1 (2018).

¹⁹See https://www.comsol.com/ for details on the COMSOL software.

 $^{\mathbf{20}}$ F. Columbro, "The search for primordial B-modes in the polarization of the cosmic microwave background with LSPW/SWIPE and LiteBIRD," Ph.D. thesis, Sapienza, University of Rome, Italy, 2020.

²¹Y. Sekimoto, P. Ade, K. Arnold, J. Aumont, J. Austermann, C. Baccigalupi, A. Banday, R. Banerji, S. Basak, S. Beckman, M. Bersanelli, J. Borrill, F. Boulanger, M. L. Brown, M. Bucher, E. Calabrese, A. Challinor, Y. Chinone, F. Columbro, A. Cukierman, D. Curtis, P. de Bernardis, M. de Petris, M. Dobbs, T. Dotani, L. Duband, A. Ducout, K. Ebisawa, T. Elleflot, H. Eriksen, J. Errard, R. Flauger, C. Franceschet, U. Fuskeland, K. Ganga, J. Gao, T. Ghigna, J. Grain, A. Gruppuso, N. Halverson, P. Hargrave, T. Hasebe, M. Hasegawa, M. Hattori, M. Hazumi, S. Henrot-Versille, C. Hill, Y. Hirota, E. Hivon, D. T. Hoang, J. Hubmayr, K. Ichiki, H. Imada, H. Ishino, G. Jaehnig, H. Kanai, S. Kashima, Y. Kataoka, N. Katayama, T. Kawasaki, R. Keskitalo, A. Kibayashi, T. Kikuchi, K. Kimura, T. Kisner, Y. Kobayashi, N. Kogiso, K. Kohri, E. Komatsu, K. Komatsu, K. Konishi, N. Krachmalnicoff, C. L. Kuo, N. Kurinsky, A. Kushino, L. Lamagna, A. T. Lee, E. Linder, B. Maffei, M. Maki, A. Mangilli, E. Martinez-Gonzalez, S. Masi, T. Matsumura, A. Mennella, Y. Minami, K. Mistuda, D. Molinari, L. Montier, G. Morgante, B. Mot, Y. Murata, A. Murphy, M. Nagai, R. Nagata, S. Nakamura, T. Namikawa, P. Natoli, T. Nishibori, H. Nishino, F. Noviello, C. O'Sullivan, H. Ochi, H. Ogawa, H. Ogawa, H. Ohsaki, I. Ohta, N. Okada, G. Patanchon, F. Piacentini, G. Pisano, G. Polenta, D. Poletti, G. Puglisi, C. Raum, S. Realini, M. Remazeilles, H. Sakurai, Y. Sakurai, G. Savini, B. Sherwin, K. Shinozaki, M. Shiraishi, G. Signorelli, G. Smecher, R. Stompor, H. Sugai, S. Sugiyama, A. Suzuki, J. Suzuki, R. Takaku, H. Takakura, S. Takakura, E. Taylor, Y. Terao, K. L. Thompson, B. Thorne, M. Tomasi, H. Tomida, N. Trappe, M. Tristram, M. Tsuji, M. Tsujimoto, S. Uozumi, S. Utsunomiya, N. Vittorio, N. Watanabe, I. Wehus, B. Westbrook, B. Winter, R. Yamamoto, N. Y. Yamasaki, M. Yanagisawa, T. Yoshida, J. Yumoto, M. Zannoni, and A. Zonca, Proc. SPIE 10698, 106981Y (2018).

²²CERNOXTM is a trademark of Lake Shore Cryotronics, Inc.

²³See https://www.minicircuits.com/pdfs/MAR-8A+.pdf for the complete datasheet of the component.

²⁴See https://www.analog.com/media/en/technical-documentation/data-sheets/ AD8361.pdf for the complete data-sheet of the component.

²⁵L. Mele, P. Ade, J. G. Alberro, A. Almela, G. Amico, L. H. Arnaldi, D. Auguste, J. Aumont, S. Azzoni, S. Banfi, E. Battistelli, A. Bau', B. Belier, D. Bennett, L. Berge, J.-P. Bernard, M. Bersanelli, M.-A. Bigot-Sazy, N. Bleurvacq, J. Bonaparte, J. Bonis, A. Bottani, E. Bunn, D. Burke, D. Buzi, F. Cavaliere, P. Chanial, C. Chapron, R. Charlassier, F. Columbro, A. Coppolecchia, G. D'Alessandro, P. de Bernardis, G. D. Gasperis, M. D. Leo, M. D. Petris, S. Dheilly, L. Dumoulin, A. Etchegoyen, A. Fasciszewski, L. Ferreyro, D. Fracchia, C. Franceschet, M. G. Lerena, K. Ganga, B. Garcia, M. G. Redondo, M. Gaspard, D. Gayer, M. Gervasi, M. Giard, V. Gilles, Y. Giraud-Heraud, M. G. Berisso, M. Gonzalez, M. Gradziel, L. Grandsire, J.-C. Hamilton, D. Harari, S. Henrot-Versille, D. Hoang, F. Incardona, E. Jules, J. Kaplan, C. Kristukat, L. Lamagna, S. Loucatos, T. Louis, B. Maffei, S. Marnieros, W. Marty, S. Masi, A. Mattei, A. May, M. McCulloch, S. Melhuish, A. Mennella, L. Montier, L. Mousset, L. M. Mundo, J. A. Murphy, J. Murphy, F. Nati, E. Olivieri, C. Oriol, C. O'Sullivan, A. Paiella, F. Pajot, A. Passerini, H. Pastoriza, A. Pelosi, C. Perbost, M. Perciballi, F. Pezzotta, F. Piacentini, M. Piat, L. Piccirillo, G. Pisano, M. Platino, G. Polenta, D. Prele, R. Puddu, D. Rambaud, P. Ringegni, G. E. Romero, M. Salatino, J. Salum, A. Schillaci, C. Scoccola, S. Scully, S. Spinelli, G. Stankowiak, M. Stolpovskiy, A. Tartari, J.-P. Thermeau, P. Timbie, M. Tomasi, S. Torchinsky, M. Tristram, G. Tucker, C. Tucker, D. Vigano', N. Vittorio, F. Voisin, F. Wicek, M. Zannoni, and A. Zullo, "The QUBIC instrument for CMB polarization measurements," J. Phys.: Conf. Ser.

²⁶G. D'Alessandro, L. Mele, F. Columbro, L. Pagano, F. Piacentini, P. de Bernardis, and S. Masi, Astron. Astrophys. 627, A160 (2019).